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Ingenious COCKER! (Non to Rest thou 't Gond Noe Art can Show they fully but theme own Thy rare Arithmetick alone can show The vast Sound of Thanks wee for the Laboure

de Cocker's

ARITHMETICK

BEING

A plain and familiar Method, fuitable to the meanest Capacity for the full understanding of that Incomparable Art, as it is now taught by the ablest School-Masters in City and Country.

COMPOSED

By Edward Cocker, late Practitioner in the Arts of VVriting, Arithmetick, and Engraving. Being that so long since promised to the World.

PERUSED and PUBLISHED

By John Hawkins Writing-Master near St. Georges Church in Southwark, by the Authors correct Copy, and commended to the World by many eminent Mathematicians and Writing-Masters in and near London.

The Two and Twentieth Edition carefully Corrected, with Additions.

Licensed Sept. 3. 1677. Roger L'Estrange.

LONDON

Printed by W. Richardson, for Eben. Tracey, at the Three Bibles on London-Bridge. 1702.

50.0.10

TO his much Honoured Friends, Manwaring Davies of the Inner Temple, Esquire, and Mr. Humpbry Davies of St. Mary Newington Butts, in the County of Surry.

John Hawkins, As an Acknowledgment of Unmerited Favours, humbly Dedicateth this Manual of

Arithmetick.

Allo Walling

A 3

To

To the READER.

Courteous Reader.

Having the Happiness of an Intimate Acquaintance with Mr. Cocker in his Lifetime, often folicited him to remember his Promise to the World, of Publishing his Arithmerick, but (for Reasons belt known to himself) he refused it; and (after his Death) the Copy falling accidentally into my Hands, I thought it not convenient to smother a Work of so confiderable a moment, not questioning but it might be as kindly accepted as if it had been presented by his own Hand. The Method is familiar and easie, discovering as well the Theorick as the Practice of that Necessary Art of Yulgar Arithmetick : And in this new Edition there are many remarkable Alterations for the benefit of the Teacher or Learner, which I hope will be very acceptable to the World: I have also performed my promile in Publishing the Decimal Arithmetick, which finds Encouragement to my Expectation, and the Booksellers too, I am,

Thine to serve thee,

John Hawkins.

Mr.

Mr. Edward Cocker's

PROEME or PREFACE.

The sacred Influence of Divine Providence, I have been Instrumental to the benefit of many; by vertue of those useful Arts, Writing and Engraving: And do now with the same wonted atacrity cass this my Arithmetical Mite into the Publick Treasury, beseeching the Almighty to grant the like Blessing to these as to my former Labours.

Seven Sciences supremely excellent,
Are the chief Stars in Wisdoms Firmament,
Whereof Arithmetick is one, whose worth
The Beams of Prosit and Delight shines forth;
Ton crowns the rest; this makes Man's Mind complete;
This treats of Numbers, and of this we treat.

I have been often desired by my intimate. Friends to publish something on this Subject; who in a pteasing Freedom have signified to me that they expected it would be extraordinary. How far I have answered their Expectation. I know not; but this I know, that I have defigned this Work not extraordinary abstrase or profound,

The Proeme or Preface.

profound, but have by all means possible mithin the Circumference of my Capacity, endeavoured to render it extraordinary useful to all those, whose Occasions shall induce them to make use of Number, If it be objected that the Books already published, treating of Numbers, are innumerable; I Answer, that's but a small Wonder, since the Art is infinite. But that there should be so many excellent Tracts of Practical Arithmetick extant, and so little practised, is to me a greater wonder; knowing that as Mer-chandise is the Life of the Weal-Publick, so Practical Arithmetick is the Soul of Marchandize. Therefore I do ingenuously profess, that in the beginning of this Undertaking, the memerous Concords of the honoured Merchants first possessed my Consideration: And how far I have accommodated this Composure for his most worthy Service, let his own profitable Experience be judge.

Secondly, For your Service, most excellent Professors, whose Wonderstandings foar to the Sublimity of the Theory and Practice of this No-blew Science, may this Arithmetical Frustate composed; which you may please to implay as a Moustor to instruct your young Tyxoes; and thereby take occasion to reserve your precious Moments, which might be exhausted that way, for your more important Assains.

Thirdly,

The Proeme or Preface.

Thirdly, For you, the ingenious Off-spring of happy Parents, who will willingly pay the full Price of Industry and Exercise for those Arts and choice Accomplishments which may contribute to the Felicity of your suture State. For you, I say, (ingenious Practitioners) was this Work composed, which may prove the Pleasure of your south, and the Glory of your Age.

Lastly, For you the pretended Numerists of this vapouring Age, who are more disingeniously witty to propound unnesessary Questions, than ingeniously judicious to resolve such as are necessary. For you was this Book composed and published, if you will deny your selves so much as to invert the streams of your Ingenuity, and by studiously conferring with the Notes, Names, Orders, Progress, Species, Properties, Proprieties, Proportions, Powers, Affections and Apptications of Numbers delivered herein, become such Artists indeed, as you now only seem to be. This Arithmetick ingeniously observed, and diligently practised, will turn to good account to all that shall be concerned in Accompts. All whose Rules are grounded on Verity, and deliver'd with Sincerity. The Examples are built up gradually from the smallest Consideration to the greatest. All the Problems or Propositions are well weighed, pertinent and clear, and not one

The Proeme or Preface. of them throughout the Trast taken upon trust; therefore now,

Zoilus and Momus lie you down and dye, For these Inventions your whole force desie.

Edmard Cocker.

Courteous

Courteous Reader,

DEing well Acquainted with the deceased D Author, and finding him knowing and studions in the Mysteries of Numbers and Algebra, of which he had some choice Manuscripes, and a great Collection of Printed Authors in Several Languages, I doubt not but he hath writ his Arithmetick suitable to bis own Preface, and worthy acceptation; which I thought to certifie on a Request to that purpose made to him that wisheth thy Welfare, and the Progress of Arts.

John Collens.

November 27th, 1677.

This Manual of Arithmetick is recommended to the World by Us whose Names are subferibod, viz.

Mr. John Collens Mr. James At-Matth. kinson Mr. Peter Perkins

Mr. Rich. Laurence, Senior Mr. Eleazer Wigan

Mr. Rich. Noble of Guilford Mr. William Norgate

Mr. William Mason Mr. Steph. Thomas

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Mr. Joseph Symmonds Mr. Jerem. Milles

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Mc. Foliah Cufley Mr. John Hawkins

And generally Approved by all Ingenious Artifts.

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Notation of Numbers.

Rithmetick is an Art of Numbring or Know-ledge, which teacheth to number well, (viz.) the Doctrine of Accounting by Numbers. And there are divers Species and Kinds of Arithmetick and Geometry, the which we do intend to treat of in order; applying the Principles of the one to the Definitions of the other: For as Magnitude or Greatness is the subject of Geometry, so Multitude or Number is the subject of Arithmetick; and if then their first Principles and chief Fundamentals, must have like Definitions; or at least, a Semblable Congruency.

2. Number is that by which the Quantity of any thing is expressed or numbered; as the Unit is the number by which the quantity of one thing is expressed or said to be one, and two by which it is named two, and \frac{1}{2} half by which it is named or called half; and the Root of \(2, \) by which it is called the Root of \(2, \) the

like of any other.

3. Hence it is that Unit is Number, for the part is of the same matter that is his whole, the Unit is part of the multitude of Units, therefore the Unit is of the same matter that is the multitude of Units; but the matter of the multitude of Units is Number, therefore the matter of Unit is Number; for else if from a given number no number be subtracted, the number given remaineth; let three be the number given; from which number subtract or take away one; (which as some conceive, is no number) therefore the

number given remaineth, that is to say, there remaineth three, which is absurd.

4. Hence it will be convenient to examine from whence Number hath its rife or beginning: Most Authers maintain that Unit is the beginning of Number. and it self no number; but looking upon the Principles and Definitions in the first Rudiments of Geometry, we shall find, that the definition of a Point is in no way congruous with the definition of an Unit in Arithmetick; and therefore one, or Unit must be in the bounds or limits of Number, and confequently the beginning of Number is not to be found in the Mumber one; wherefore to make number and magnitude congruent in Principles, and like in Definitions, we make and constitute a Cypher to be the beginning of number, or rather the medium between encreasing and decreasing Numbers, commonly called absolute or whole Numbers, and negative or fractional Numbers. between which nothing can be imagined more agreeable to the definition of a point in Geometry; for as a point is an adjunct number, and it self no line, so is (o) Cypher an adjunct of number, and it felf no number . And as a point in Geometry cannot be divided or increased into parts; so likewise (0) cannot be divided or increased into parts; for as many points though in number infinite do make no line, fo many (o) Cyphers, though in number infinite do make no number. For the line A B eannot be increased by the addition of the point C, neither can D the number D be increased by the E addition of the (o) Cypher E, for if you add nothing to 6, ſum the Sum will be 6, (6) neither increasing nor diminishing the number 6. but if it be granted that A B be extended or prolonged to the point C, so that A C be made E } 60 a continued line, then AB is increased by the addition of the point C, in like man-

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ner if we grant D 6 be prolonged to E(0) fo that D E (60) be a continued number making 60, then 6 is augmented by the aid of (0) as to the conflicting the approber (60) fixty; and furthermore that one or unit is material and a number, and that (0) is the beginning of number is proved by all Authors, altho' indirectly, for the Tables of Sines and Tangents prove one degree to the a number, because the Sine of 1 degree is 174524, (the Radius being 10000000) and the beginning of that Table is (0) and to it answereth 00000, Gre.

5. Hence it is that number is not quantity discontinued, for all that which is but one quantity, is not quantity disjunct, (60) fixty as it is a number, is one quantity, viz. one number (60) fixty; therefore as it is number, it is not quantity disjunct; for number is fome such thing in magnitude, as humidity in Water; for as humidity extends it felf through all and every part of Water, so number related to magnitude dota extend it self through all and every part of magnitude.

Also as to continued Water doth answer continued humidity, so to a continued magnitude doth answer a continued number. As the continued humidity of any intire Water, suffereth the same Division and distinction that his Water doth : so the continued Number suffereth the same division and distinction that his magnitude doth. From all which Confiderations we might enlarge a further digression concerning number and magnitude, by comparing the definitions of the one with the Principles of the other, for having found a (0) Cypher to be answerable in definition to a point in magnitude, we may very well conclude that number may be congruent to a line; as also the Figu-rative Number to be consonant in definition with a Superficies, and Solid, Gr. in the order of Geometrical Magnitudes.

6. The Characters or Notes by which Numbers are figuified, or by which a Number is ordinarily expressed are these following, (viz.) o Cypher or nothing, 1 One, 2 Two, 3 Three 4 Four, 5 Five, 6 Six, 7 Seven, 8 Right, 9 Nine: The Cypher, which though of it

felf fignifieth nothing, (viz.) expresset not any certain or known quantity, but is the beginning, Radix, or Root of Number, and the other nine Figures or Characters are led fignificant Figures or Digits.

7. In numbers of any fort, two things are to be con-

sidered, (viz.) Notation and Numeration.

8. Notation teacheth how to describe any number by certain Notes and Characters, and to declare the value thereof being so described, and that is by Degrees and Periods.

9. A degree confifts of three figures, viz. of three places comprehending Units, Tens and Hundreds, so 36; is a degree, and the first figure (5) on the right-hand, stands simply for its own value, being Units or so many ones, (viz.) sive; the second in order from the right, signifies as many times ten, as there are Units contained in it, (viz.) sixty; the third in the same order signifies so many hundreds as it contains Units, so will the expression of the Number be, three hundred sixty sive; also 789, is seven hundred eighty nine, syc.

10. A Period is when a Number confifts of more than three figures, or places, and whose proper order is to prick or distinguish every third place beginning at the right hand, and so on to the left; so the number 63452 being given, it will be distinguished thus, 63.452, and expressed thus, fixty three thousand four hundred fifty two, likewise 4.578.235.782, being distinguished as you see, will be expressed thus, sour thousand five hundred seventy eight millions, two hundred thirty five thousand, seven hundred eighty two.

11. Number is either Absolute or Negative.

12. An absolute, or intire, whole, increasing number, is that which by annexing of another Figure or Cypher it becomes ten times as much as it stood for before; and if two Figures or Cyphers be annexed, it makes it a hundred times more than it stood for betore, (3c. as if you annex to the figure 6 a Cypher, then it will become (60) fixty: So if two Cyphers are

annexed, then it will be (600) fix hundred, and if you do annex to it a (4) four, then it will be (64) fixty four; and if you annex (78) feventy eight, it will be then (678) fix hundred feventy eight, and to on: By annexing more Figures or Cyphers, it will encrease in

a decuple proportion ad Infinitum. 13. A Negative, or Broken, Fractional, Decreasing Number, is that which by prefixing a Point or Prick towards the left hand its value is decreased from so many Units, to fo many tenth parts of any thing, and if a point and (c) Cypher, or a Digit be prefixed, it will be then so many hundred parts, and if a point and two Cyphers or Digits be prefixed, its Value is decreafed to be so many thousand parts; as if you would prefix before the figure 3 a point (.) or prick thus (.3) it is then decreased from 3 Units or Integers, to (3) three tenth parts of an Unit or Integer; and if you prefix a Point and Cypher thus (.03) it is decreased from 3 Integers to 3 hundred parts of an Integer, and by this means 51. Absolute, by prefixing of a point will be decreased to 5 l. Negative, which is five tenth parts of a Pound, equal in value to ten Shillings, and fo by prefixing of more Cyphers or Digits, its value is decreased in a decuple proportion ad infinitum. the following Scheme, or rather order of Numbers, we have placed (o) Cypher in its due place and order, as it is both the beginning and medium of number; for going from (o) towards the left hand you deal with intire, absolute, whole, increasing Numbers.

| | | ng Nu | | | | | | iumber | | |
|------|--------------------------------|-------|------------------|--------------|-----|------------------|-------------------------|------------------------------|--------|--|
| unm) | 876 m m nmm nmm CX | CX | 256 mmm CX | Ź I C CXU | IXC | 345 mmm XC | 678 nmm nmm XC | 976 nmm mr Mr XC | 3) n n | |

But going from (o) the place of Units towards the right hand, you meet with broken, negative, fractional and decreasing Numbers. And hence it follows that

Multiplication encreaseth the product in absolute Numbers, but decreaseth the product in negative Numbers. Also Division decreaseth the Quotient in whole Numbers, and increaseth it in negative or fractional Numbers.

14. An absolute, entire, whole, increasing Number, hath always a point annexed towards the right hand;

and therefore,

15. A negative, broken, decimal, decreasing Number, hath always a point prefixed before it towards the left hand. When we express Integers or whole Numbers, as 5 pounds, 5 feet, 26 men, we usually annex a

1. feet men. inch.

point or prick after the number thus, 5. 5. 26. 347. But when we express Decimals, or Numbers that are denied to be entire, as decreasing Numbers, we do commonly prefix a point or prick before the said Decimal or decreasing Number, thus (3), that is 3 tenths, or 3 primes, .03, that is 3 hundredths, or 3 seconds.

16. A whole or absolute Number is an Unit, or a composed multitude of Units, and it is either a prime,

or eife a compounded Number.

17. Prime Numbers amongst themselves are those which have no multitude of Units for a common measurer as 8 and 7, or 10 and 13, because not any multitude of Units can equally measure or divide them without a Remainder.

18 Compound Numbers amongst themselves are those which have a multitude of Units for a common measurer, as 9 and 12, because 3 measures them exactly, and abbreviates them to 3, and

19. A broken Number commonly called a Fraction, is a part or parts of a whole Number, viz. a part of an Integer, as \(\frac{1}{2}\) one third, is one third part of an Unit.

20. A broken Number or Fraction, confifts of 2 parts,

viz. the Numerator and the Denominator.

21. The Numerator and Denominator of a Fraction, are fet one over the other, with a line between them; and the Numerator is fet above the line, and expressent the parts therein contained.

22. The

22. The denominator of a Fraction is the inferiour number placed below the line, and expressent the number of parts into which the Unit or Integer is divided; as let \$\frac{1}{4}\$ be the Fraction given, so shall \$\frac{1}{4}\$ be the humerator, and doth express or number the multitude of parts contained in this Fraction; for \$\frac{1}{4}\$ is a Fraction composed of Fourths or Quarters; and the figure \$\frac{1}{4}\$ in numbring shews us, that in that Fraction there are \$\frac{1}{4}\$ of those fourth parts or quarters; also in the same Fraction \$\frac{1}{4}\$, \$\frac{1}{4}\$ is the denominator, and doth express the quality of the Fraction, viz. that the whole, or Integer, is here divided into \$\frac{1}{4}\$ equal parts.

23. A broken number is either proper or improper, wix. proper, when the numerator is lefter than the denominator; so \(\frac{1}{2} \) is a perfect proper Fraction, but an improper Fraction hath its numerator greater, or at least equal to the denominator; thus \(\frac{1}{2} \) is an improper Fraction.

Chian, the Reason is given in the definition.

24. A proper broken number is either Simple or Compound, viz. Simple, when it hath one denomination; and Compound, when it confifeth of divers denominations. It \$1.\frac{1}{2},\frac{1}{1}\frac{1}{2}

25. When a fingle broken Number or Fraction hath for his denominator a number confiding of a Unit in the first place towards the left hand, and nothing but Cyphers from the Unit towards the right hand, it is then the more aptly and rightly called a Decimal Fraction; under this Head are all our decreasing Numbers placed, and in our 13th definition called Negative, and by that order there prescribed, we order them to be Decimals, by signing a point or prick before them, or the numerator rejecting the denominator: Therefore according

cording to our last Rule, $\frac{1}{15}$, $\frac{1}{15}$, $\frac{1}{15}$, $\frac{1}{15}$, $\frac{1}{15}$, are said to be Decimals; and a Decimal Fraction may be expressed without its denominator (as before) by prefixing a point or prick before the numerator of the said Fraction, and then shall the former Fraction $\frac{1}{15}$, and $\frac{1}{15}$, francthus. 5, and .25.

But oftentimes, as in the second and fourth Frallions 75. and 725., a prick or point will not do without the help of a Cypher or Cyphers prefixed before the agnificant figures of the numerator, and therefore when the numerator of a desimal Frallion, consistent not of so many places as the denominator hath Cyphers, fill up the void places of the numerator, with prefixing Cyphers before the significant Figures of the numerator, and then sign it for a decimal, so shall 75. be 105, and 725. will be 1025, and 725. will be 1025, and 725. will be 1025. Now by this we may easily discover the denominator having the numerator; for always the denominator of any decimal Frallion consists of so many Cyphers, as the numerator hath places, with a Unit prefixed before the said Cyphers, viz. under the point or prick.

26. A decimal Number or Fraction, is that which is expressed by Primes, Seconds, Toirds, Fourths, &c. and is number decreasing. Here instead of Natural and C. mmon Fractions, as 3 of a thing, we order the thing or integer into Primes, Seconds, Thirds, Fourths, Fifths, e.e. that our Expression may be consonant to our for

mer order.

27. In Decimal Arithmetick we always imagine (and it would be very commodious if it were really so) that all intire Units, Integers, and things are divided first into ten equal parts, and these parts so divided we call Primes; and secondly, we divide also each of the former Primes into other ten equal parts; and every of these divisions we call Seconds; and thirdly, we divide each of the said Seconds into ten other equal parts, and those so divided we call Thirds, and so by decimating the former, and sub-degimating these latter, we run on ad infinitum.

n on ad infinitum.
28. Let a pound sterling, Troy-weight, Averdus,

pois-weight, Liquid-Measure, Dry-Measure, Long-Measure, Time, Dozen, or any other thing, or integer be given to be decimally divided; in this notion premifed we ought to let the first Division be Primes, the next division Seconds, the next Thirds, &c. So one pound sterling being 20 shillings, which divided into ten equal parts, the value of each part will be 2 shillings; therefore one Prime of a pound sterling will stand thus (.1) which is in value 2 shillings, three Primes will fland thus (.3) and that is in value 6 shillings. Again, a Prime or . I being divided into ten equal parts, each of those parts will be one Second, and is thus expressed, (.01) and its value will be found to be 2 d. farthing, and of a farthing; and fo will .05 fignifie one shilling, or five Seconds. And if or be divided into ten other equal parts, each of those parts fo divided will be Inirds, and will stand thus :001, and its value will be found to be .96 of a farthing, or -95. of a farthing; and .009 Thirds will be 2d, and 64 of a farthing, or +24 of a farthing, Gr. So that .375 1. will be found to represent 7s. and 6d.; for the 3 Primes are is shillings, and the 7 Seconds are is. 4d. and 7 bf: a penny, and the & Thirds are i penny and 72 of a. penny, both which added together make 7 s. 8 d.

20. If you put any bulk or body, representing an. Integer if it be decimally divided, then the parts in the first decimation are Primes, the pent Seconds, and the next decimation is Thirds, the next Fourths, &c. As. let there beigiven a Bullet of Lead, on such like whose weight lettle bergo 45 Troy, this call an Unit, Integer, or: things; then with the like weight and matter, make 10 others the which together will be equal to 90 h, and will weigh canh of them & La piece, take of the same matter, and equal to gir make 10 more, then each of those will weigh o minceampiece; also if again, you... take of ounces, and thereof: make 10, other finall Bullets, each of them will weigh 12 penny-weight Troy; and, thus have you made Primes, Seconds, and Thirds, in respect of the Integer containing so I. Troy, and that s Primes is equal to the half mais, and a Primes and s Seconds is a quarter of the mass; and therefore I B Digitized by Google

of the first division, 2 of the second division, and 5 of the third division, will be equal in weight to 1 a quarter of the mass, and contain 6 l. and 2 ounces.

20. When a decimal Fraction followeth a whole number, you are to separate or part the decimal from the while number, by a point or prick; so if .75 followed the whole number 32, set them thus 32.75. You shall find that divers Authors have divers ways in expressing mixt numbers, as thus, 32/75, or 32775, or 32.75, or 32/75, or 32375, but you will find that 32.75 thus placed and expressed is fittest for Calculation.

21. A mixt number hath 2 parts, the whole and the broken; the whole is that which is composed of Integers, and the broken is a Fraction annexed thereunto. So the mixt number 36-\$ being given, we fay that 36 is the whole number, which is composed of Integers and the - is the broken number annexed, which sheweth that one of the former integers (of that 36) being divided into 12 parts, this T, doth express 8 of those 12 parts more belonging to the faid 36 Integers.

22. Demominative numbers are of one, or of many, and those are of divers forts and kinds, viz. Singular, called Unit, as 1; and Plural, called multitude; as 2, 3, 4, 5. Single of one kind only, called digits; as 1, 2, 3, 4, 5, 6, 7, 8, 9, and Compounds of many, 10, 11,

12. (cc. 102, 369, Cc.

Proportional, as Single, Multiple, Double, Triple, Quadruple, Gc. Denominate, as Pounds, Shillings, Pence ; Undenominate, as 1, 2, 3, 6%. Perfect, as 6, 28, 496; 8128, 130816, 2096128, 6%. whose parts are equal to the numbers; Imperfect, unequal and more than the sum, as 12 to 1, 2, 3, 4, 6. Imperfect, unequal and less than the sum, as 8 to 1, 2, 4. Numbers Commenfurable and Incommenfurable, as 12 and 9 are Commensurable, because 3 measures them both.

But 6 and 17 are Incommensurable, because no one common number or measure can measure them Lincar in form of a Line, as Superficial in form of a Superficies or Plane, as:::, or ::, &c. and num-

ber cubical or folid in form of a Cube. These two latter are otherwise called figurative Numbers: There are also other Numbers called Tabular, as Sines, Tangents, Secants, &c. Others that be called Logarithms or borrowed Numbers, fitted to proportion for ease and speedy Calculation of all manner of Question.

CHAP. II.

Of the Natural Division of Integers, and the several Denominations of the Parts.

I. Defore we come to Calculation or the ordering of Numbers to operate any Arithmetical Question proposed, we will lay down Tables of the denomination of several Integers; and after that (having mentioned the several species or kinds of Arithmetick) we shall immediately handle the species of Numeration, which are the main Pillars upon which the whole Fabrick of this Art is built.

Of Money, Weights, &c.

2. The least Denomination or Fraction of Money used in England is a Farthing, from whence is produced the following Table, called the Table of Corn, viz.

And therefore

4 Farth.
4 Farth.
12 Pence
20 Shill.

And therefore
1 Farthing L 4. d. qrs.
1 Penny 1 —20—12—4
1—20—240—960
1—12—48

The first of these Tables, viz. that on the left hand, is plain and easie to be understood, and therefore wants

no directions. In the second Table above the line you have 1 l. 20 s. 12 d. 4 grs. whereby is meant that I pound is equal to 20 shillings, and one shilling is equal to 12 pencey and one penny is equal to 4 farthings; under the line is 1 l. 20 s. 240 d. 960 grs. which signifies one pound to contain 20 shillings, or 240 pence, or 960 farthings; in the second line below that 1 s. 12 d. 48 grs. the first standing under the denomination of Shillings, whereby is to be noted that one shilling is equal to 12 pence, or 48 farthings, and likewise that below that, one penny is equal in value to sour farthings; understand the like reason in 21 the following Tables of Weight, Measure, Time, Motion and Dozen.

Of Troy Weight.

The least Fraction or Denomination of Weight used in England, is a grain of Wheat gathered out of the middle of the Err, and well dried; from whence are produced these following Tables of Weight, called Iroj-weight.

32 Grains of Wheat
24 Artificial Grains
20 Penny-weight
12 Ounces

21 Penny-weight
12 Pound Troy-weight
12 Pound Troy-weight

And therefore,

| , C 63 | | | |
|--------------|-------------------------------------|----------|----------------|
| . / | . oun- | p.w. | grain s |
| | والشنشنة والسنادة | 20 | 24 |
| L37 = | | . دسائست | |
| A second | 12-1 | 240 | - 4760 |
| - | | | 480 |
| 100 | | | 400 |
| 7.5 | رسه ا رد د درواند | 20 | 480 |

Troy-weight serveth only to weigh Bread, Gold, Silver, and Electivaries, with also regulate the and prescribeth in Formation to keep the Money of England at a certain standard

standard. The Goldiniths have divided the ounce Trop-weight into other parts, which they generally call, Mark weight; the denominative parts thereof are as followeth, viz. A Mark (being an ounce Troy) is divided into 24 equal parts, called Carells, and each Carest into 4 grains, so that in a Mark are 96 Grains; by this weight they difting the different finencis of their Gold; for if to the finencis of Gold be put 2 Carects of Alloy (which is of Silver, Copper, or other baker Metal, with which they are to mix their Gold or Silver to abate the faceness thereof) both making when cold but an ounce, or 24 Carects, then this Gold is faid to be 22 Carects fine, for if it come to be refined the 2 Carects of alloy will the away, and leave only 22 Carects of pure Gold, the like to be considered of a greater or leffer quantity; and as the finences of Gold is estimated by Carects, so the finences of Silver is distinguished by ounces; for if a pound of it be pure, and loseth nothing in the Refining, such Silver is said to be twelve ounces fine; but if it loseth any thing, it is said to contain fo much finenels as the loss wanteth of 12 ounces, as if it lose an ounce, it is said to be II ounces fine, and if it lose one ounce 14 penny-weight, then it is faid to be 10 ounces of penny-weight fine, and that which loseth 2 ounces 4 penny-weight 10 grains, is said to be 9 ounces 15 penny-weight 8 grains fine, &c. the like of a greater or leffer quantity. Of Apothecaries Weights.

4. The Apothecaries have their Weights deduc'd from Troy-weight, a pound Troy being the greatest Integer, a Table of whose division and sub-division followeth,

| I | pound) | Si 2 ounces | And therefore, [l. oun. drams fernp. gr. 1-12-8-3-20 |
|---|---------|--------------|--|
| I | dram(g |) z seruples | 1-12-96-288-5760 |
| I | scrup.) | 20 grains | 1- 8- 24- 480 |
| - | | | 15-3-50 |

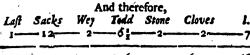
5. Thus much concerning Troy-weight, and its derivative weights (which as was faid before) ferveth to weigh Bread, Gold, Silver, and Electuaries; now besides Troy-weight there is another kind of weight used in England, commonly known by the name of Averdupois-weight (a pounded which is equal to 14 ounces 12 penny-weight The weight) and it serveth to weigh all kinds of Grocery-Wares, as also Butter, Cheefe, Flesh, Wax, Tallow, Rosin, Pitch, Lead, and all such kind of Garble, the Table of which weight is as followeth.

14

```
The Table of Averdupois-weight.
 4 quarters of a dram
                           1 dram
16 drams
                          I sunce
16 ounces
                          I pound
                          1 quarter of a bundred
1 bundred mei. or 112 l.
28 pounds
 4 quarters
20 bundred
                 And therefore.
                                dra.
                -28--- 16-
  1-20-80-2240-35840-573440-2293760
1-4-112-1792-28672-114688
           1-28-448-7168-28672
```

Wooll is weighed with this Weight, but only the Divitions are not the same; A Table whereof followeth.

A Table of the denominative parts of Woell-weight.
7 pounds
2 cloves
2 flones
6 todd 1 flone
2 meys
12 facks
1 laft



-24- 156-212---624- 4468 -13- 26- 52-364 26-

Note, that in some Counties, the Wey is 256 l. Averdupois, as is the Suffolk Wey; but in Effex there is

226 l. in a Wey.

6. The least denominative part of Liquid Measure is a pint, which was formerly taken from Troy weight, (a pound of Wheat Troy weight making I pint of liquid Measure) but in regard of the difference between the Brewers and the Farmers of His Majesty's Excise concerning the gauging of Vessels occasion'd by the different Opinions of Artists, concerning the folid inches in a Gallon, it was lately decided by Act of Parliament, the Statute making 282 folid Inches in a Beer Gallon, and 231 in a Wine-measure, and consequently the pint Beer-measure to contain 35% solid Inches, and the pint Wine-measure to contain 28% cubical or solid Inches; from whence is drawn the following Table.

| The T | able of Liqui | d Measure. |
|--------------------|---------------|-------------------------------|
| 35% cubical Inches |) (| 1 pint beer-measure |
| 28% cubical Inches | | 1 pint wine-measure |
| 2 pints | ' ! I | 1 quart |
| 2 quarts | | r pettle |
| 2 potiles ···· | - 1 | 1 gallon |
| 8-gallons | | 1 firk. of ale, foap or berr. |
| 9 gallons | | 1 firk of beer |
| 10 gallons and a l | alf PAS | i firk of Salmon or Eels |
| 2 firkins | - 1 - 1 - 1 | 1 kilderkin |
| 2 kilderkins | | a barrel |
| 42 gallons | | 1 Tierce of wine |
| 63 gallons | 1 1 | n boelbead |
| 2 bogsbeads | | I pipe or buts |
| a pines or butts | | 1 tun of wine And |

| And therefore, | | | | |
|----------------|---|--------------|-----------------|------|
| Tun | | | 63 | |
| - | | | - 03 | 8 |
| 1 | 2 | 4 | - 252 -126 | 2016 |
| | 1 | | | |
| | | 1 | - 63 | |
| | | | ı — | 8 |

7. The least denominative part of Dry-Measure is also a pint, and this is likewise taken from Troy-weight. The Table of whose division followeth.

The Table of Dry-Measure.

| | pound Troy | |) | [] fint. |
|---|------------|-----|-------------------|------------|
| 2 | pints | · . | } | I quart |
| 2 | quarts | | 1 | I pottle |
| 2 | potites | | | 1 gallon: |
| 2 | gallons | : ; | ای | 1 peck. |
| 4 | pecks | | .> ` } | I bushel |
| 4 | bushels | / | i, E | 1 comb |
| 2 | combs | | <u>-</u> -i | I quarter |
| 4 | quarters | | 1. | 1 chaldron |
| 5 | quarters | 2.4 | 1 | 1 wey |
| | meys | | ر راز | l last |

And therefore,

| last | wey q | rs. com. | bush. | pecks | gall. | pints |
|------|-------|----------|-------|-------|----------------------------|-------|
| | | | | | | |
| | | | | | -640- | |
| . É. | 1— | | | | ~38¢~ | |
| | | | | | — 64— — 32 ~ | |
| | ٠, | • | - | | 8- | |
| | • | | - | , i | <u> </u> | - 16 |
| | 4 | | - | | 1 | 8 |

8. The

8. The least denominative part of Long Measure is a Barly-corn well dried, and taken out of the middle of the Ear; whose Table of parts followeth:

The Tuble of Long Measure.

```
3 barly-corns
12 inches
3 feet
3 feet 9 inches, or a
yard and quarter
6 feet
5 yards and a half
40 poles or perches
8 furlongs
```

And therefore,

| mile | furl. poles | yards feet | inches | barly-corns |
|------|-------------|--|--------|-------------|
| 1- | - 8 40- | -5 ¹ -3- | | |
| , I~ | | -1760-5280- | -63360 | 190080 |
| | | - 220 660- 4 ¹ 16 ¹ | | |
| | | 13- | | |
| • | | 1- | 12- | 36 3 |

And note that the yard, as also the ell, is usually divided into 4 quarters, and each quarter into 4 Nails,

Note also that a Geometrical Pace is 4 feet; and there are 1056 such Paces in an English mile.

2. The parts of the Superficial Measures of Land are such as are mentioned in the following Table, viz.

The Table of Land Measure.

or Perches make an Acre.

December

By the foregoing Table of Ling Measure, you are informed what a Pole, or (which is all one) Perch is; and by this that 40 square Perches are 1 Rood. Now by a square Perch is a superficies very aptly resembled by a square Trencher, every side thereof being a Perch, or 5 Yards and a half in length, 40 of them is a Rood, and 4 Roods an Acre. So that a Superficies that is 40 Perches long and 4 broad is an Acre of Land, the Acre containing in all 160 square Perches.

10. The least denominative part of Time is a Minute, the greatest Integer being a Tear; from whence

is produced this following Table.

The Table of Time.

| I | Minute | • | (1 | Minute |
|----|----------------|---------|-------------|-------------|
| 60 | Minutes | · / / · | λ_1 | Hour |
| 24 | Hours | (3 | 2) [| Dav natural |
| 7 | Days . | 7 | 151 | Week |
| 4 | Weeks | | . / a | Month . |
| 13 | Months, I day, | 6 hou. | Li | Year. |

But the Year is usually divided into 12 unequal Kalendar Months, whose Names and the number of Days that they contain, follow, viz.

| | days | · · · · - |
|------------|------|---|
| Fannary | 31 | • • |
| February . | 28 | So that the Year containeth 365 |
| March | 31 | Days, and 6 Hours, but the 6 Hours |
| April | 30 | |
| May | 31 | Year, and then there is a day added |
| June | . 30 | sto the latter end of February, and |
| July | 31 | then it containeth 29 days, and that |
| Auzust | 31 | year is called Leap-year, and con- |
| September | 30 | taineth 366 days. |
| OEtober | 31 | |
| MT L | • | 1 · · · · · · · · · · · · · · · · · · · |

And here note, that as the Hours is divided into 60 Minutes, so each Minute is subdivided into 60 Seconds, and each Second into 60 Thirds, and each Third into 60 Fourths, 476.

The Tropical Year by the exactest observations of the most accurate Astronomers is found to be 365 Days,

5 Hours, 49 Minuts, 4 Seconds, and 21 Thirds.

CHAP. III.

Of the Species or Kinds of Arithmetick.

1. A Rithmetick is either Natural, Artificial, Avalytical, Algebraical, Lineal or Influmental.

2. Natural Arithmetick is that which is performed by the Numbers themselves; and this is either Positive or Negative. Positive which is wrought by certain infallible Numbers propounded, and this either Single or Comparative; Single which considereth the nature of Numbers simply by themselves; and Comparative, which is wrought by Numbers as they have relation one to another. And the Negative part relates to the Rule of False.

3. Artificial (by fome call'd Logarithmetical) Arithmetick is that which is performed by artificial or borrowed Numbers invented for that purpose, and are cal-

led Logarithms.

4. Analytical Arithmetick, is that which shews from a thing unknown to find truly that which is sought; always keeping the Species without Change.

5- Algebraical Arithmetick, is an obscure and hidden. Art of Accompting by Numbers in resolving of hard Questions.

6. Lineal Arithmetick, is that which is perform'd by lines fitted to proportions, as Geometrical Projections.

7. Instrumental Arithmetick, is that which is performed by Instruments fitted with Circular and Right Lines of Proportion, by the motion of an Index, or otherwise.

8. The

8. The parts of Single Arithmetick are Numeration

and the Extraction of Roots.

9. Numeration is that by which certain known Numbers propounded, we discover another Number unknown.

10. Numeration hath four Species; viz. Addition,

Subtraction, Multiplication and Division.

CHAP. IV.

Of Addition of Whole Number's.

Total. Or it is that by which divers numbers are added together, to the end that the Sum or Total value of them all may be discovered.

The first number in every Addition is called the addible number, the other, the number or numbers added, and the number invented by the Addition is called the Aggregate or Sum containing the value of the Addition.

The Collation of the numbers, is the right placing of the numbers given respectively to each denomination, and the Operation is the artificial adding of the numbers given together in order to the finding out of the Azzregate or Sun.

2. In Addition, place the numbers given respectively the one above the other, in such sort, that the like degree, place or denomination, may stand in the same Series, viz. Units under Units, Tens under Tens, stunderes under Hundreds, Gr. Pounds under Peunds, Shillings under Shillings, Pence under Pence, Gr. Yards under Yards, Feet under Feet, Gr.

3. Having thus placed the numbers given (as before) and drawn a line under them, add them together, beginning with the leffer denomination. viz. at the right hand, and so on, subscribing the sum under the line

respectively; as for Example.

Let there be given 3352 and 213 and 133 to be added together, I set the Units in each particular number under each other, and so likewise the Tens under the Tens, Oc. and draw a line under them, as in the Margent, then I begin at the 3352 place of Units, and add them together up. 212 wards, saying, 3 and 3 are 6 and 2 make 8, which I set under the line, and under the 132 fame Figures added together; then I pro-2668 ceed to the next place, being the place of Tens, and add them up in the same manner as I did the place of Units, faying, a and 1 are 4 and 5 are 5, which I likewise set under the line respectively; then I go to the place of Hundreds, and add them up as I did the other, faying, 1 and 2 are 2 and 3 are 6, which I also set under the line; and lastly, I go to the place of Thoulands, and because there are no other Figures to add to the 3, I fet it under the line in its respective place, and so the work is finished; and I find the sum of the 2 given numbers to be 2698. 4. But if the 5um of the Figures of any Series exceeds ten, or any number of tens, subscribe under the same the Excess above the tens, and for every ten carry one to be added to the next Series towards the left hand, and to go on till you have finished your addition; always remembring, that how great soever the fum of the Figures of the last Series is, it must all be let down under the line respectively. So 3678 being given to be added to 2357, I fet them down as is before directed, and as you see in the Margent, with a line drawn under them, then I begin and add them together, faying, 7 and 8 are 15, which is 5 above 10, wherefore I fet 5 under the line, and carry it for the 10 to be added to the next feries, faying, I that I carried and 6095 5 is 6 and 7 are 13, wherefore I fet down 3 and carry I (for the ten) to the next series, then I fay I that I carried and 3 are 4 and 6 are 10, now because it comes to just 10 and no more, I set o under the line and carry 1 for the 10 to the next, and say, 1

 ${}_{\text{Digitized by}}Google$

that I carried and 2 are 3, and 3 are 6, which I fet 604n in its respective place, thus the addition is ended, and the total Sum of these Numbers is found to be 6035, Everal Examples of this kind follow.

5. If the Numbers given to be added, are contained under divers Denominations; as of Pounds, Shil-lings, Pence and Farthings; or of Tuns, Hundreds, Quarters, Pounds, &cc. Then in this case having disposed of the Numbers, each denomination under other of like kind; beginning at the least denomina-tion, minding how many of one denomination do make an Integer of the next) and having added them up, for every Integer of the next greater denomination that you find therein contained, bear an Unit in mind to be added to the faid next greater denomination, expressing the excess respectively under the line, proceed in this manner until your Addition be finished; the following Examples will make the Rule plain to the Learner. Thus these several Sums being given to be added, viz. 136 l. 13 s. 4 d. 2 grs. and 79 l. 09 s. 10 d. 2 grrs. and 33 l. 18 s. c9 d. 1 gr. also 15 l. 09 s. 05 d. 0 gr. The Numbers being disposed according to order will stand as in the Margent. Then I being at the denomination of Farthings,

and add them up, faying, 1 and 2 are 4 and 2 make 6, now I consider that 6 Farthings is r 136-13-04-2 Penny and a Farthings, wherefore I let down the 2 Farthings 33-18-09-1 in its place under the line, and 15-00-05-0 keep I in mind to be added to the next denomination of Pence; . 265-09-05-2 then I go on, faying 1 that I car-ried and 5 are 6 and 9 are 15 and 10 are 25 and 4 are 20. now I consider that 20 pence are 2 shillings and 5 pence, whereof I fet the 5 pence in order under the line and keep 2 in mind for the 2 shillings, to be added to the shillings; then I go on, faying, that 2 I carried and 9 are 11, and 18 are 29, and 7 are 36, and 13 are 49; then I confider that 49 shillings are 2 pounds and 9 thillings, wherefore I fet the 9 thillings under the line, and carry 2 for the 2 pounds, to the next and last denomination of pounds, and proceed, faying 2 that I carried and 5 make 7, and 3 are 10, and 9 are 19, and 6 are 25; then I fet down 5, and carry 2 for the tens, and proceed, faying, 2 that I carry and 1 is 3, and 3 are 6, and 7 are 13, and 3 make 16; I fet down 6 and carry 1 for the 10, and go on, faying I that I carried and I are 2, which I fet

in its place under the line, and the work is finished; and thus I find the Sum of the foresaid Numbers to be 2651. 95. 5th 2 grs. This to the ingenious Practitioner is sufficient, but I shall (for the further illuminating of weaker apprehensions) explain the operation of another Example in Troy-weight; and here the Learner must take notice of the Table of Troy-weight mentioned or set down in the third Section of the second Chapter. The Numbers given in this Example

are 38 l. 70%. 13 p.w. 18 gr. and 50 l. 10 sx. 10 p.w. 12 gr. and 42 l. 08 sx. 05 pw. 16 gr. and in order to the Addition thereof, I place them as you fee, and proceed to operation; faying 16 and 12 are 38, and 18 are 46; now because 24 grains make 19eans

r penny-weight, 46 grains are 1 penny-weight and 22 grains; wherefore I fet down 22, and carry 1 for the penny-weight, and going on I fay, I that I carry and s make 6, and 10 are 16, and 12 are 29. which is one ounce and

l. oz. p.w. gr. 28-7-13-18 50-10-10-12 42-08-05-16

o penny-weight, I set down 9 in its place under the line, and carry 1 to the ounces, faying 1 that I carry and 8 are 9, and 10 are 19, and 7 are 26, and because 26 cuaces make 2 pound 2 ounces, I fet down 2 for the ounces, and carry 2 to the pounds: going on, 2 that I carry and 2 are 4, and 8 make 12, that is 2 and go 1 5 then 1 I carry and 4 are 5, and 5 are 10, and 3 are 13, which I fet down as in the Margent, and the work is finished, and I find the sum of the said numbers to amount to 122 l. 20z. 9 p.w. 22 gr. This is sufficient for the understanding of the following Examples, or any other that shall come to thy view. The way, of proving these, or any Sums in this Rule, is shewed immediately after the enfuing Examples.

-12-c7-1

768-17-04-2 564-11-11-0

Addition of English Money. d. grs 48-15-11-1 76-10-07-3 24-19-09-2

Addition of Troy-weight.

l. oz. p.w. gr. 15-07-13-12 18—c6—04—20 . 11-10-16-18 09-04-10-22 19-11-11-04

22-0C-0C-00,

97-04-17-04

oz. p.w. gr. 145-09-12-18 725-08-14-10 380-07-06-13

82-10-16-20 130-00-10-12 74-07-15-0

Addition of Apothecaries Weights.

| | ` . |
|-------------------------------|-----------------------|
| 1. oz. dr. sc. gr. | . In ozan dr. sc. gr. |
| 48-07-1-C-14 | 60-03-4-0-10 |
| 74-05-5-2-10 | 48-10-57-0-14 |
| 64-10-7-1-16 | 34-08-2-1-15 |
| 17-08-1-0-11 | 18-11-2 -2-JI. |
| 34-09-5-1-09 | 160-07-1-2-15 |
| | -35-02-5-107 |
| 240-05-6-1-00 | |
| هسست استهاست و الطلقة في سيست | 358-07-7-9-12 |
| | |
| | |

Addition of Averdupois-weight.

| | 1. oun. dr. |
|--|-------------|
| Tun _C. qrs . | |
| 48 3 21 | 22-11-13 |
| 60———————————————————————————————————— | 15-04-10 |
| 12-16-0-11 | 20 |
| 218—16—0—05 | 1.603 |
| Statement of the last principle of the last of the las | |

Addition of Liquid Measure.

| Tun | pipe bhd | gall. | Tiens ; | bhd | gall. | pts |
|-----|-----------------|-----------------|---------|------|------------------|-----|
| 45- | | -48 | 30- | -3- | -4 0- | 4 |
| _ | - 01 | • | | | —28.— —6ე_ | |
| 7 | - Io | • /. | | - | 22- | |
| | — I —— I — | | | | QQ | , |
| 133 | | - 60 | 166- | عنوا | 26 | 2 |
| | | | 1 | | | |

Addition of Dry Measure.

| Chald. qrs. bnfh. pec. 48 3 7 3 13 1 4 0 54 0 6 12 16 3 6 1 40 1 0 1 | gro. bush. pec. gall. 17 3 1 1 50 1 3 0 F4 5 3 1 40 2 0 1 30 3 0 |
|---|---|
| | |

Addition of Long Measure.

| yards | qrs. | na. | | qrs. | |
|-------|----------|---------------|----|------------|----|
| | 3- |) (| | | |
| | | | 48 | 2 | Į. |
| 38 | ······ | I¹ | , | Fine | |
| | | | | بند استهمي | |
| | سنسننت س | <u>ڪٽ ٿ ڪ</u> | | | |
| | | | | | |

Addition of Land Measure.

| Acre wood percit | Acre rood perc. |
|--------------------|----------------------|
| 12 | 8636 |
| 1424 | 73 - 24 |
| 30 2 19 48 3 30 | 60 0 0 0 0 0 7 0 0 8 |
| 28 3 38 | 1414 |
| 185-3-35 | 285-3-27 |

The

The Proof of Addition.

6. Addition is proved after this manner, when you have found out the sum of the Numbers given, then separate the uppermost line from the rest, with a stroke or dash of the pen, and then add them all up again as you did before, leaving out the uppermost line, and having so done add this new invented sum to the uppermost line you separated, and if the sum of those two lines be equal to the sum sirst sound out, then the work was performed true, otherwise not. As for Example, Let us prove the first Example of Addition of Money, whole sam we sound to be 2651. 9s. 5d. 2975.

and which we prove thus, having feparated the uppermost number from the rest, by a line as you see in the Margent, then I add the same together again, leaving out the said uppermost line, and the sum thereof I set under the first sum or true sum, which doth amount to 128 l. 16 s. 01 d. o qrs. then again I add this new sum to the uppermost line that before was separated from the rest, and the sum of these two is 26 s 1. 09 s. 65 d. 2 qrs. the

265-09-05-2 128-16-01-0 265-09-05-2

s. d. grs

136-13-04-2

79-07-10-3 33-18-09-1 15-09-05-0

is 2641. 69 s. 65 d. 2 grs. the same with the first sum; and therefore I conclude that the Operation was rightly performed.

7. The main end of Addition in Questions Resolvable thereby, is to know the sum of several Debts, Parcels, Integers, &c. Some Questions may be these that follow.

Quest. 1. There was an Old Man whose Age was requited, to which he replied. Phave seven Sons, each having two years between the birth of each other, and in the 34 year of my Age my eldest Son was born, which is now the Age of my youngest; I demand what was the Old Man's Age

Now to resolve this Question, first set down 44 the Fathers Age at the birth of his first Child, · I2 which was 44, then the difference between the 44 eldest and the youngest, which is 12 years, and then the Age of the youngest which is 44, and 100 then add them all together, and their fum is 100 the compleat Age of the Father.

Quest. 2. A Man lent his Friend, at several times, these several Sums, (viz.) at one time 63 l. at another time soil, at another time 48 l. at another time-156 l. now I desire to know how much was lent him

in all.

Set the Sums lent one under another, as you see in the Margent, and then add them together, and you will find their Sum to amount to 2171, which is the Total of all the several Sums lent, and so much is due to the Creditor. 317

Quest. 3. From London to Ware is 20 miles, thence to Huntington 29 miles, thence to Stamford 21 miles, thence to Tuxford 36 miles, thence to Wentbridge 25 miles, from thence to Tork 20 miles. Now I defire toknow how many miles it is from London to Tork accord-

ing to this reckoning.

Now to answer to this Question, set down -the several distances given, as you see in the Margent, and add them together, and you will find their Sum to amount to 151, which is the true distance in miles between London and Tork.

Quest. 4. There are two numbers, the least whereof is 40, and their difference is 14, I defire to know what is the greatest Number, and also what is the Sum of them both? First, set down the least, viz. 40, and 14 the difference, and add them topether, and their fum is 54 for the greatest number, then I

40 14

171

greatest. least

fet 40 (the least) under 54 (the greatest) and add them together, and their sum is 94 equal to the greatest and least numbers.

CHAP. V.

Of Subtraction of Whole Numbers.

of a greater of like kind, whereby to find out a third Number, being or declaring the inequality, excess, or difference between the numbers given; or Subtraction is that by which one number is taken out of another number given, to the end that the refidue or Remainder may be known, which Remainder is also called the Rest, Remainder, or Difference of the numbers given.

2. The number out of which Subtraction is to be made, must be greater, or at least equal with the other number given, the higher or superiour number is called the major number, and the lower or inferiour is called the minor number; and the Operation of Subtraction being finished, the Rest or Remainder is called the Difference

of the Numbers given.

3. In Subtraction place the Numbers given respectively, the one under the other, in such sort as like degrees, places or denominations, may stand in the same Series, viz. Units under Units, Tens under Tens Gr. Pounds under Pounds, Gr. Feet under Feet, and Parts under Parts, Gr. This being done, draw a line undergeath, as in Addition.

4. Having placed the Numbers given as is before directed, and drawn the line under them, subtract the lower Number (which in this case must always be lesser than the uppermost) out of the higher Number, and subscribe the difference or remainder respectively below the line; and when the Work is finished, the

number below the line will give you the remainder: As for Example, let 364521 be given to be subtracted from 795836, I set the lesser under the greater as in the Margent, and draw a line under them, then beginning at the right hand, I say, I out of 6 and there remains 5, which I fet 794826 in order under the line; then I proceed 364521 to the next, faying, 2 from 2 refts 1. which I note also under the line, and 431216 thus I go on until I have finished the work,

and then I find the Remainder or Difference to be 431214. 5. But if it so happen (as commonly it doth) that the lowermost number or figure is greater than the uppermost; then in this case add ten to the uppermost number, and subtract the said lowermost number from their Sum, and the remainder place under the Line, and when you go to the next Figure below. ray an Unit by adding it thereto for the ten you bor-. rowed before, and subtract that from the higher number or figure .: And thus go on until your Subtraction te finished. As for Example; Let 427502 be given. from whence it is required to subtract 153827, I dispose of the numbers as is before directed, and as you fee in the Margent; then I begin, saying, 7 from 3 I cannot, but (adding 10 thereto I say) 7 from 12 and there remains 6, which I set under the Line in order; then I proceed to the 437503 next Figure, faying, I that I borrowed 153827 and 2 is 3 from 0 I cannot, but 3 from 10, and there remains 7, which I like-283676 wie fet down as before; then I that I porrowed and 8 is 9 from 5 I cannot, but a from 15 and there remains 6; then 1 I borrowed and a is 4 from 7 and there remains as then 5 from 3 I cannot, but 5 from 13 and there remains 8; then 1 I borrowed and 1 are 2 from 4 and there refts 2; and thus the Work is finished; And after these numbers are subtracted one from another, the Inequality, Remainder, Excess or Difference, is found to be

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From 3475016 Take 728642

From 2614746 Take 5864

Refts 2725274 Refts 3609882

6. If the Sum or Numbers to be subtracted are of several Denominations, place the lesser sum below the greater, and in the same rank and order as is shewed in Addition of the same Numbers; then begin at the right hand and take the lower Number out of the uppermost if it be lesser; but if it be bigger than the uppermost, then borrow an Unit from the next greater Denomination, and turn it into the Parts of the he's Denomination, and add those parts to the uppermost Number, and from their fum subtrast the lowermost. noting the remainder below the Line; then proceed and pay 1 to the next Denomination for that which you borrowed before, and proceed in this order until the work be finished. An Example of this Rule may be this that followeth, let 375 l. 13 s. 07 d. 1 gr. be given, from whence let it be required to subtract 57 1. 16 s. 03 d. 2 qrs. In order whereunto I place the Numbers as you see in the Mar-

gent, and thus I begin at the least Denomination, faying, two from 375-13-67-1 one I cannot, therefore I borrow 57-16-63-2 one penny from the next Deno-

mination, and turn it into farthings, which is 4, and adding 4 to 1 which is 5, I say, but 2

from 5 and there remains 3, which I put under the line; then going on, I fay, I that I borrowed and 3 is 4 from 7 and there rests 2; then going on, I say, 16 from 13 I cannot, (but borrowing one pound and turning it into 20 shillings, I add it to 13, and that is 33) wherefore I say, fixteen from 33, and there remains 17, which I fet under the Line and go on, faring, I that I borrowed and 7 is 8 from 5 I cannot, but 8 from 15, and there remains 7; the one that I

borowed and 5 is 6 from 7 there refis 1, and 0 from 3 refts 3, and the work is done: And I find the remainder or difference to be 317 l. 17 s. 03 d. 3 grs.

Another Example of Troy-weight may be this, I would fubtraft 17 1. 10 07. 11 per. 20 gr. from 24 1. C & oz. CO p.w. 68 gr. I place the Numbers according to the 1. oz. p.w. gr. Rule, and begin, saying, 20 from 24-05-00-08 8 I cannot, but borrow ! Penny-17-10-11weight, which is 24 Grains, and add them to 8, and they are 22. 06-06-08-12 wherefore I say 20 from 32 rest

12; then I that I borrowed and 11 is 12 from 00 I cannot, but 12 from 20 (borrowing an Ounce which is 20 Penny-weight) and there remains 8, then I that I borrowed and 10 is II from c I cannot, but 11 from 17 and there rests 6; then I that

I borrowed and 7 is 8 from 4 I cannot, but 8 from 14 and there refts 6; then I that I borrowed and I is 2

from 2 and there refts nothing; so that I find the remainder or difference to be 61. 6 oz. 8 p.w. 12 gr.

7. It many times happeneth that you have many Sums or Numbers to be subtracted from one number; as suppose a Man should lend his Friend a certain sum of Money, and his Friend hath paid him part of his Debt at several times, then before you can conveniently know what is still owing, you are to add the several Numbers or Sums of Payment together, and subtract their Sum from the whole Debt, and the remainder is the Sum due to the Creditor: As suppose A lendeth to E 5641. 135. 10 d. and B hath repaid him 79 l. 16 s. Lent ~54-12-10 08 d- at one time, and 163 L. 18 s. 11 d. at another time, and 241 L 155 féveral c8d at another time; and you would know how the

Accompt standeth between

them, or what is more due A. In order whereunto

Paid in all 485-11-03

Remains 79-02-07

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I first set down the Sum which A lent, and draw a line underneath it; then under that line set the several Sum; of Payment'as you see in the Margent; and having brought the several Sums of Payment into one total by the fifth Rule of the south Chapter foregoing, I find their Sum amounteth to 48; 1. 11 s. 3d. which I subtract from the Sum first lent by A, by the fixth Rule of this Chapter, and I find the remainder to be 79 l. 2 s. 7 d- and so much is still due to A.

When the Learner hath good knowledge of whathhath been already delivered in this and the foregoing Chapter, he will with ease understand the manner of-

working the following Examples.

| | | | - | | | |
|----------|-----------|---------------|-------------|--------|------|-------------|
| | Subt | ra&ion of | Whole M | foney. | | |
| · - | | 3. d. | | S. | d. | qrs |
| Borrowed | 374 | 5c 0 3 | 700- | -10- | -11- | |
| Paid | 69 | 15-11 | 9- | -03 | -11- | —- ş |
| Remains | 304 | 14-04 | 691- | -06 | -11- | 3 |
| Ç 14 - | | | | . , | 14 | , |
| | <i>l.</i> | s. d. | <i>l</i> : | S | ď. | qr.s |
| Birrowed | | 0900 | • | -0'g | | 0 |
| Paid | 19- | oc06 | 11 | -13 | -00- | I |
| Remains | 980- | 19+-06 | 699- | -09- | -11 | |
| | - | | | | | |
| | | 1. ~ | | | q#6 | -13-5 |
| Botro | wed | 3300 | 00- | | 2 | • |
| - 1 | 4 | C 170 | - 1a- | | | |
| Paid | at seve- | 361 | <u>13</u> - | | | |
| ral P | ayments. | | ó3- | | | |
| | • ' ' | 73 | | 11- | | <u>.</u> |
| Paid | in all " | TIOS | 12- | | | ¥ , |
| · | 217 FF86 | 1195 | | | | mo 🗽 |
| Rema | ins due | 2104 | 07: | | Z | ٠. |
| • | | | _ | Google | | Sic |

Subtraction of Troy-weight.

| Brught Sold | 78- | | p.w. 13 16 | 00 15 |
|--------------|------------------|------|------------------|----------------|
| Remains | | -07- | <u> </u> | -09 |
| Bought | 479- | 107 | 13 | -00 |
| | P. 50- | 00 | | 00 |
| several |) : 16 — | -07- | co | —с§ |
| , | 23 | | 00 | 00 |
| Sold in all. | - 245 | 10 | 07 | 07 |
| Rem.unfold | 225- | -00- | °5- | -17 |

Subtraction of Apothecaries Weights.

Subtraction of Averdupois-weight.

| 5 4 | C. grs. l. | Tun C. qrs L. ox. dr. |
|----------|------------|-----------------------|
| Bought . | 2 < 00-15 | 15-07-01-10-10-05 |
| Sold | -16-02-20 | 03-17-01-10-09-13 |
| | | 11-09-03-22-00-08 |

Subtraction of Liquid Measure.

| Bought Sold | Tuns hhd gall. 40—1—30 16—1—40 | Tun bbd gall. pin. 60-3-42-4 15-3-46-6 |
|----------------|--------------------------------|--|
| Remains: | 23 — 3 — 53 | 44-3-58-6 |

Subtraction of Dry Measure.

| • | Chald. qrs. bush.pec. | Chald. grs. | bush. | pec. |
|---------|-----------------------|-------------|-------|------------|
| Bought | 100-0-00-0 | 732- | —3 | — 2 |
| Sold | 54-1-04-3 | 462 | -3- | -3 |
| Remains | 45-2-03-1 | 263- | | |

Subtraction of Long Measure.

| | yards | qrs | nails | yards | qrs. | nails |
|---------|-------|-----|-----------------|-------|------|-------|
| Bought | 160- | 1 | 0 : | 344 | 0 | |
| Sold | | | | | | |
| Damaina | | | | | | |
| Remains | 95 | | | 100- | | |

Subtraction of Land Measure.

| Bought Sold | 140 | Acres roods perc. 600 00 00 54 16 |
|----------------|-----|-----------------------------------|
| Remains | | 545324 |

The Proof of Subtraction.

8. When your Subtraction is ended, if you desire

to prove your Work, whether it be true or no, then add the remainders to the minor Number, and if the Aggregate of these two be equal to the major number, then is your Operation true, otherwise false; thus let us prove the first Example of the fifth Ru'e of this Chapter, where after Subtracti-437503 on is ended, the Numbers stand as in the 152827 Margent; the remainder or difference being 282676. Now to prove the Work, I 282676 add the faid. Remainder 283676 to the minor number 153827, by the fourth Rule of 437503 the foregoing Chapter, and I find the Sum 152827 or Aggregate to be 437503 equal to the major Number, or Number from whence the 283676 . leffer is subtracted. Behold the Work in the Margent. 437503

The Proof of another Example may be of the first Example of the sixth Rule of this Chapter, where it is required to subtract 57 l. 16 s. 03 d. 2 qrs. from 375 l. 13 s. 07 d. 1 qr. and by the Rule I find the Remainder to be 217 l. 17 s. 02 d.

Remainder to be 317 l. 17 s. 03 d.
3 grs. now to prove it, I add the fall Remainder 317 l. 17 s. 03 d.
3 grs. to the minor number 57 l.
16 s. 03 d. 2 grs. and their fum is 375 l. 13 t. 07 d. I gr. Equal to the major number, which proves the work to be true, but if it had happened to have been either

375-13-07-1 57-16-3-2

375-13-07-1

more or less than the said major number, then the Operation had been false.

o. The general effect of Subtraction is to find the differences or excess between two numbers, and the rest when a payment is made in part of a greater Sum, the date of Books printed, the age of any thing by knowing the present year, and the year wherein they were made, created or built, and such like.

The Questions appropriated to this Rule are such as

follow.

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87

Quest. 1. What difference is there between one thing of 125 foot long and another of 66 foot long?

To resolve this Question, I first set down the major or greater number 125, and under 124 it the minor or lesser number 66, as is di-66 refted in the third Rule of this Chapter and according to the fourth Rule of the same. 59 I subtract the minor from the major, and the Remainder, Excels or Difference, I find to be so. See the Work in the Margent.

Quest. 2. A Gentléman oweth a Merchant 464 1. whereof he hath paid 278 L what more doth he owe?

To give an Answer to this Question, I first - fet down the major number 3651. and under 365 it I place 278 the minor, and subtract the one 278 from the other, and thereby I discover the Excess. Difference or Remainder to be 87. and so much is still due to the Creditor : 25 per Margent.

Quest. 2. An Obligation was written, a Book printed, a Child born, a Church built, or any other thing, made in the year of our Lord 170 I 1572, and now we account the year of our 1572 Lord For, the Question is to know the Age of the said things, that is, how many Years 129 are passed since the said things were made? I say, if you subtract the lesser number 1572, from the greater 1701, the remainder will be 129, and fo many Years are past since the making of the said things; as by the Workin the Margent.

Quest. 4. There are three Towns lie in a streight line, viz. London, Huntington, and Tork, now the distance between the farthest of these Towns, viz. London and Tork is 151 miles, and from London to Huntington is 49 miles, I demand how far it is from Huntington to Tork.

To resolve this Question, subtract 40 the distance between London and Huntington, from 151 Is the distance between London and Tork . and the Remainder is 102, for the true distance between Huntington and York. See the Work in the Margent.

49 102

CHAP. VI.

Of Multiplication of Whole Numbers.

A Ultiplication is performed by two Numbers of like kind for the production of a third, which shall have such reason to the one, as the other hath to a Unit, and in effect is a most brief and artificial com-, pound Addition of many equal Numbers of like kind into one Sum. Or Multiplication is that by which we multiply two or more Numbers, the one into the other, to the end that their Product may come forth, or be discovered.

Or, Multiplication is the increasing of any one number by another: fo often as therefare Units in that Number, by which the other is increased, or by having two Numbers given to find a third, which shall contain one of the Numbers as many times as there are Units

in the other.

2. Multiplication hath three parts: First, the Multiplicand, or number to be multiplied. Secondly, the Multiplier, or number given, by which the Multiplicand is to be multiplied. And Thirdly, the Product, or number produced by the other two, the one being multiplied by the other, as if 8 were given to be multiplied by 4. I say 4 times 8 is 32, here 8 is the 3 4 Multiplicand, and 4 is the Multiplier, and 32 is the Product. 32

2. Multiplication is either fingle by one Figure; compound, that confifts of many.

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Single Multiplication is faid to confift of one figure, because the Multiplicand and Multiplier confist each of them of a Digit, and no more, so that the greatest Product that can arise by single Multiplication is 8 t, being the square of 9; and Compound Multiplication is said to confist of many Figures, because the multiplicand or multiplier consists of more places than one; as if I were to multiply 436 by 6, it is called Compound, because the multiplicand 436 is of more places than one, (viz.) 3 places.

4. The Learner ought to have all the varieties of Single Multiplication by heart before he can well proceed any further in this Art, it being of most Excellent Use, and none of the following Rules in Arithmetick but what have their principal dependance thereupon, which may be learnt by the following Table.

Multiplication Table.

| 1 | 2 | 3 | 4 | . 5 | 6 | 7 | 8 | 9 |
|----|-----|------|-----|------|-----|-----|----|------|
| 2 | . 4 | 6 | 8. | 10 | 12 | 14. | 16 | 18 |
| 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | . 27 |
| 4 | 8 | 12 | 16 | 20 | 2/1 | 28 | 32 | 35 |
| 15 | 10 | . 15 | 20 | 25. | 30 | 35 | 40 | 45 |
| 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 |
| 7 | 14 | -21 | 28 | 35 | 42 | 49 | 55 | 63 |
| 8 | 16 | 24 | 3,2 | 40 | 48 | 56 | 34 | 72 |
| 9 | 18 | 27 | 36; | . 45 | 54 | 63 | 72 | 1,8 |

The use of the precedent Table is this. In the uppermost Line or Column you have expressed all the digits from 1, to 9; and likewise beginning at 1 and going downwards in the side Column you have the same; so that if you would know the Product of any

any two fingle Numbers multiplied by one another, look for one of them (which you please) in the uppermost Column, and for the other in the side Column, and running your eye from each sigure along the respective Column, in the common Angle (or place) where these two Columns meet, there is the product required. As for Example, I would know how much is 8 times 7; first, I look for 8 in the uppermost Column, and 7 in the side Column; then do I cast my eye from 8 along the Column downwards from the same, and likewise from 7 in the side Column, I cast my eye from thence towards the right-hand, and find it to meet with the first Golumn at 56, so that I conclude 56 to be the Product required, it would have been the same if you had looked for 7 in the top, and 8 on the side, the like is to be understood of any other such Numbers. The Learner being perfect herein, it will be necessary to proceed.

4. In compound Multiplication, if the Multiplicand confifts of many places, and the Multiplier of but one Figure ; first set down the Multiplicand, and under it place the Multiplier in the place of Units, and draw a Line underneath them; then begins. and multiply the Multiplier into every particular Figure of the Multiplicand, beginning at the place of Units, and so proceed towards the left-hand, setting each particular Product under the Line, in order as you proceed, but if any of the Product exceed 10 or any number of Tens, fet down the Excess, and for every 10 carry a Unit to be added to the next Product, always remembring to fet down the total Product of the laft Figure; which Work being finished, the Sum or Number placed under the Line shall be the true and Total Product required. As for Example, I

would multiply 478 by 6, first I set down 478, and underneath it 6 in the place of Units, and draw a Line underneath them, as in the Margent, then I begin, laying, 6 times 8 is 48, which is 8 above 4 Tens, therefore I set down 8 (the Exces) and

478 6

2868

bear

bear 4 in mind for the 4 tens, then I proceed, saying, 6 times 7 is 42, and 4 that I carried is 46, I then set down 6 and carry 4, and go on, saying 6 times 4 is 24, and 4 that I carried is 28, and because it is the last figure, I set it all down, and so the work is smilled, and the product is found to be 2868, as was required.

the product is found to be 2868, as was required,
6. When in compound Multiplication the multiplier confifteth of divers places, then begin with the figure in the place of Units in the multiplier, and multiply it into all the figures in the multiplicand, placing the product below the line as was directed in the last Example; then begin with the figure of the fecond place of the multiplier, (viz.) the place of Tens, and multiply it likewise into the whole multiplicand (as you did the first figure) placing its product under the product of the first figure, do in the same manner by the third, fourth and fisth, Gre. until you have multiplied all the figures of the multiplier particularly into the whole multiplicand, still placing the product of each particular figure under the product of its precedent figure; herein observing the following Caution.

In the placing of the product of each A Caution. particular figure of the multiplier, you are not to follow the 2d Rule of the 4th Chapter, viz. not to place Units under Units, and Tens under Tens, &c. but to put the Figure or Cypher in the place of Units of the fecond line under the fecond figure or place of the Tens in the line above it, and the figure or Cypher in the place of Units of the third line under the place of Tens in the fecond line, &c. Observing this order till you have sinished the Work, viz. Still placing the first Figure of every line or product under the second Figure or place of Tens in that which was above it, and having so done, draw a line under all these particular products, and add them together; so shall the sum of all these products be the total product required.

As if it were required to multiply 764 by 27, I fet them down the one under the other, with a line drawn

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| | | | :) ~ |
|------------------|--------------|--------------------|--------------------|
| underneath th | em; then | I begin, | faying, 7 |
| times 4 is 28, t | hen I fet de | ówn 8, and | carry 2, |
| then lay 7 time | s 6 is 42, : | a nd 2 that | l carried |
| is 44, that is 4 | and go 4; | then 7 1 | imes 7 is |
| 49, and 4 that | I carry is | 3,which I | set down |
| because I have | not anoth | er Figure | to multi- |
| ply; thus have | I done wi | th the 7, | th en I be- |
| gin with the 2 | faying, 2 | times 4 is | 8, which |
| I let down u | | | |

20628 place of Tens, in the Line above it, as you may fee in the Margent: Then I proceed, saying, 2 times 6 is 12, that is two and carry one, then 2 times 7 is 14, and I that I carry is 15, which I fet down because tis the product of the last Figure; so that the product of 764 by 27 is 5348, and by 2 is 1528, which being placed the one under the other, as before is directed, and as you see in the Margent, and a Line drawn under them, and they added together respectively, make 20628 the true product required, being equal to 27 times 764.

Another Example may be this; Let it be required to multiply 5486 by 465, I dispose of the Multiplicand and Multiplier, according to 5486

the Rule, and begin multiplying the first figure of the Multiplier, which is 5 into the whole Multiplicand, and the Product is 27430; then I proceed and multiply the second figure (6) of the Multiplier into the Multiplicand, and find the Product to amount to 32916, which is subscribed under the other Product respectively, then do I multiply the third and last figure (4) of the Multiplier into the Multiplicand, and the Product is

21944 2550990

465

27430

32916

5348 .1528

21944, which is likewise placed under the second Line respectively; then I draw a Line under the said Product (being placed the one under the other according to this Rule) and add them together, and the fum is 2550900, the true Product fought, being equal to 5486 times 465, or 465 times 5486. केंग्रामां विक्र केंग्र

More Examples in this Rule are thefe following.

| 430865 4739 | 64co758 3 37498 |
|----------------|--------------------|
| 3877785 | 38404548 |
| 1292595 | 57605822 |
| 3016055 | 25603032 |
| 1723460 | 44805306 |
| | 19202274 |
| 2041869235 | 240002821968 |

Compendiums in Multiplication.

7. Although the former Rules are sufficient for all

Cases in Multiplication, yet because in the Work of Mulindication many times great labour may be faved, I shall acquaint the Learner with fome Compendiums in order thereto, viz. If the Multiplicand or Multiplier, or both of them end with Cyphers, then

in your multiplying you may neglect the Cyphers, and multiply only the fignificant Eigures, and to the Product of those fignificant Figures, add so many Cyphers as the Numbers given to be multiplied did end with;

that is, annex them on the Right-hand of the faid Product, so shall that give you the true Product required. were to multiply 32000 by 4300, I set

them down in order to be multiplied as you fee in the Margent, but neglecting the Cyphers in both numbers, I only

multiply 32 by 43, and the Product I find to be 1376, to which I annex the 5

Cyphers that are in the Multiplicand and Multiplier, and then it makes 127600000 for the true Product of 22000 by 4300.

Si e numeria propulitis unus vel uterque adjunitus habeat ad dextram circulos ; omissis. circulis fiat ipforum numerorum multiplicatio, & fallo demum tot insuper integrorum loci accenfenntur quot sunt omissi circuit in utroque falle. re, Clavis Mat.c. 4. 3.

22:00 4300

96 . 1 28

نوoogle

1 37600000

8. If in the multiplier Cyphers are placed between fignificant figures, then multi-

ply only by the figuificant Figures, neglecting the Cyphers, but here special notice is tobe taken of the true placing of

Si intermedio multiplicantie loco circulus fuerit, ille nego ligetur: Alfted. cap. 9. de

Arithman

the first figure after the neglect of such Gypher or Cyphers; and therefore you must observe in what place of the multiplier the figure you multiply by standeth, and let the first figure of that product under the same place of the product of the first figure of your multiplier: As for Example, let it be required to multiply 371568 by 40007, first I multiply the multiplicand by 7, and the product is 2600976, then neglecting the Cyphers I multiply by 4, and that product is 1486272; now I confider that 4 is the fifth figure in the multiplier, therefore I place two (the first figure of the product by 4) under the fifth place of the first product by 7, and

1486 3320976

the rest in order, and having added them together, the total product is found to be 14865320976. Other Examples in this Rule are these following;

| 327586 | 7864371 |
|------------|----------------------|
| 6030 | 20604 |
| 9827520 | 21409484 |
| 1965515 | 31457484 47186226 |
| | 15728742 |
| 1975343580 | 162037500084 |

9. If you are to multiply any Number by an Unit with Cyphers, (viz.) by 10, 100, 1000, Oc. then annex so many Cyphers before the Multiplicand, and that number when the Cyphers are annexed is the product required; as if you would multiply 428 by 100. annex two Cyphers to 428 and it is 42800 : If it were Google required required to multiply 102 by 1000; annex 4 Cyphers, and it gives 1020,00 for the Product required.

The Proof of Multiplication.

10. Multiplication is proved by Division, and to speak truth all other ways are falle; and therefore it

will be most convenient in the first place to learn Division, and by that to prove Multiplication. There is a Way (at this day generally used in Schools) to prove Multiplica-

Non est quod aliam expelles examinandes viam, nam alia vulgares & falfa sunt, & nullo innixa sundamento, Genma Frissu,

tion, which is this, first add all the Figures in the Multiplicand together, as if they were simple Numbers, casting away the Nines as often as it comes to so much, and noting the remainder at last, which in this case cannot be so much as 9: Cast likewise the Nines out of the Multiplier as you did out of the Multiplicand. and note that remainder; then multiply the Remainders, the one by the other, and cast the Nines out of the Product, observing the Remainder; and lastly, cast the Nines out of the total Product, and if this Remainder be equal to the Remainder last found, then they conclude the Work to be rightly performed; but there may be given a thouland (nay infinite) false Products in Multiplication, which after this manner may be proved to be true, and therefore this way of proving doth not deferve any Example; but we shall defer the proof of this Rule till we come to prove Division, and then we shall prove them both together

11. The general effect of Multiplication is contained in the definition of the same, which is to find out a third number, so often containing one of the two given

Numbers as the other containeth Units.

The second effect is by having the length and breadth of any thing (as a Parallelogram, or long Plane) to find the superficial Content of the same, and by having the superficial Content of the Base, and the length to find out the solidity of any Parallelipipedon, Cylinder, or other solid Figures.

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The third Effect is by the Contents, Price, Value, Buying, Selling, Expence, Wages, Exchange, fimple Interest, Gain or Loss of any one thing, be it Money. Merchandize, drc. to find out the Value, Price, Expence, Buying, Selling, Exchange, or Interest of any number of things of like Name, Nature and Kind.

The fourth Effect is (not much unlike the other) by the Contents, Value, or Price of one part of any thing denominated, to find out the Content, Value, or Price of the whole thing, all the parts into which the whole is divided, multiplying the price of one of

those parts.

The fifth Effect is, to aid, to compound, and to make other Rules, as chiefly the Rule of Proportion, called the Golden Rule, or Rule of Three; also by it, things of one denomination are reduced to another.

If you multiply any number of Integers or the price of the Integer, the product will discover the price of

the Quantity or Number of Integers given.

In a Restangular Solid, if you multiply the breadth of the Base by the depth, and that product by the length, this last product will discover the Solidity or Content of the same Solids to the

Some Questions proper to this Rule may be these following.

Quest. 1. What is the Content of a square piece of Ground, whose length is 28 Perches, and breadth 12 Perches?

Answ. 264 square Perches; for multiplying 28 the

length by the breadth, the product is formuch.

Quest. 2. There is a square Battle whose Flank is 47 Men, and the Files 19 deep, what number of Men doth that Battle contain? Facit 802; for multiply-

ing 47 by 19, the product is 893.

Quest. 3. If any one thing cost 4 Shillings, what finall 9 such things cost? Answ. 36 Shillings; for multiply-

ing 4 by 9, the product is 36.

Quest. 4. If a piece of Money or Merchandize be worth or cost 17 Shillings, what shall 19 such pieces :::1

of Money or Merchandize coft ? Facit 323 Shillings,

which is equal to 16 1. 3 s.

Quest. 5. If a Soldier or Servant get or spend 14 s. per Month, what is the Wages or Charges of 49 Soldiers or Servants for the same time? Multiply 49 by 14, the Product is 686 s. or:241.6 s. for the Answer.

Quest. 6. If in a day there are 24 hours, how many hours are there in a year, accounting 365 days to conditute the year? Facis 8760 hours; to which if you add the 6 hours over and above 365 days, as there is in a year, then it will be 8766 hours; now if you multiply this 8766 by 60, the number of minutes in an hour, it will produce \$25960 for the number of minutes in a year.

CHAP. VII.

Of Division of Whole Numbers.

I. IVIS ION is the separating or parting of any Number or Quantity, given into any parts as signed; or to find how often one Number is contained in another :: Or from any two Numbers given to find a third that shall confist of so many besits, as the one of those two given Numbers is comprehended or contained in the otherwise.

"2. Division hathithree Parts or Numbers remarkable, viz. Eirst, the Dividend. Secondly, the Divisor. Thirdly; the Quotient. The Dividend is the Humber given to be parted or divided. The Divisor is the blumber given, by which the Dividend is divided. Or it is the Number which sheweth how many parts the Dividend is to be divided into 2. And the Quotient is the Number produced by the Division of the two given Numbers, the one by the other.

So 12 being given to be divided by 3, or into three equal parts, the Quotient will be 4, for 3 is contain'd in 12 four times, where 12 is the Dividend, and 3 is the Divisor, and 4 is the Quotient.

3. In Division fet down your dividend, and draw a crooked line at each end of it, and before the line at the left-hand, place the divisor, and behind that on the right-hand, place the Figures of the quotient, as in the Margent, where it is 3) 12 (4 required to divide 12 by 312 First, 1 fet down 12 the dividend, and on reach side of it do I draw a crooked line, and before that on the left hand do I place 3 the divisor; then do I feek now often 3 is pon-

tained in 12, and because I find it 4 times, I put 4 behind the crooked line on the right-hand of the divi-

dend, denoting the quotient.

4. But if when the divisor is a single kigure, the dividend confisheth of two or more places, then that ving placed them for the Work as is before directed) put a point under the first figure on the lest-hand of the dividend, provided it be bigger than (or equal to) the divisor, but if it be lesser than the divisor, then put a point under the second figure from the lefthand of the dividend, which figures as far as the point goeth from the left-hand are to be reckoned by themselves, as if they had no dependance upon the other part of the dividend, and for distinction sake may be called the dividual; then ask how often the divisor is contained in the dividual, placing the Anfwer in the quotient; then multiply the divisor by the figure that you placed in the quotient, and let the product thereof under the dividual; then draw a line under that product, and subtract the faid product from the dividual, placing the remainder under the faid line, then put a point under the next figure in the dividend, on the right-hand of that which you out the point before, and draw it down, placing it on the right hand of the remainder; which you found by Subtraction; which remainder with the faid figure annexed before it, shall be a new dividual; then seek again how often the divisor is contained in this new dividual; and put the Answer in the quotient on the right-hand of the figure which you put there before, then multiply the divisor by the last figure that you nighted by Google ... put

put in the Quotient, and subscribe the product under the dividual, and make Subtraction, and to the re-mainder draw down the next figure from the grand dividend, (having first put a point under it) and put it on the right hand of the remainder for a new dividual as before, &c. and proceed thus till the Work is finished.

Observing this general Rule in all kinds of Division. first to seek how often the divisor is contained, in the dividual; then (having put the Answer in the Quotient) multiply the divisor thereby, and subtract the product from the dividual. An Example or two will make the Rule plain. Let it be required to divide 2184 by 6. I dispose of the Numbers given as is before directed, and as you fee in the Mar-

gent, in order to the Work; then (because 6 the divisor is more than 2 the first Flgure of the dividend) I put a point under 1 the fecond Figure, which makes the 21 for the dividual, then do I ask how often 6 the divisor is contained in 21, and because I cannot have it more than 3 times, I put a in the Quotient, and thereby do I multiply the divisor (6) and the product by 18, which I fet in order under the dividual, and subtract it therefrom, and the remainder (3) I place in order under the line, as you fee in the Margent.

Then do I make a point under the next Figure of the dividend being 8, and draw it down, placing it before the re-mainder 3, so have 1 38 for a new dividual, then do I feek how often 6 is contained in 38, and because I cannot have more than 6 times, I put 6 in the Quotient, and thereby do I multiply the divisor 6, and the product (36) I put under the dividual (38) and subtract it therefrom, and the remainder 2 I put under the Line, as you fee in the Margent.

6)2184(

6)2184(3

6)2184(36

Then

Chap. 7.

| Then do I put a point under the next gure of the dividend (being 4) and draw | (and laft) fi- |
|---|----------------|
| It down to the remainder 2, and putting | 6)2184(364 |
| it on the Right-hand thereof, it marketh 24 for a new dividual; then I | 18 |
| feek how often 6 is contained in 24, and the Answer is 4, which I put in the | |
| quotient, and multiply the divisor (6) | 38 30 |
| thereby; and the product (24) I put under the dividual (24) and subtract | 24 |
| it therefrom, and the remainder is d. | 24 |
| and thus the Work is finished, and I find the quotient to be 364, that is, 6 | (0) |
| is contained in 2184 just 364 times, or 2184 being divided into 6 equal parts, 36 | ' - |
| those parts. | 4 15 One or |

Again, If it were required to divide 2646 by 7, or into 7 equal parts, the quotient would be found to be 378, as by the following Operation appeareth.

| 7) | 2 64 6 | (378 |
|----|----------------------|------|
| | 21 | |
| , | 54 49 | |
| | 56 56 | |
| | (o) | • |

So if it were required to divide 946 by 8, the quotient will be found to be 118, and 2 remaining after Division is ended. The Work followeth.

| hap. 7. | whole Numbe |
|---------|-------------|
| | 8) 946 (118 |
| | 8. |
| • | 14 |
| | 66 |

Many times the dividend cannot exactly be divided by the divisor, but something will remain, as in the last Example, where 946 was given to be divided by 8, the quotient was 118, and there remaineth 2 after the Division is ended: Now what is to be done in this case with the remainder, the Learner shall be taught when we come to treat of reducing (or Reduction) of Fractions.

(2)

And here note, that if after your Division is ended, any thing do remain, it must be lesser than your divisor, for otherwise your Work is not rightly perform d.

Other Examples are such as follow.

| 8) 73464 (9:83 | 9) 13758 (1528 |
|----------------|----------------|
| 72 | 9 |
| 14. | 47 |
| 66 | 25 18 |
| 24 | 78 72 • |
| (o) D 2 | (6) |

5. But if the divisor consistent of more places than one, then chuse so many figures from the left side of the dividend for a dividual as there are figures in the divider, and put a point under the farthest figure of that dividual to the right-hand, and seek how often the first sigure on the left side of the divisor, is contained in the first sigure on the left side of the dividual, and place the Answer in the Quotient, and thereby multiply your divisor, placing your product under your dividual, and subtrast it therefrom, placing the

remainder below the line; then put a point under the next figure in the dividend, and draw it down to the faid remainder, and annex it on the right fide thereof, which makes a new dividual, and proceed as before,

till the Work is finished.

And if it so happen that after you have chosen your first dividual (as is before directed) you find it to, be lesser than the divisor, then put a point under a figure more near to the right-hand, and seek how often the first figure on the lest side of the divisor is contained in the two first figures on the lest side of the dividual, and place the answer in the quotient, by which multiply the divisor, and place the product thereof in order under the dividual, and subtract it therefrom, and proceed as before.

Always remembring, that (in all the cases of Division) if after you have multiplied your divisor by the figure last placed in the Quotient, the product be greater than the dividual, then you must cancel that figure in the Quotient, and instead thereof put a figure lesser by a Unit, (or one) and multiply the divisor thereby, and if still the product be greater than the dividual, make the figure in the quotient yet lesser by a Unit, and thus do until your product be lesser than the dividual, or at the most equal thereto, and then make Subtraction, Occ.

So if you would divide 9454 by 24, the quotient will be found to be 394; I first put down the given Numbers, as is before directed in the third Rule: Now because

because my divisor consistent of two
Figures, I therefore put a point under
the Iccond Figure from the left-hand
in my dividend, which here is 4,
wherefore I seek how often 2 the first
figure (on the left fide of the divisor)
is contained in 9 (the like first in the
dividual) the answer is 4, which I put in the q
and thereby multiply all the divisors, and find

24) 9464 (4 72 22

dividual) the answer is 4. which I put in the quotient, and thereby multiply all the divisors, and find the product to be 96, which is greater than the dividual 94, wherefore I cancel the 4 in the quotient, and instead thereof I put 3 (a Unit lesser) and by it multiply the divisor 34, and the product is 72, which I subtract from 94 the dividual, and the remainder is 22, then do I make a point under the next figure 6 in the dividual

dend, and draw it do vn and place it on the right fide of the remainder 22, and it makes 226 for a new dividual.

24) 9464 (39 -

and it makes 225 for a new dividual, now because the dividual 226 consistent of a Figure more than the divisor, therefore I seek how often 2 (the first figure of the divisor is contained in 22, the two first of the dividual) I say 9 times, wherefore I put 9 in the quotient, and thereby multiply the

226

divisor 24, the product (216) I place under the dividual 226, and subtract it from it, and there remains
eth 10.

Then I go on and make a point under the next and last Figure (4) in the dividend, and draw it down to the remainder 10, and it maketh 104, for a new dividual, which is also a figure more than the divisor, and therefore I seek how often two is contained in 10, I answer 5 times, but multiplying my divisor by 5, the product is 120, which is greater than the dividual, and therefore I make it but 4, and by it multiply the divisor, and the product is 96, which being placed under, and subtracted from the dividual, there remainesh 8, and thus the whole Work of this Division is ended, and I find that 9464 being divided by 24,

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. *(*

or into 24 equal parts, is found to be 304, as was faid before, and the remainder is 8, as you fee in the work fellowing,

24) 9464 (394

| 72 | |
|------------|--|
| 226 216 | |
| 104 96 | |
| (8) | |

Another Example may be this, let there be required the quotient of 1183653 divided by 385; first I difpose of the numbers in order

to their dividing, and because 118 the three first figures of the

dividend is leffer than the di-

visor 385, I therefore make a point under the fourth figure, which is 3, and feek how often 3 (the first figure of the divisor) is contained in 11? The Answer is 3, which I put in the Quotient, and thereby multiply the

divifor 385, and the product is 1155, which I subtract from the dividual 1188, and there remains 28. Then (as before) I draw down the next figure, which is 6, and 385) 1183653 (30

place it before the remainder 28, To have I 286 for a new dividual, and because it hath no more fi-

gures than the divilor. I feek how

often 3 (the first figure in the di-

often 3 (the first figure in the di-visor) is contained in 2 (the first figure of the dividu-al) and the Answer is 0, for a greater number cannot be contained in a lesser, wherefore I put o in the quotient, and thereby (according to the 5th Rule) I should multiply my divisor, but if I do the product will be c,

385) 1183653 (3.

| Unap. 7. whose Inum | moers. |
|---|---------------------------|
| and o fubtracted from the divid | dual 286, the remainder |
| is the fame; wherefore I dra | |
| down the next figure (5) fro | om 385) 1183653 (307 |
| the dividend, and put it befo | ore ··· |
| the faid remainder 286, so ha | we 1155 |
| I 2865 for a new dividual, at | nd |
| because it consistes of four pl | la- 2865 |
| ces, viz. a place more than t | the 2695 |
| divisor, I seek how often 3 (t | the |
| first figure of the divisor) is co | 30- (170) · · |
| tained in 28 (the two first of t | the and the second |
| dividual) and I fay there is 9 t | times 3 in 28, but mul- |
| tiplying my whole divisor (| (284) thereby I find the |
| product to be 2465, which is | s greater than the divi- |
| dual 2865, wherefore I chufe | e 8, which is leffer by |
| a Unit than 9, and thereby | I multiply my divifor |
| 385, and the product is 3080 | o, which still is greater |
| than the faid dividual, wheref | fore I chuse another num- |
| ber jet a Unit lesser, viz. 7; | and having multiplied |
| my divisor thereby, the pro- | stuck is 2605, which is |
| lefter than the dividual 2865, | wherefore I put 7 in the |
| quotient, and subtract 2695 | from the dividual 2365, |
| and there remains 170; then | I draw down the last si- |
| gure (3) in the dividend, and | place it before the faid |
| remainder 170, and it mak | tes |
| 1703 for a new dividual, the | cu 385)1183553(3074 |
| (for the Reason abovefuld) |) I |
| feek how often 3 is contained | in 1155 |
| 17, the answer is 5, but mult | []- |
| plying the divisor thereby, the | he 2865 🔻 |
| product is (1925) greater the | an 2595 |
| product is (1925) greater the dividual, wherefore I for | ay —— |
| it wall bear 1 (a Unit Jeller) ar | nd 1703: |
| by it 1 multiply the divisor 38 | 85 1540 |
| and the product is 1540, which | ch . |
| is lesser than the dividual, ar | nd (163) |
| therefore I put 4 in the qu | IO- |

tient, and subtract the said product from the dividual, and there remaineth 163, and thus the Work is finished, and I find that 1183653 being divided by 385, or.

or into 385 equal shares or parts, the Quotient (or one of those parts) is 3074, and besides there is 163 remaining.

And thus the Learner being well versed in the Method of the foregoing Examples, he may be sufficiently qualified for the dividing of any greater Sum or Number into as many parts as he pleaseth, that is, he may understand the method of dividing by a divisor, which consistes of 4, or 5, or 6, or any greater

vifor, which confifteth of 4, or 5, or 6, or any greater number of places, the Method being the same with the foregoing Examples in every respect.

Other Examples in Division. 27986) 835684790 (29860

196374) 473986018 (2413

812380 785496

268841 196374

> 72467**8** 589122

Remains (135556)

So it you divide 47386473 by 58736, you will find the Quotient to be 806, and 45257 will remain after the work is ended.

In like manner if you would divide 3846789204 by 483064, the quotient will be 7963, and the re-

mainder after Division will be 100572.

Compendiams in Division.

I. IF any given Number be to be divided by another number that hath Cyphers annexed on the right fide thereof, (omitting the Cyphers) you may cut off

for miny Figures from the right hand of the dividend, as there are Gyphers before the divisor, and let the remaining Number in the dividend, be divided by the remaining number or numbers in the divisor, ob-

Et in Divifor adjunctos fibi habeat Circulos ad dextran, omifficirculis & absolits rotades ultimis Figuris dividendi in num-ris religati fact divitio, in fine autem divitions reft taroda funt tum on fill circuli; tum figura absolits. Ought. Cla. Marth. cap. § 3.

ferving this Gaution, that if after your Division is ended any thing remain, you are to annex thereso, the number or numbers that were cut off from the dividend; and such new found number shall be the Bernainder.

As for Example: Let it be required to divide 456,8 by 400; now because there are two Cyphers before the Divisor, I cut off as many Figures from before the Dividend, viz. 58, so that then there will remain only 465 to be divided by 4, and the quotient will be 116, and there will remain 2, to which, I annex the two figures (58) which were cut off from the dividend, and it makes 258 for the true remainder, so that I conclude

4 00) 456 | 58 (116.

46658 being divided by 400, the quotient will be 115, and 258 remainerh after the Work is ended; as by the Work in the Margent-

2. And

a. And hence it followeth that if the divisor be (1) or a Unit with Cyphersan-

nexed, you may cut off so many figures from before the dividend, as there are Cyphers in the divisor, and then the figure or fi-

Divisurus quemeumojue numerum per 10. Austre ex dextra parte unicam, eamque primam figuram 2 Relique enim figura produktum oftendunt. Ablatum Residuum, &c. Gem. Fris Arith. part. 1.

gures that are on the Left-hand, will be the Quotient, and those that are on the Right-hand will be the Remainder after the Division is ended: As thus, if 45783 were to be divided by 10, I cut off the last singure (3) with a dash thus (4578|3) and the work is done, and the quotient is 4578 (the number on the lest-hand of the dash) and the remainder is 3 (on the right-hand;) in like manner if the same number 45783 were to be divided by 200, I cut off two figures from the end thus (457|83) and the quotient is 457, and the remainder is 83. And if I were to divide the same by 1000, I cut off 3 figures from the end thus, (45|783) and the Quotient is 45, and 783 the remainder. Orc.

6. The General Effect of Division is contained in the definition of the same (that is) by having two unequal numbers given to find a third Number in such proportion to the dividend, as the divisor hath to Unit or 1, it also discovers what reason or proportion there is between numbers, so if you divide 12 by 4, it quotes 3, which shows the reason or proportion of 4 to 12

is triple.

The fecond effect is by the superficial measure or content, and the length of any Oblong, Restangular Parellelogram, or square Plane known, to find out the

breadth thereby, or contrariwife by having the superficies, and breadth of the said figure, to find out the length thereof. Also by having the solidity and length of a solid, to find the superficies of the Base, & contra.

The third Effect is, by the Contents, Reason, Price, Value, Buying, Selling, Expences, Wages, Exchange, Interest, Profit or Loss of any number of things (be it Money, Merchandize, or what else) to find out the

Con-

Contents, Reason, Price, Value, Buying, Selling, Expense, Wages, Exchange, Interest, Profit or Los, of

any one thing of like kind.

The fourth Effect is to aid, to compole, and to make other Rules, but principally the Rule of Proportion, called the Golden Rule, or Rule of Three, and the Reduction of Moneys, Weights, and Measures, of one denomination into another, by it also Fractions are abbreviated by finding a common measurer, unto the Numerator and Denominator, thereby discovering commensurable numbers.

If you divide the value of any certain quantity, by the same quantity, the quotient discovers the rate or value of the Integer, as if 8 yards of Cloth cost 96 smillings; if you divide (96) the value or price of the given quantity, by (8) the same quantity, the quotient will be 12, which is the price or value of 1 of those

yards, & è contra.

If you divide the value or price of any unknown quantity, by the value of the Integer, it gives you in the quotient that unknown quantity whose price is thus divided; as if 12 shillings were the value of a yard, I would know how many yards are worth 96 shillings: Here if you divide (96) the price or value of the unknown quantity, by (12) the rate of the Integer, or one yard, the quotient will be 8, which is the number of yards worth 96 shillings.

Some Questions answered by Division may be these following.

Quest. 1. If 22 things cost 66 shillings, what will a such thing cost? Facit, 3 shillings; for if you divide 66 by 22, the quotient is 3 for the Answer; so if 36 yards or ells of any thing be bought or sold for 108 show much shall 1 yard or ell be bought or sold for 2 Facit 31. for if you divide 108 show 36 yards, the quotient will be 3 show price of the integer.

Queft. 2. If the Expence, Charges or Wages of quears amount to 868 l. what is the Expence, Charges or Wages of one year? Facit 124 l. for if you divide

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868 (the Wages of 7 years) by 7 (the number of years) the quotient will be 124 l. for the Answer. See the Work.

7) 868 (124

(0)

Quest. 3. If the content of one superficial Foot be 144 Inches, and the breadth of a board be 9 Inches, how many inches of that board in length will make such a foot? Facit, 16 inches, for by dividing 144 (the number of square inches in a square foot) by 9 (the inches in the breadth of the board) the Quotient is 16 for the number of inches in length of that board to make a superficial Foot.

9) 144 (16 Inches

54

· (o) :

gaest. 4. If the content of an Acre of Ground be 160 square Perches, and the length of a Furlong (propounded) be 80 Perches, how many Perches will there go in breadth to make an Acre? Facit, 2 Perches; for if you divide 160 (the number of Perches in an Acre) by 80 (the length of the Furlong in Perches) the quotient is 2 Perches; and so many in breath of that Furlong will make an Acre.

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80) 160 (2 Perches

160

Quest. 5. If there be 893 Men to be mide up into a Battle, the front consists of 47 Men, what number must there be in the File? Facit, 19 deep in the File: For if you divide 893 (the number of Men) by 47 (the number in front) the quotient will be 19 File in depth; the Work followeth;

47) 893 (19 dap in file

guest. 6. There is a Table whose superficial content is 72 feet; and the breadth of it at the end is 3 feet, now I demand what is the length of this Table? Facit, 24 feet long; for if you divide 72 (the content of the Table in feet) by 3 (the breadth of it) the Quotient is 24 feet for the length thereof, which was required. See the Operation as followeth;

3) 72 (24

6

12

12

(0)

The Proof of Multiplication and Division.

Multiplication and Division interchangeably prove each other; for if you would prove a Sum in Division, whether the Operation be right or no, multiply the

the quotient by the divisor; and if any thing remain after the Division was ended, add it to the product, which product (if your sum was rightly divided) will be equal to the dividend: And contrariwise, if you would prove a sum in Multiplication, divide the product by the multiplyer, and if the Work was rightly performed, the quotient will be equal to the multiplicand. See the Example where the Work is done and undone. Let 7654 be given to be multiplied by 3242, the product will be 24814268, as by the Work appeareth.

And then if you divide the faid product 24814268 by 3242 the multiplyer, the quotient will be 7654, equal to the given multiplicand.

(o)

In like manner (to prove 2 sum or number in Division) if 24814268 were divided by 3242, the Quotient will be found to be 7654; then for proof, if you multiply 7654 the quotient by 3254 the divisor, the product will amount to 24814268, equal to the dividend.

Or you may prove the last, or any other Example in Multiplication thus, viz. divide the product by the multiplicand, and the Quotient will be equal to the mul-

tiplier. See the Work.

| | 7654 3242 | |
|-------|----------------------------------|--------------|
| | 15308 30616 15308 22962 | , |
| 7654) | 24814268 | (324 |
| • | 18522 15308 | |
| | 32146 30616 | |
| | 15308 | - |
| ** - | (0) | |

From whence there arises this Corollary, that any Operation in Division may be proved by Division; for if after your Division is ended, you divide the dividend by the quotient, the new quotient thence arising will be equal to the divisor of the first Operation; for tryal whereof let the last Example be again repeated.

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3242) 24814268 (7654

| 22694 |
|----------------|
| 21202 19452 |
| 17506 |
| 12968 |
| (0) |

For Proof whereof divide again 24814268 by the Quotient 5654, and the Quotient hence will be equal to the first divisor 3242; see the Work.

7654) 24814268 (3242

Rut in proving Division by Division, the Learner is to observe this following Caution, that if after his Division is ended there be any Remainder, before you go about to prove your Work, subtract that Remainder out of your dividend, and then work as before, as in the following Example, where it is required to divide 428.76 by 755, the Quotient here is 57, and the remainder is 271; see the Work following.

765)

765) 43876 (57

3825 5626 5355

(271)

Now to prove this Work, subtract the remainder 271 out of the dividend 43876, and there remaineth 43605 for a new dividend to be divided by the former quotient 57, and the quotient thence arising is 765 equal to the given Divisor, which proveth the Operation to be right.

43876 271

57) 43605 (765

399

370 342

> 285. 285

(o)

Thus have we gone through the four Species of

Arithmetick, viz. Addition, Subtraction, Multiplication, and Division; upon which all the following Rules and all other Operations whatsoever that are possible to be wrought by Numbers have their immediate dependance

who will be their immediate dependance, and by them are resolved. Therefore before the Learner make a surther step in this Art, let him be well acquainted with what hath been delivered in the foregoing Chapters.

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Ha sunt igitur quatur illa species Arithmetices per quas omnia

quacunque deinceps dicenda funt

iel que per numeros fieri possi-

bile eft, abselvuniur Quare eas

quisquis es ante omnia perdisces. Gem. Fist. Arich par.-1.

CHAP. VIII.

Of Reduction.

Reduction is that which brings together two or more numbers of different denominations into one denomination; or it ferveth to thill's Arith. change or alter Numbers, Money, Weight, c. 13, p.152. Measure of Time, from one denomination to another; and likewise to abridge. Fractions to their lowest Terms. All which it dother for precisely, that the first proportion remained without the least jot of Error or Wrong committed; so that it belongeth as well to Fractions as Integers, of which in its proper place. Reduction is generally performed either by Multiplication or Division; from whence we may gather, that,

2. Reduction is either descending or ascending.

3. Reduction descending, is when it is required to reduce a Sum or Number of a greater denomination, into a lesser; which Number, when it is so reduced, shall be equal in value to the Number sirst given in the greater denomination; as if it were re-

wing. Arith. quired to know how many shiftings, pence ch. 7. 2, 3, 4. or farthings are equal in value to an hundred pounds? or how many ounces are con-

tained in 45 hundred weight? or how many days, hours or minutes there are in 240 years, Go. And this kind of Reduction is generally performed by Multiplication.

4. Reduction alcending, is when it is required to reduce or bring a fum or number of a similar denomination into a greater, which shall be equivalent to the given number; as suppose it were required to find out how many Pence, Shillings or Pounds are equal in value to 4378; Farthings; or how many hundreds are equal to (or in) 3748 Pounds, Gr. and this kind of Reduction is always performed by Division.

5. When a Sum or Number is given to be reduced into another denomination; you are to confider when

ther it ought to be refolved by the Rule descending or ascending, viz. by Multiplication or Division: If it be to be performed by Multiplication, consider how many parts of the denomination into which you would reduce it, are contained in a Unit or Integer of the given number, and multiply the said given number thereby, and the product thereof will be the Answer to the Question. As if the Question were in 38 Pounds, how many Shillings? Here I 38 consider, that in one Pound are 20 Shillings, 20 and that the number of shillings in 38 pounds will be 20 times 38, where I multiply 750 38 l. by 20, and that product is 750, and so many shillings are contained in 38 pounds, as in the Margent.

But when there is a denomination, or denominations between the number given, and the number required, you may (if you please) reduce it into the next inferiour denomination, and then into the next

lower than that, Gr. until you have brought it into the denomination required: As for Example. Let it be demanded in 132 pounds how many farthings? First, I multiply 132 (the number of pounds given) by 20, to bring it into shillings, and it makes 2640 shillings, then do I multiply the shillings (2640) by 12, to bring them into pence, and it produceth 31680, and so many pence are contained in 2640 shillings, or 132 pounds; then do I multiply the pence, viz. 31680

132 pounds

2640 Shill.

5280

2640

31680 pence

4

116720 farth.

by 4 to bring them into farrhings (because 4 farthings is a penny) and I find the product thereof to be 126720, and so many farthings are equal in value to 132 pounds, the Work is manifest in the Margent.

6. And if the number propounded to be reduced, is to be divided, or wrought by the Rule Afcending,

an Unit or Integer, in that denomination to which you w. uld reduce your given number, and make that your divifor, and the given number your dividend; and the quotient thence arifing will be the number fought or required: As for Example, Let it be required to reduce 2640 Shillings into Pounds. Here I confider that 20 Shillings are equal to one Pound; wherefore I divide 2640 (the given Number) by 20, and the Quotient is 132, and so many Pounds are contained in 2640 Shillings. In Reduction descending and ascending the Learner is advised to take particular. notice of the Tables delivered in the fecond Chapter of this Book,

where he may be informed what

20) 264 C (122

Multipliers or Divisors to make use of in the reducing of any Number to any other denomination whatfoever, especially English Moneys, Weights, Measures, Time and Motion; but in this place it is not convenient to meddle with Foreign Coins, Weights or Measures.

But if in Reduction alcending it happen that there is a denomination or denominations between the number given, and the number required, then you may reduce your number given into the next superiour denomination, and when it is so reduced, bring it into the next above that, and to on until you have brought it into the denomination required. As for Example,

Let it be demanded in 125720 furthings how many Pounds? First, I divide my given number (being farthings) by 4, to bring them into pence (because 4 farthings make one penny) and they are 21680 pence, then I divide 31680 pence by 12, and the Quotient giveth 2540 (hillings, and then I divide 2640 shillings by 20, and the quotient giveth 132 pounds, which are equal in value to 125720 farthings. See the whole Work as it followeth.

| .4) 126720 | T2) (31580 | 2 0) (264 0 | L (132 |
|------------|---------------|----------------|-----------|
| 12 | 24 . | 2 | |
| 6 | 76 72 | '6 6 | |
| 27 24 | 48 | 4 | |
| 32 | (o) | (0) | |
| (0) | | • | |

7. when the number given to be reduced, confifteth of divers denominations, as pounds, Willings, pence and farthings, or of hundreds, quarters, pounds and ounces,&c. then you are to reduce the highest (or greatest) denomination into the next interiour, and add thereunto the number standing in that denomination which your greatell or highest number is reflyced to; then reduce that Sum into the next inferiour Denomination, adding thereto the number flanding in that denon instion; do. so until you have brought the number given into the denomination proposed. As if it were required to reduce 42 l. 13 s. 4 d-into pence; first, I bring 48 l. into shillings, by multiplying it by 20, and the product is 960 shillings, to which I add the 13 shillings, and they make 973, then | multiply 973 by 12, to rring the shillings into rence, and they make 11675 pence, to which I add the 10 pence, and they make 11686 pence for the Answer. See the Work done.

as Bar Agtors

d. 48--13--10 20 960 (hillings

Add 12

Sum 973 shillings I Ź

> 1946 973

11676 pence Add

Sum 11686 pence

8. If (in Reduction Ascending) after Division is ended, any thing remain, such remainder is of the same denomination with the dividend.

In 4783 farthings, I demand how many Example.

pounds.

First, I divide the given number of farthings, (viz. 4783) by 4 to bring them into pence, and the quotient is 1195 pence, and there remaineth 3 after the work of Division is ended, which is 3 farthings.

Again, I divide 1195 pence (the said quotient) by 12, to reduce them into shillings, and the quotient is 99 shillings, and there is a remainder of 7, which is 7

pence.

And then I divide 99 shillings (the last quotient) by 20, to bring it into pounds, and the quotient is 4 l. and there remaineth 19 shillings; so that I conclude that in 4783 (the proposed number of farthings) there is 4 pounds, 19 shillings, 7 pence, 3 farthings. View the following Operation.

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Chap. 8.

4) 4783 (1195 (99 (4 pounds

4 108 8

7 115 (19) shillings

4 108

38 rem. (7) pence

36

1. s. d. qre.

22 Eacit 4—15—7—3

Rem. (3) farthings

20/

More Examples in Reduction of Coin.

Quest. t. In 438 L how many shillings? Facit 8760 shillings; for by multiplying 438 by 20, the product amounteth to so much. See the Work.

20

Facit 8760 shillings
Quest. 2. In 467 l. how many pence? First, multiply the given number of pounds (467) by 20 to bring it into shillings, and it makes 9340 shillings, then multiply the shillings by 12, and it produceth 112080 pence; thus,

457 pounds 20 shillings

9340 shillings

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18680 **9**340

Facit 112080 pence

Or it may be refolved thus, viz. multiply the given number of pounds (467) by (240) the number of pence in a pound, and the product is the fame, viz. 112080 pence, as by the Operation appeareth.

| | 467 240 | pouna |
|---|-------------|-------|
| _ | 8689 34. | |

Facit 112080 pence

Quest. 3 In 5673 l. how many farthings? First, multiply the given number by 20, to bring it info shillings, and it produceth 113460 shillings, then multiply that product by 12, to bring it into pence, and it produceth 1361520 pence; then lastly, multiply the pence by 4, and it produceth 5446080 farthings. See the Operation.

Facit 5446680 farthings.

Or this Question might have been thus resolved, viz. Multiply 5673 (the given number of pounds) by 960 (the number of farthings in a pound) and it produceth the same Essett, as you may see by the Work.

| 5673 pounds | 20 shillings |
|--------------------------|---------------|
| 960 | _12 |
| - | |
| 3 4038 0 ` | 240 pence |
| 51057 | 4 |
| Facit 5446080 farthings | 960 farthings |

Otherwise thus: First bring the given number 5673 l. into shillings, and multiply the shillings by 48, the number of farthings in a shilling, and the same effect is thereby likewise produced, viz.

| 5673 pounds | | 12 pence |
|------------------------|---|--------------|
| 113460 fbillings 48 | | 48 farthings |
| 907680 | • | |

Facit 5446080 farthings

These various ways of operating are expressed to inform the Judgment of the Learner, with the Reufon of the Rule; more ways may be shown, but these are sufficient even for the meanest Capacities.

Quest. 4. In 458 l. 16 s. 7 d. 3 grs. how many farthings ? To resolve this Question consider the seventh Rule of this Chapter, and work as you are there directed, and you will find the aforesaid given number to amount to 440479 farthings, viz.

⊕

| _ | , |
|-----|-------------------------------|
| • | 1. s. d. o 458—16—7— 20 |
| Add | 9160 shillings |
| Sum | '9176 shillings |
| - | 18352 9176 |
| Add | 110112 pence 7 |
| Sum | 110119 pence |
| Add | 440476 farthings 3 |
| Sum | 440479 farthings |

This last Question (or any other of this kind, viz. where the number given to be reduced consistent of several denominations) may be more concisely resolved thus, viz. when you multiply the pounds by 20, to bring them into shillings, to the product of the first Figure, add the Figure standing in the place of Units in the denomination of shillings, but because the first figure in the Multiplyer is (o) I say 0 times 8 is nothing, but 6 is 6, which I put down for the first figure in the product, then because this multiplyer is 0, I go on no further with it, for if I should, the whole product would be 0, but proceed, and when I come to multiply by the second figure in the multiplyer, and to the product of it, I add the figure standing in the place of Tens in the denomination of shillings which

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is.(1) faying 2 times 8 is 16, and (the faid figure) 1 is 17, then I set down 7, and carry an Unit to the product of the next figure as is directed in the fifth Rule of the fixth Chapter foregoing; and finish the Work. So that you now have the whole product and sum of Shillings at one Operation, which is the same as before, and when you multiply the Shillings by 12, to bring them into pence (after the same manner) add to the product the number standing in the denomination of pence, and so when you multiply the pence by 4 to bring them into farthings, add to the product the number standing under the denomination of farthings. See the last Question thus wrought.

1. s. d. qrs
458—16—7—3
20
9176 shillings
12
18359
9176
110119 pence
4

Facit 440479 farthings

After the method last prescribed (which if rightly confidered, differeth not any thing from the 7th Rule of this Chapter) are all the following Examples that are of the same nature wrought and resolved.

Quest. 5. In 4375866 tarthings, I demand how ma-

ny pounds, shillings, pence, and farthings?

To resolve this Question; First, I divide the given number of farthings by 4, and the quotient is 1093966 pence, and there remaineth 2 after the Division is ended (which by the 8th Rule foregoing) is two farthings; then I divide 1093966 pence by 12, and the E. 2

Quotient is 91163 shillings, and there remaineth 10 after Division, which by the said 8th Rule is so many pence, viz. to d. then I divide 91163 shillings by 20, and the Quotient is 4558 l. and there remaineth 3 shillings, so the Work is finished, and I find that in 4375866 farthings there are 4558 l. 3s. to d. 2 qrs See the Operation.

| 4) 43 | 375866 | 12) (1093966 | 2 0) (9116 3 | l. (4548 | ·, . |
|-------|----------|------------------|-----------------|-------------|-----------|
| 4 | 17 16 | 13 12 19 | 11 | | |
| • | 38 36 | 76 72 | 16 | | · |
| | 26 24 | 46 36 | (3) | ş. | , · · · · |
| (| 26 24 | |). d. | | |
| | (2) | grs. | | | |
| | Facit | 4558 | s. — 3—— | d. 10 | qrs. |

Quest. 6. In 4386 l. I demand how many Groats? To resolve this Question, 1 reduce the given number of Pounds into Shillings, and they are 87720 Shillings, now I confider that in a Shilling are 3 Groats, therefore I multiply the Shillings by 3, and it produceth 263160 Groats. See the Work.

4286 pownds

87720 (billings

Facit 263160 groats

This Question might have been otherwise resolved thus, viz. confidering that in a pound (or 20 shillings) there are 3 times 20 Groats, which make 60, by which I multiply the number of pounds given, and it produceth the same Effect at one Operation, as followeth.

| 386 60 | pounds groats in | 20 3. | . 2 0 |
|-----------|---------------------|-------|--------------|
| | - | | |

· Facit 263160 groats in 4386 l.

Quest. 7. In 43758 three-pences, I defire to know

how many pounds?

To refolve this (and many such like) Questions; First, I divide my given number of 3 pences by 4, because 4 three-pences are in a shilling, and the quotient is 10939 shillings, and there remainest 2 after Division is ended, which is 2 three pences (by the 8th Rule of this Chapter) which are equal in value to 6 d. then I divide 10939 shillings by 20, and the quote giveth 546 l. and 19 s. remain; so that I conclude in 43758 pieces of three-pence per piece, there are sa6 l. 19 s. 6 d. as by the Work appeareth.

d.

|) 43758 (| 1003/2 | (54 | 5—1 | 9—6 |
|-----------|----------|------|--------|-----|
| 4 | 10 | * | • | |
| 37 36 | 8 - | | , y.s. | , |
| #5 12 | 13 12 | | | • |
| 38. | (19 |) s. | • | |

(2) three-pences or 6 d.

This Question might have been otherwise resolved thus, viz. first multiply the given number of three pences 43758, by three the number of pence in three pence, and the product (viz. 131274) is the number of pence equal to the given number of three-pences, which number of pence may be brought into pounds, by dividing by 12 and by 20, and the quotient you will find to be equal to the former work, viz. 546 1. 15's. 6 d.

43758 20 (546-(1093|9 112 108 13 12 114 re. (19) s.

Remains (6) pence

108

Or thus, divide the given number of 3 pences by the number of 3 pences in a pound or 20 (hillings, (which you will find to be 80, if you multiply 20 s. by 4, the number of three-pences in a (hilling) and you will find the quote to be 546 l. as before, and a remainder of 78 three-pences, and if you divide those 78 three-pences by 4 (because there are 4 three-pences in a (hilling) you will find the quote to be 10 s. and 2 three-pences remain, which are equal to 6 d. which is the same that was before found.

| l. s. d. 8(0) 4375/8 (546—19—6 | 20 |
|-----------------------------------|-----|
| • • • | 4 |
| 40 | 80 |
| 37 | , |
| 32 | |
| 55 | ` |
| 48 | |
| 4) 78 (195- | : |
| A | • |
| ` ` | 2 |
| 38 36 | |
| | |
| (2) three-pences or 6 d. | *** |

Quest. 8. In 4785 l. 19 s. how many pieces of 13 \(\frac{1}{2} d\).

This Question cannot be resolved by Reduction, defeending or ascending, absolutely, (because 13 ½ d. is no even part of a pound) but rather by them both jointly, viz. by Multiplication and Division; for if you bring the number given into half-pence, and divide the half-pence, by the half-pence, in 13½ d. viz 27, the Quotient will be the Answer; for houndstrongth

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brought 4785 l. 12 s. into half-pence, I find it makes 2297112, which I divide by 27, (because there are to many half-pence in $13\frac{1}{2}d$, and the quote gives 85078 pieces of $13\frac{1}{2}d$, and 6 half-pence remain over and above: Observe the Work following.

| l. s. 4785—13 | d. 13 : |
|--|---------------|
| 20 | 2 |
| 95713 Shillings 24 half pence in a shilling | 27 half-pence |

332852 191126

2297112 half-pence in the given number.

27) 2297112 (85078 pieces of 12 1 d.

Rem. (6) half-pence

It would have produced the same Answer if you had reduced your given number into farthings, and divided by the farthings in 13 td. viz. 54, (for always the Dividend and the Divisor must be of one denomination) and then you would have had a remuinder of 12 farthings, which are equal in value to the former remainder of 6 half-pence, as you may prove at your leifure. Dinitized by Google

Quest. 9. In 540 Dollars at 4 s. 4 d. per Dollar, how

many pounds sterling?

First, Bring your given Number of Dollars into pence, and then your pence into pounds according to the former Directions. Thus in 4s. 4d. (viz. a Dollar) you will find 52 pence, by which multiply 540 Dollars, and it produceth 28080 pence, which if you divide by 240 (the pence in one pound) the quotient will give you 117 l. which are equal in value to 540 Dollars, at 4s. 4d. per Dollar. Observe the Operation.

| | • |
|-----------------|---|
| | s. d. |
| 540 | 4-4 |
| 52 | 12 |
| 1080 2700 | 52 pence |
| 24/0) 2808/0 (1 | |
| 24 | |
| 40 24 | |
| 168 | • |

The foregoing Question might have been otherwise wrought, thus, viz. Multiply-(540) your given number of Dollars, by 13 the number of Groats in a Dollar (or 45. 4 d.) and it produceth 7020 groats, which divide by 60 (the groats in 1 pound or 20 shillings) and the quote is 117 l. as before. See the Work.

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| | 540 | s. d. 4-4 3 |
|-----|---------------------------|---------------------|
| 6 0 | 1620 540) 702 0 (1 | 13 17 <i>l</i> . |
| , | 10 | est (etc.) |
| | 42 42 | |
| | · (0) | , |

Quest. 10. In 547386 pieces of 4 d. per piece, I demand how many Pounds, Shillings, and Pence.

First, Bring your given number of four pence halfpenies all into half-pence, which you will do if you multiply by 9 the number of half-pence in $4\frac{1}{2}d$. and the product is 4926474 half-pence, which are brought into Pounds, if you divide them by 24 (the half-pence in a Shilling) and 20 (the Shillings in a Pound) it makes 10263 l. 9 s. 9 d. as by the Work.

| . — | Tr. Of. | 2000 | CE POIA. | | |
|-------|-------------|------------------|-------------|----------------------|----------|
| , , . | 547386 9 | • | | d. 4 | |
| - | | 20 (20526)9 (| 1. 10263 | 9 ha | lf-pence |
| ` | 48 | 2 | , ` | | γ. |
| | 126 120 | 05 | * | | |
| | 64 48 | 12 | Facit | l. 10263- | s. d. |
| | 167 | 6 | , | , | |
| | 234 216 | a (9) | • | | |

Remains (18) balf-pence or 9 d.

Quest. 11. In 4386 l. I demand how many pieces of 6 d. of 4 d. and of 2 d. of each an equal number? that is to say, what number of fix-pences, groats, and two-pences, will make up 4386 l. and the number of each equal?

The way to refolve Questions of this Nature, is to add the several pieces (into which the given Number is to be brought) into one Sum, and to reduce the given number into the same denomination with their sum, and to divide the said given number (so reduced) by the said Sum, and the Quotient will give you the exact number of each piece. And after the same Method will we proceed to resolve the present Question, viz.

(°)

24

So that I conclude by the operation that 87720 fix pences, and 87720 groats, and 87720 two-pences are just as much as (or equal to) 4386 l. or if you admit of 5 s. to be thus divided, it is equal to 5 fix-pences, and 5 two-pences. For if two Right Lines (or two Numbers)- be given, and one of them be divided into as many Parts, or Sigments as you please, the kectangle (or Praud) comprehended under the two whole right lines (or number sieven) shall be equal to all the Restangles (or Produsts) contained under the whole time (or number) and the several Segments (or Parts) into which the other line (or number) is divided. Eucl. 2. 1.

Another Question of the same Nature with the

last may be this following, viz.

Quell. 12. A Merchant is desirous to change 148 l. 18to preces of $13 d. \frac{1}{3}$ of 12 d. of 9 d. of 6 d. and of 4 d.; and he will have of each fort an equal number of pieces. I desire to know the number i

Do as you were taught in the 'aft Question, via, add the several pieces together, and reduce the Sum

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into half-pence, then reduce the Sum to be changed. viz. 148 l. into the same denomination, and divide the greater by the leffer, and in the Quotient you will find the Answer, viz. 798 is the Number of each of the pieces required, and 18 remaineth, which is 18 half-pence by the 8th Rule of this Chapter. See the Work as followeth.

| | ď. |
|----------------------|---|
| 148 | 13 <u>1</u> |
| 240 pence in a 1. | 12 |
| 5920 | 9 6 |
| 296 | 4 |
| 35520 pence in 148 L | Sum 44 |
| 2 | 21 |
| 71040 balf-pence | 89 half-pence (798 pieces of each fort |
| 89) 71040 | (798 pieces of each fort |

Rem. (18) half-pence

The truth of the two foregoing Operations will thus be proved, viz. multiply the Answer by the parts, or pieces into which the given Numbers was reduced, and having added the leveral products together, if their Sum be equal to the given number, the Answer is right, otherwise not.

So the Answer to the 11th Question was 87720,

which is proved as followeth, viz-

Six-pences make 2193 Four-pences make 1462 Two-pences make 731

The total Sun of them 4386 which was the Sum given to be changed.

The Answer to the 12th Question was 798, and 18 half-pence remained after the Work was ended, now the truth of the Work may be proved as the former was, viz.

| | _ | | | l | | |
|--------------|-----------|-----|------|-----------------------|-------------|------------|
| (| Pieces of | 131 | make | 44 - - | 17- | -09 |
| · ' | Picces of | 12 | make | 39- | 18— | -00 |
| 798 | Pieces of | 9 | make | 29`— | 18 | -06 |
| | Pieces of | 6 | make | 19- | 19- | -00 |
| (| Pieces of | 4 | make | 13 | o6 – | -co |
| and 18 balf- | | | | | | |
| | • | | , | | | -5 |

The Total Sum of them 148-00-00

which total fum is equal to the number that was first given to be changed, and therefore the Operation was rightly performed.

Reduction of Troy-weight.

We come now to give the Learner some Examples in Troy-weight, wherein we shall be brief, having given so large a Taste of Reduction in the foregoing Examples of Coyn, and now the Learner must be mindful of the Table of Troy weight delivered in the second Chapter of this Book.

Quest. 13. In 482 l. 07 oz. 13 p.m. 21 gr. How

many Grains?

Multiply by 12, by 20, and by 24, taking in the figures standing in the several denominations, according to the Direction given in the 7th Rule of this Chapter, and you will find the product to be 2780013 Grains, which is the Number required, or Answer to the Question. See the whole Work as followeth.

l. oz. p.w. gr. 482-7-13-21

971 482

5791 ounces 20

115823 penny-weight.

464333 221668

Facit 2780013 grains Quest. 14. In 2780013 grains, I demand how many

pounds, ounces, penny-weights and grains? This is but the foregoing Question inverted, and is

resolved by dividing 24 by 20, and by 12, and the Answer is 482 l. 7 oz. 13 p.m .- 21 gr.

24) 2780013 (11583 3 (5791 (482

| 24 | 10 | 48 |
|-----|-----|---------------|
| 38 | 15 | 99 \ |
| 24 | 14 | 96 |
| 140 | 18 | 31 |
| 120 | 18 | 24 |
| 200 | 2 R | Lem. (7) ound |

192

72

81 Rem.(13) penny-weight

07. p.w. gr.

Facit 482-

Quali. 15. A Merchant sent to a Goldsmith 16 Ingots of Silver, each containing in weight 2 l. 402 and ordered it to be made into Bowls of 2 l. 802. per Bowl, and Tankards of 1 l. 602. per piece, and Salts of 1002. 10 p.m. per Salt, and Spoons of 102. 18 p.m. per Spoon; and of each an equal number, 1 desire to know how many of each fort he must make?

This Question is of the same nature with the 11 and 12 Questions foregoing, and may be answered after the same Method; viz. First, add the weight of the several Vessels (into which the Silver is to be made) into one Sum, and reduce it to one Denomination, and they make 1248 penny-weights, then reduce the weight of the Ingot into the same denomination, viz. penny-weights, (and it makes 560 penny-weights) and multiply them by the number of Ingots, viz. 16, and the product will give you the weight of the 16 lagots, viz. 8960, then divide this product by the weight of the Vessels, viz. 1248, and the quotient giveth you the Answer to the Question, viz. 7, and 224 p.w. remaining over and above.

| mg or | ,. MIIG | above. | |
|-------|----------------------|-------------------------|---|
| • | 2. 12 28 20 | oz. 4 | 1. 02. p.w 2-08-00 1-05-00 0-10-10 |
| | 560 16 | penny-weights Ingots | Sun 5-02-08 12 62 |
| | 3350 560 | | 20 1248 f.w. |
| 1248) | 8960 8736 | (7 Vessels of each | 2 |
| Rem. | (224) | penny-weights | |

The Proof of the Work is as followeth, viz.

l. (Bowls of 2-08-00 per Bowl is 18-08-00 Salts of 0-10-10 per Tank, is 10-06-00. (Spoons of 0-01-18 per Spoon is 01-01-06 224 penny-weight remaining is 00-11-04

Total Sum 37-04-00

So that you fee the Sum of the Weights of each Vessel, together with the Remainder is 37 1. 403. which is equal to the Weight of the 16 Ingots delivered. For if 371. 4 07 be reduced to penny-weights. it makes 8960.

Reduction of Averdupois Weight.

In Reducing Aver dupois Weight, the Learner must have recourse to the Table of Averdupois weight delivered in the Second Chapter foregoing.

Rueft. 16. In 47 C. 1 qr. 20 L. how many Ounces? Multiply by 4, by 28, and by 16, and the last product will be the Answer, viz. 84992 Ounces.

C. qr. l. -1-20

189 quarters 28

1512 **280**

5312 L. 16

21872 5212

Facit 84992 ounces

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Quest. 17. In 84992 Ounces, I demand how many

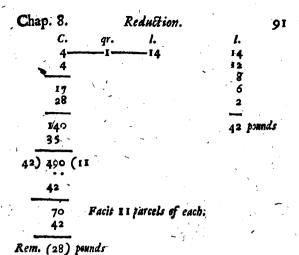
C. qrs. 1. oz.

This is the foregoing Question inverted, and will be resolved if you divide by 16, by 28, and by 4, and the Answer is 47 C. 1 qr. 20 L. equal to the given Numbers in the foregoing Question.

Quest. 18. A Chapman buyeth of a Grocer 4 C. 1 qr. 14 l. of Pepper, and ordered it to be made up into Parcels of 14 l. of 12 l. of 8 l. of 6 l. and of 2 l. and of each parcel an equal number, now I would know the number of each parcel.

, This Example is of the same nature with the 11, and 12, and 15 Questions foregoing, and after the same manner is resolved. See the Operation as fol-

loweth.



Reduction of Liquid Measure.

Quest. 19. In 45 Tun of Wine how many gallons?
Multiply by 4, and by 63, the product is 11340
Gallons for the Answer.

Facit 11340 gallons

Queft. 20. In 43 Rundlets of Wine, each containing

18 Gallons, I demand how many Hogsheads?

First, Find how many Gallons is in the 34 Rundlets, which you may do if you multiply 34 by 18, the content of a Rundlet, and the product is 612 Gallons, which

92 Reduction. Chap. 8. which you may reduce into Hogsheads if you divide them by 63, and the Quote will be 9 Hogsheads, and 45 Gallons. See the Work.

Rem. (45) gallons
Facit 9 bbds 45 gallous.

Saeff. 21. In 12 Tuns how many Rundlets of 14

Gallons per Rundlet?

Reduce your Tuns into Gallons, and divide them by 14, the Gallons in a Rundlet, and the Quotient (216) is your Answer. See the Work following.

4) 3024 (216

22 14: 84

84 facit 216 rundl.

(•) Digitized by Google Reduction

Reduction of Long Measure.

Quest. 22. I demand how many Furlongs, Poles. Inches and Barley-Corns will reach from London to Tork, it being accounted 151 miles?

151 miles
8 furlongs in a mile
1208 furlongs
40 poles in a furbong
48320 poles
11 balf-yards
48320
48320
531520 balf-yards
18 inches in balf a yard
4252160
531520
9567360 inches
3 barly-corns in an inch

Facit 28702080 barly-corns in 151 miles

Ones. 23. The Circumference of the Earth (as all other Circles are) is divided into 360 degrees, and each degree into 60 minutes, which (upon the Superficies of the Earth) are equal to 60 miles; now I demand how many miles, furlongs, perches, yards, feer, and Barly corns will reach round the Globe of the Earth?

360 degrees 60 minutes or miles in a degree

21600 miles about the Earth 8 furlongs in a mile

172800 furlongs about the Earth
40 perches in a furlong

6912000 poles or perches about the Earth
11 half yards in a perch

6912000 6912000

2) 76032000 half yards about the Earth

(38016000 yards, viz. the half yards
2 divided by 2.

114048000 feet about the Earth

2280960**00** 114048000

1368576000 inches about the Earth
2 barly-corns in an inch

Facit 4105728000 barly-corns

And so many will reach round the World, the whole being 21600 miles; so that if any person were to go round, and go 15 miles every day, he would go the whole circumference in 1440 days, which is 3 years, 11 months, and 15 days.

Reduction

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Reduction of Time.

Queft. 24. In-28 Years, 24 Weeks, 4 Days, 16 Hours, 30 Minutes, how many Minutes?

41462

248752 hours

14925150 minutes

Note, That in resolving the last Question after the Method expressed, there is lost in every Year 30. Hours, For the Year consistent of 365 Days and 6 Hours, but by multiplying the Years by 52 Weeks, which is but 364 Days, you lose I Day and 6 Hours every Year; wherefore to find an exact Answer, bring the odd Weeks, Days, and Hours, into Hours, and then multiply the Years by the number of Hours in a Year, viz. 8766, and to the Product add the Hours contained in the odd time, and you have the exact time of Hours, which bring into Minutes as before. See the last Question thus resolved.

| • | | weeks | aays nou |
|--------------|-----------------|-------|----------|
| | * | 24 | -4-10 |
| - | | 7 | |
| | days hou. | 172 | |
| 28 | 365-6 | 24 | |
| 8766 | 24 | - | • |
| - | | 694 | |
| 172 | 1466 | 345 | |
| 172 | 730 | 4144 | houre |
| 197 228 | 8766 hours in a | year | WORL'S. |
| 240402 hours | | | |

14975520 minetes in 28 years and 4144 hours.

So you see that according to the method first used to resolve this Question, the Hours contained in the given time are 248752, but according to the last, best, or true Method, they are 249592, which exceeds the

former by 840 hours.

60

But for most occasions it will be sufficient to multiply the given years by 355, and to the product add the days in the odd time, if there be any, and then there will be only a loss of 6 hours in every year, which may be supplied by taking a fourth part of the given years, and adding it to the contained days, and you have your desire.

Quest. 25. In 438657540 minutes, how many years? Facit 834 years, 4 days, 19 hours.

| هٔ اه) 438 | 657540 | 87 66 | | years (834— |
|------------|----------------------|--------------|--------------|-------------------|
| 42 | | 17012 | 8 , | |
| - 18 | - | 298 262 | 315 | , . |
| | 6 | 3: | 5179 5064 | |
| | 57 54 35 30 | 24) | 96 | (4 days) hwrs |
| | 54 54 | | | |

Quest. 26. I defire to know how many hours and minutes it is fince the Birth of our Saviour Jesus Christ to this present Year, being accounted took Years.

to this present Year, being accounted 1700 Years?
This Question is of the same nature with the 24th foregoing, and after the same manner is resolved, vize Multiply the given number of Years by 8766, the product is 14902200 hours, and that by 60, and the product is 894122000 minutes. See the Work.

1700 years 8766 hours in a year

(o)

10200 10200 11900

14902200 hours in 1700 years.

854132300 mm. in 1700 years

Not

Note that as Multiplication and Division do interchangeably prove each other, so Reduction descending and ascending, prove each other, by inverting the Question, as the 13 and 14, and likewise the 16 and 17 Questions foregoing, by Inversion, do interchangeably prove each other; the like may be performed for the proof of any Question in Reduction whatsoever.

Thus far have we discoursed concerning single Arithmetick, whose Nature and Parts are defined in the second, eighth, ninth, and tenth Definitions of the third Chapter of this Book, for although Reduction is not reckoned or defined among the parts of single Arithmetick, yet considered abstractly, it is the proper effect of Multiplication and Division; and as for the extraction of Roots (which ought to be handled in the next place as parts of single Arithmetick) we shall omit it in this place, and refer the Learner to Mr. Cockers Decimal Arithmetick, which is (with great care and pains) now published, together with his Logarithmetical Arithmetick, showing the Genesis or Fabrick of the Logarithms, and their general uses in Arithmetick, Gr. As also his Algebraical Arithmetick, containing the Doctrine of composing and resolving an Equation, with all other Rules necessary for the understanding of that Mysterious Art, Gr.

CHAP. IX.

Of Comparative Arithmetick; viz. The Relation of Numbers one to another.

1. Comparative Arithmetick is that which is wrought by Numbers, as they are confidered to have relation one to another, and this confists either in Quantity, or in hib. 1. cap. 21. Quality.

2. Relation of Numbers in quantity. is the reference or respect that the Numbers themselves have one to another, where the Vide Wing. A-Terms or Numbers propounded are al- rith. cap. 24. ways two, the first called the Antecedent, and the other the Consequent.

2. The relation of Numbers and Quantity confifts in the differences, or in the rate or reason that is found , betwixt the Terms propounded, the difference of two

Numbers being the remainder found by Subtraction, but the rate or reason. Alfled, Mathebetwixt two numbers is the quotient mat. lib. 2. cap. of the Antecedent divided by the Con- 11, & 12. sequent. So 21 and 7 being given, the

difference betwixt them will be found to be 14, but the rate or reason that is betwixt 21 and 7 will be found to be triple reason, for 21 divided by 7 quotes 2. the reason or rate.

4. The relation of Numbers is Quality, (otherwise called Proportion) is the reference or respect that the reason of Numbers have one unto another; therefore the Terms given, ought to be more than two. Now this proportion or Alsted. Mathereason between Numbers relating one mat. lib.2. cap. to another, is either Arithmetical, or Geometrical.

5. Arithmetical Proportion (by some called Progreffion) is when divers Numbers differ one from another by equal Reason, that is, have equal differences.

So this rank of Numbers 3, 5, 7, 9, 11, 13, 15, 17, differ by equal Reason; viz. by 2, as you may prove.
6. In a rank of Numbers that differ by Arithmeti-

cal Proportion, the fum of the first and last Term being multiplied by half the number of Terms, the product is the total fum of all the Terms.

Or if you multiply the number of the Terms by the half fum of the first and last Terms, the product there-

of will be the total fum of all the Terms.

So in the former Progression given, 3 and 17 is 20, which multiplied by 4 (viz. half the number of Terms)

the product gives 80, the sum of all the Terms; or multiply 8 (the Number of Terms) by 10 (half the sum of the first and last Terms) the product gives 80 as before.

So also 21, 18, 15, 12, 9, 6, 3, being given, the sum of all the Terms will be found to be 84; for here the number of Terms is 7, and the sum of the first and last (viz. 21 and 3) is 24, half whereof (viz. 12) multiplied by 7 produceth 84, the sum of the Terms sought.

7. Three Numbers that differ by Arithmetical Proportion, the double of the mean (or middle number)

is equal to the fum of the Extreams.

So 9, 12, and 15 being given, the double of the mean 12 (viz. 24) is equal to the fum of the Extreams o and 14.

8. Four Numbers that differ by Arithmetical Proportion (either continued or interrupted) the sum of the two Means is equal to the sum of the two Extreams.

Vide Wing. Afum of 12 and 18 will be equal to the
fum of 9 and 21, viz. 30; also 6, 8,
14, 16 being given, the sum of 8 and

14 is equal to the fum of 6 and 16, viz. 22, &c.
9. Geometrical Proportion (by fome called Geome-

trical Progression) is when divers numbers differ ac-

cording to like Reason.

So 1, 2, 4, 8, 16, 32, 64. Gc. differ by double Reason, and 3, 9, 27, 81, 243, 729, differ by triple Reason, 4, 16, 64, 256, Gc. differ by quadruple

Reason, Gr.

ro. In any numbers that increase by Geometrical Proportion, if you multiply the last Term by the Quotient of any one of the Terms divided by another of the Terms, which being less is next unto it, and having deducted, or subtracted, the first Term out of that product, divide the remainder by a number that is an Unit less than the said Quotient, the last quote will give the sum of all the Terms.

So, 1, 2, 4, 8, 16, 32, 64, being given, first I take one of the Terms, viz. 8, and divide it by the Term which is less and next to it, (viz. by 4) and the Quotient is 2, by which I multiply the last Term 64, and the product is 128, from whence I subtract the first Term, (viz. 1) the remainder is 127, which divided by the Quotient 2 made less by I (viz. 1) the quote is 127, for the sum of all the given Terms. 25 by the Work in the Margent.

of all the given Terms, as by the Work in the Margent.
So if 4, 16, 64, 256, 1024 were given, the sum of all the Terms will be found to be 1354. For first, I divide 64, one of the Terms, by his next lesser Term, 16) 64 (4 and the Quotient is 4, by which I multiply the last Term 1024, and it multiply the last Term 1024, and it produceth 4096; from whence I subtract the first Term 4, and the remainder is 4092, which I divide by the quote less 1 (viz 3) and the quote is 1264, for the total sum of all the Terms, 'as per Margent.

So likewise if 2, 6, 18, 54, 162, 486 were given, the sum or total of all the Terms will be found to be 728. See the Work.

115 Three Geometrical Proportionals given, the Square of the Mean is equal to the Rectangle, or Product of the Extreams,

So 8, 16, 32, being given, the Square of the Mean, viz 16 is 256, which is equal to the product of the Extreams 8 and 32, for 8 times 32 is equal to 256.

12. Of 4 Geometrical Proportional numbers given, the product of the two Means is equal to the product of the two Extreams.

So 8, 16, 32, 64, being given, I say that the product of the two Means, viz. 16 times 32, which is 512, is equal to 8 times 64, the product of the Extreams.

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2) 1456 (7.28

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Also if 3, 9, 21, 63, were given (which are intersupted) I say 9 times 21 is equal to 3 times 63, which

is equal to 189.

From hence arifeth that precious Gem in Arithmetick, which for the Excellency thereof is called the Golden Rule, or Rule of Three.

CHAP. X.

The Single Rule of Three Direct.

1. HE Rule of Three (not undefervedly call'd the Golden Rule) is, that by which we find out a fourth number, in proportion unto three given Numbers, so as this fourth Number sought may bear the same Rate, Reason, or Proportion to the third (given) number, as this second doth to the first, from whence it is also called the Rule of Proportion.

2. Four Numbers are said to be Proportional, when the first containeth or is contained by the second, as often as the third containeth or is contained by the fourth. Vide Wingate's Arith Chap. 8. Selli 4.

3, 6, 9, 18, for as often as the first Number is contained in the second, so often is the third contained in the fourth, viz. twice. Also 9, 3, 15, 5, are said to be proportional, for as often as the first Number contained the second, so often the third Number contained the fourth; viz. 3 times.

3. The Rule of Three is either simple or composed.

4. The simple (or single) Rule of Three, consistent of 4 Numbers; that is to say, it hath 3 Numbers given to find out a sourth; and this is either Direct, or Inverse. Vide Alsted. Math. lib. 2. cap. 13.

verse. Vide Alsted. Math. lib. 2. cap. 13.

5. The single Rule of Three Direct, is when the proportion of the first Term is to the second, as the third is to the sourch; or when it is required that the Number sought

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fought (viz.) the fourth Number must have the same proportion to the fecond, as the third hath to the first.

6. In the Rule of Three, the greatest difficulty is (after the Question is propounded) to discover the order of the 3. Terms, viz. which is the first, which is the second, and which the third, which that you may understand, observe, That (of the three given numbers) two are always of one kind, and the other is of the fame kind with the proportional number that is fought; as in this Quellion, viz. If 4 yards of Cloth coft 12 shillings, what will 6 yards cost at that rate. Here the two numbers of one kind are 4 and 6, viz. they both fignifie for many yards; and 12 hillings is the fame kind with the number fought, for the price of 6 yards is fought.

Again, observe, that of the 3 given numbers, those two that are of the fame kind, one of them mult be the first and the other the third, and that which is of the same kind with the number sought, must be the second number in the Rule of Three; and that you may know which of the faid numbers to make your first, and which your third, know this, that to one of those two numbers there is always affixed a demand, and that number upon which the demand lieth must always be . reckoned the third number. As in the forementioned Question, the demand is affixed to the number 6, for it is demanded what 6 yards will cost? and therefore 6. must be the third number, and 4 (which is of the same denomination (or kind) with it) must be the first, and consequently the number 12 must be the second, and then the numbers being placed in the forementioned order, will stand as followeth, viz.

yards

7. In the Rule of Three Direct (having placed the numbers, as is before directed) the next thing to be done will be to find out the fourth number in proportion, which (that you may do), multiply the second number

by the third, and divide the product thereof by the first, (or which is all one) multiply the third term (or number) by the second, and divide the product thereof by the first, and the Quotient thence arising is the 4th number in a direct proportion, and is the number fought, or Answer to the question, and is of the same denomination that the second number is of. As thus, let the same Question be again repeated, viz. If 4 yards of Cloth cost 12 Shillings, what will 6 yards cost?

Having placed my numbers according to the fixth Rule (of this Chapter) foregoing, I multiply (the fecond number) 12 by (the third number) 6, and the product is 72, which product I divide by (the first number) 4, and the quotient thence arising is 18, which is the fourth proportional or number sought, wiz. 18 shillings, (because the second number is shillings) which is the price of the 6 yards, as was required by the que-

ftion. See the Work following:

Quest. 2. Another Question may be this, viz. If 7 C. of Pepper cost 21 l. how much will 16 C. cost at

that rate?

To resolve which question, I consider that (according to the 6th Rule of this Chapter) the terms or numbers ought to be placed thus, viz. the Demand lying upon 16 C. it must be the third number, and that of the same kind with it soust be the first, viz. 7 C. and 21 l. (being of the same kind with the number sought) must be the second number in this question; then I proceed according

according to this 7th Rule, and multiply the second number or the third, viz. 21 by 16, and the product is 336, which I divide by the first number 7, and the quotient is 48 l. which is the value of 16 C. of Pepper at the rate of 21 l. for 7 C. See the Work following.

8. If when you have divided the product; of the &-. cond and third numbers by the first, any thing remains after Division is ended, such remainder may be medtiplied by the parts of the next inferiour Denomination, that are equal to an Unit (or Integer) of the fecond number in the Question, and the product thereof divide by the first number in the Question, and the Quotient is of the same Denomination with the parts. by which you multiplied the remainder, and is put of the fourth number which is fought. And furthermore, if any thing remain, after this last Division is ended. multiply it by the parts of the next inferiour denomination equal to an Unit of the last Quotient, and divide the Product by the same Divisor, (viz. the fiest number in the Question) and the quote is still of the same denomination with your multiplier; follow this. method until you have reduced your Remainder into the lowest Denomination, &c. An Example or two

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will make the Rule very plain, which may be this following.

Queft. 3. If 13 yards of Velvet (or any other thing) cost 21 L. what will 27 yards of the same cost at that

rate ?

Having ordered and wrought my numbers according to the 6 and 7 Rules of this Chapter, I find the Quotient to be 43 l. and there is a remainder of 8, fo that I conclude the price of 27 yards to be more than 43 l. and to the intent that I may know how much more, I work according to the foregoing Rule, viz. I multiply the faid Remainder 8 by 20 s. (because the second number in the Question was Pounds) and the product is 160, which divided by the first and the product is 160, which divided by the first number, viz. 13, it quotes 12, which are 12 shillings, and there is yet a remainder of 4, which I multiply by 12 pence, (because the last quotient was shillings) and the product is 48, which I divide by 13 (the first number) and the quotient is 3d. and yet there remaineth 9, which I multiply by 4 Farthings, and the product is 36, which divided by 13 again, it quotes 2 Farthings, and there is yet a remainder of 10, which because it cometh not to the value of a Farthing) may be regarded or rather fat. (After the Farthing) may be neglected, or rather set (after the 2 Farthings) over the divisor, with a Line between them, and then (by the 21 and 22 Definitions of the first Chapter of this Book) it will be 19 of a Farthing; so that I conclude, that if 13 yards of Velvet cost 21 l. 27 yards of the same will cost 43 l. 12 s. 03 d. 219 grs, which Fraction is 10 thirteenths of a Farthing. See the Operation as followeth.

```
of Three Direct.
Chap. 10.2
                     147
                     42
                 12) 569 (40 l
             Remains (8)
             Multiply"
                       20
                   3] 160 (1254)
             Remains (4)
             Multiply
                 13) 48 (3
             Remains (9)
             Multiply
                  13) 36 (218
             Remains (10) Facit 43-12-3-213
   Quest. 4. Another Example may be this following.
 viz. If 141. of Tobacco cost 27 J. what will 4781. cost
```

at that rate? Work according to the last Rule, and you will find it to amount to 921 s. 10d. 172 grs. and by the 5th.

. d. grs.

107

Rule of the 8th Chapter, 9215. may be reduced to 46l.

1.s. So that then the whole worth or value of the 478l. will be 46l.

1.s. 10d. $17\frac{1}{4}qrs$. the whole Work followeth.

Remains (4) Multiply 4

14) 16 (174 qr.

Remains (2) · . l. s. d. q

Facit 45-1-10-1-1

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9. In the Rule of Three it many times happeneth, that although the first and third numbers be Homogeneal (that is, of one kind) as both Money, Weight, Measure, Go. yet they may not be of one denomination, or perhaps they may both consist of many denominations, in which case you are to reduce both numbers to one denomination; and likewise your second number (if it consistent (at any time) of divers denominations) must be reduced to the least name mentioned, or lower if you please, which being done, multiply the second and third together, and divide by the first, as is directed in the 7th Rule of this Chapter.

And note that always the Answer to the Question is in the same denomination that your second number is

of, or is reduced to, as was hinted before.

Quest. 5. If 15 Ounces of Silver be worth 3 l. 15 s.

what are 86 Ounces worth at that rate?

In this Question the numbers being ordered according to the 6th Rule of this Chapter, the first and third numbers are ounces, and the second number is of divers denominations, viz. 31. 15 s. which must be reduced to stillings, and the shillings multiplied by the third number, and the product divided by the first, gives you the answer in shillings, viz. 430 shillings, which are reduced to 21 l. 10 s. See the Work.

TTO:

In refolving the last Question, the Work would have been the same, if you had reduced your second number into pence, for then the Answer would have been \$100 pence, equal to 21 h. 10 s. or if you had reduced the fecond number into farthings, the Quotient or Answer would have been 20640 farthings equal to the fame. as you may prove at your leifure.

Quest. 6. If 8 1. of Pepper cost 4 s. 8 d. what will

7 C. 3 grs. 14 l. coft ?

In this Question the first number is 81. and the third is 7 C. 3 qrs. 14 l. which must be reduced to the same denomination with the first, viz. into pounds, and the second number must be reduced into pence; then multiply and divide according to the 7th Rule foregoing, and you will find the Answer to be 6174 pence. which is reduced into 25 l. 14 s. 6 d.

C. qrs 1. -8 what will 7-3-14 coft? If 8 coft 4-

> 12 46

882 46 second numbe 5292 4410 20) 8) 49392 (6174 (514 (25-14.

| | • • | • • |
|-------|--------|----------------------|
| 48 | 60 | 4 |
| 13 | 17 | 11. |
| 8 | 12 | 10 |
| 59 | • 54 - | (14) 50 |
| _56_ | . 49 | , |
| 32 | . (6) | 7. |
| 32 | | |
| (0) | E an | ار کار است می |
| . (6) | Faci | t 25 -1 4 |

Quest. 7. If 3 C. 1 qr. 14 L of Raisins cost 9 L. 9 s. what will 6 C. 3 qrs. 20 L of the same cost?

Here the first and third numbers each confist of divers denominations, but must be brought both into one denomination, &c. as you see in the Operation which followeth; the Answer is 288 s, which is reď١

| C. qr. 1. | l. s. | what will 6 | qrs: 1. —3—20 cost?: |
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| 28 | 189 | 27 28 | |
| 108 | | 216 56 | V - 1 - 1 |
| 378 pounds | | 77 ⁶ | pounds Second number |
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| | 27 | 776 | 2 0) 1. s. (38 8 (19—8 |
| • | 3/ | • | (3010 (19—8 |
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| • • | | (0) | |

Quest. 8. If in 4 weeks I spend 13. 4 d. how long will 52 1. 6 s. last me at that rate?

Answer, 2238 days equal to 6 years, 48 days. the Work.

| 12 | 7 | 20 | • |
|-----------|---------|------------------------|------------------------------------|
| 30 | 28 days | 1066 12 | |
| 160 pence | | 2132 1066 | |
| ٠,٠ | | 12792 28 | pence second number |
| | | 102336 25584 | |
| | , , | •••• | - 365) 5 (2238 (6 years 2190 |
| • ' | | 32 —— R 38 32 | em. (48) days |
| | • | 6 I 48 | ye. davs Facit 6—48-35 |
| | · ' | 137 | |

Quest. 9. Suppose the Yearly Rent of a House, a Yearly Pension, or Wages, be 73 l. I desire to know how much it is per day?

Remains (96)

Here you are to bring the year into days, and fay, if 265 days require 73 l. what will one day require?

Now when you come to multiply 73 by 1, the product is the same, for I neither multiplieth nor divideth, and 73 cannot be divided by 365, because the

Divifor is bigger than the Dividend, wherefore bring the 73 l into shillings, and they make 1460, which divide by the first number 365, and the quote is 4 shillings for the Answer, as you see in the Work.

Quest. 10. A Merchant bought 14 pieces of Broad-Cloth, each piece containing 28 yards, for which he gave after the rate of 13 s. $6\frac{1}{3}$ d. per yard, now I defire to know how much he gave for the 14 pieces at that rate?

First, Find out how many yards are in the 14 pieces, which you will do if you multiply the 14 pieces by 28 (the number of yards in a piece) and it makes 302; then say, If 1 yard cost 13 s. 6 s. d. what will 302 yards cost? Work as followeth, and the Answer you will find to be 127400 half-pence, which reduced make 265 l. 8 s. 4 d. For after you have multiplied your second and third Numbers together, the product is 127400, which (according to the seventh Rule) should be divided by the first number, but the first number is 1, which neither multiplieth nor divideth, and therefore the Quotient or fourth number is the same with the product of the second and third, which is in-half-pence, because the second number was so reduced. See the Work as followeth.

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| • | 392 gards in the 14 pieces. |
| yd s. d. If 1 coft 13—6½ who | yds it will 392 cost? 323 the second number |
| 32 13 | 1960 784 3176 210 1 8 d. |
| | 4) 127400 (42018 (265-8-4 |

half-pence 325

Bacit 2651. 8s. 4d. Rem. (8) ; pence, or 4 d.

Quest, 11. A Draper bought 420 rds of broad Coth, and gave for it after their rate of 14 setted 4 per Ellenglish, now E demand how much the paid for the whole at that rate ?

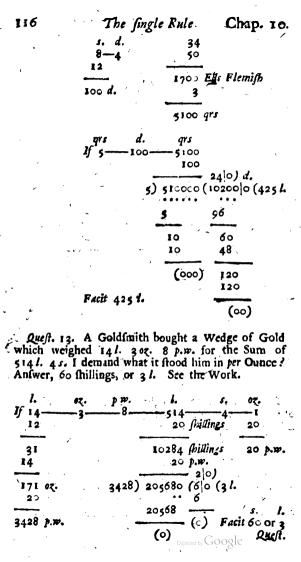
Bring your Ell into quarters, and your given, yards into quarters, the Ell is 5 quarters, and in 420 yards are 1680 quarters, then say, If 5 quarters cost 14 s. 10 3 d. (or 715 farthings) what will 1680 quarters cost? Facit 2501. 5 s. 0 d. See the Operation.

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|--------|-----------|----------|-------------|--------------------|--------|
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Quest. 12. A Draper bought of a Merchant 50 pieces of Kerseys, each piece containing 34 Ells Flemish (the Ell Flemish being 3 quarters of a yard) to pay after the rate of 8 s. 4 d. per Ell English, I demand how

much the 50 pieces cost him at that rate?

First, find how many Ells Flemish are in the 50 picces by multiplying 30 by 34, the product is 1700, which bring into quarters by 3, it makes 5100 quarters, then proceed, as in the last Question, and the Answer you will find to be 102000 pence, or 425 % Behold the Operation, as followeth.



Quest. 14. A Grocer bought 4 hhds of Sugar, each weighing neat 6 C. 2 qrs 14 l. which cost him 2 l. 8 s. 6 d. per C. I demand the value of the 4 hhds at that rate?

First, Find the weight of the 4 bhds, which you may do by reducing the weight of one of them into pounds, and multiply them by 4 (the number of bhds) and they make 2968 l. then say, If 1 C. or 112 l. cost 2 l. 8 s. 6 d. what will 2968 l. cost? Facis 64 l. 5 s. 3 d. As by the Operation.

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| | | | - | 4. | ` |
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| <i>l. l.</i> | s. d. | <i>t.</i> | 21 | | |
| 112-2- | -8c6- | 2968 | 53 | | |
| 20 | _ | 582 | | · · | |
| | | | 74 | 2 l. in | t bbd |
| 48 | | 5936 | | 4 hozshe | ads: |
| 12 | , _ | 23744 14840 | 206 | 8 l. in . | bhla |
| 102 | | -4040 | 12) | 2 (0) | 1 0003; |
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| 40 | ; -7- 7 | 77-7570 | | (10-1) | (- T |
| 582 | | 112 | 12. | 12 | |
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| | · · · | • • • • • | • • • • | • • | |
| | . · | 6c7 560 | 12. 34 24 102 | 8 8 | |
| | | 607 | 34 24 | 8 8 | spillings. |
| | • | 607 560 473 448 | 34 24 102 96 | 8 8 | |
| | | 6c7 560 | 12. 34 24 102 96 | 8 8 | |

The single Rule Chap. 10.

118 Queft. 15. A Draper bought of a Merchant 8 packs of Cloth, each pack containing 4 parcels, and each parcel 10 pieces, and in each pieces 26 yards, and gave after the rate of 41. 16 s. for 6 yards, now I defire to know how much he gave for the whole? Answer, 6656 1.

First, rind out how many yards there were in the 8 packs, as by the following Work you will find there 16 s. what

| 320 yards ; will 8320 y | ards cost | , Gr. | •. • | ·: . | packs |
|---------------------------------------|-----------------|---|-------------|-----------|------------|
| | | - | | 4 | |
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| 66 5 6 L | (0) | - | | | • |

By

By this time the Cearner is (I suppose) well exercifed in the Practick and Theorick of the Rule of Three Direct, but at his leifure he may look over the following Questions, whose Answers are given, but the operation purposely omitted as a Touchstone for the Learner, thereby to try his Ability in what hath been delivered in the former Rules.

Quest. 16. If 24 l. of Raisins cost 6 s. 6 d. what will 18 Frails cost, each weighing Neat 2 grs 18 l. Auswer,

24 l. 17 s. 2 d.

Quest. 17. If an Quace of Silver be worth 5 shillings, what is the price of 14 Ingots, each Ingot weigh-

ing 7 l. 50%. 10 p.w. Answer, 312 l. 5 s.

Quest. 18. If a piece of Cloth cost 10 1. 16 s. 8 d. I demand how many Ells English there are in the Samo, when the Ell at that rate is worth 8's. 4 d.? Answer, 26 Ells English.

Quest. 19. A Factor bought 84 pieces of Stuffs. which cost him in all 537 l. 12 s. at 5 s. 4 d. per yd. I demand how many Yards there were in all, and how many Ells English were contained in a piece of the fame? Answer, 2016 Yards in all, and 191 Ells English per piece.

27 Quest. 20. A Draper bought 212 Yards of Broadcloth, which cost him in all 254 1. 10 s. for 86 yards, of which he gave after the rate of 21 s. 4 d. per yarding I demand how many he gave per yard for the remain-

der ? Answer, 20 s. 10 d. - 12 per yard.

Quest. 2:1. A Factor bought a certain quantity of Serge and Shalloon, which together coft him 226 1. 14 s. to d. the quantity of Serge he bought was 48 yards. at a se 4 de par yard, and for every two yards of Serge he had s yards of Shalloon, I demand how many yards of Shalloon he had, and how much the Shalloon cost him per yard ? Answer, 120 yards of Shalloon at 11 1. 16 s. 5-E3 d. per yard.

Quest. 22 An Oyl-man bought 3 Tun of Oyl, which cost him 151 l. 14 s. and it so chanced that it leaked out 85 gallons, but he is minded to fell it again, so as that he may be no loser by it. I demand how he

The single Rule Chap. 10 120

must sell it per gallon ? Answer, at 4 s. 627 d. m gallon.

Quell. 23. Bought 6 packs of Cloth, each pack containing 12 Cloths, which at 8 s. 4 d. per Ell Flemift coft 1080 l. I demand how many yards there were in

each Cloth? Answer, 27 yards in each Cloth.

Quest. 21. A Gentleman hath 536 l. per annum, and his Expences are one day with another 18 s. 10 d. 2 grs. I defire to know how much he layeth up at the sears end ? Answer, 191 l. 25. 0 d. 1 gr.

Quest. 24. A Gentleman expendeth daily one day with another 27 s. 10 1 d. and at the years end lay-

eth up 340 l. I demand how much is his Yearly Income? Answer, 848 l. 14 s. 4 1 d.

Quest. 26. If I fell 14 yards for 10 l. 10 s. cod. how many Ells Flemish thall I fell for 283 l. 17 s. 6 d. at that rate ? Answer, 5043 Ells Flemish.

Quest. 27. If 100 l. in 12 Months gain 6 l. Intereft, how much will 75 L gain in the fame time, and

at the same rate? Answer, 41. 10 s. Quest. 28. If 100 l. in 12 Months gain 6 L. Inte-

rest. how much will it gain in 7 Months at that rate? Answer, 3 l. 10 s.

Quest. 29. A certain Usurer put out 75% for 12 Months, and received Principal and Interest 81 1. I demand what rate per Cent. he received Interest ? An-Jwer, 8 l. per Cent.

Quest. 30. A Grocer bought 2 Chests of Sugar, the one weighed neat 17 C. 3 qrs 14 l. at 2 l, 6 s. 8 d. per C. the other weighed neat 18 C. 1 qr 21 l, at 4 d. per l. which he mingleth together, now I defire to know how much a C. weight of this mixture is worth?

Answer, 21. 4 s. 3 d. 25.75 qrs.

Quest. 31. Two Men, viz. A and B. departed both from one place, the one goes East, and the other West, the one travelleth 4 miles a day, the other 5 miles a day, how far are they diftant the 9th day after their

departure? Answer, 81 Miles.

Ouest. 32. A flying every day 40 miles is pursued the 4th day after by B, posting 50 miles a day, now the Question is in how many days, and after how many Chap. 7. Ex.35. miles Pravel will A be overtaken?

Answer, B overtakes him in 12 days, when they have

11. The general Effect of the Rule of Three Direct, is contained in the definition of the fame, that is, to find a fourth Number in proportion confifting of two equal Reasons as bath been fully shewn in all the foregoing Examples.

The second Effect is, by the price or value of one thing to find the price or value of many things of like kind.

The third Effect is, by the price or value of many things to find the price of one, or by the price of many things (the faid price being 1) to find the price of many things of like kind.

The fourth Effect is, by the price or value of many things, to find the price or value of many things of

like kind.

The fifth Effect is, thereby to reduce any Number of Moneys, Weight, or Measure, the one fort into the other, as in the Rules of Reduction contained in the Eighth Chapter foregoing. Examples of its various Effects have been already answered.

12. The Rule of 3 Direct is thus proved, who imaltiply the first Number by the fourth, and note the Product, then multiply the second Number by the third, and Rule of Three if this product is equal to the product

of the first and fourth, then the work is rightly performed, otherwise it is erronious

So the first Question of this Chapter (whose Answer or fourth number we found to be 18 s.) is this proved, viz. the first number is 4, which multiplied by 18 (the fourth) produceth 72. And the second and third numbers are 12 and 6, which multiplied together produce 72, equal to the product of the first and fourth, and therefore I conclude the work to be rightly performed.

Always observing, that if any thing remain after you have divided the product of the second and third numbers by the arst, such remainder in proving the same, must be added to the product of the first and fourth Numbers, whose Sum will be equal to the Product of the second and third, (the second number being of the same denomination with the fourth, and the first of the same denomination with the third.)

J 22

So the fourth Question of this Chapter being again repeated, viz. If 14.6 of Tobacco cost 27 s. what will 478 s. cost at that rate? The Answer (or fourth number) was 46 s. o. s. 10 d. 1 qr. 7 which is thus proved, viz. bring the fourth number into farthings, and it makes 44249, which number into farthings, and it makes 44249, which nultiplied by the first number 14, produceth 619488 (the second which remaineth being added thereto) then (because I reduce my fourth number into farthings,) I reduce my second (viz. 27 s.) into farthings, and they are 1296, which multiplied by the third number 478, their product is 619488 equal to the product of the first and fourth Numbers. Wherefore I conclude the Operation to be true. This is an infallible way to prove the Rule of Whree Direct, and it is deduced from the 12th Sellien of the 9th Chapter of this Book.

Thus much concerning The Single Rule of Three Dired, and I question not but by this time the Learner is sufficiently qualified to resolve any Question pertinent to this Rule, not relying upon Frassions, or Geometrical Magnitudes. Those that are desirous to see the Demonstration of this Rule, let them read the fixth Chapter of (the ingenious) Mr. Kersey's Appendix to Wingate's Arithmetick. Or the fixth Chapter of Mr. Oughtred's (incomparable) Clavia Mathematica: By both which Authors this Rule is largely demonstrated, being grounded upon the 19th Prop. of the 9th, and the 19th Prop. of the 9th of Euclid. Elem.

CHAP. XI.

The Single Rule of Three Inverse.

The Golden Rule, or Rule of 3 Inverse, is when there are 3 Numbers given to find a fourth, in such proportion to the 3 given numbers, so as the 4th proceeds from the second, according to the same Rate, Reason, or Proportion that the sirst proceeds from the third, or the Proportion is.

As the third Number is in proportion to the second, so is the first to the lib. 2. cap. 14.

fourth.

So if the 3 numbers given were 8, 12, and 16, and it were required to find a fourth number in an inverted proportion to these, I say, that as 16 (the third number) is the double of the first Term or number (8) so must 12 (the second number) be the double of the fourth; so will you find the fourth term or number to be 6. And as in the Rule of 3 Dired, you multiply the second and third together, and divide their Product for a fourth proportional number.

2. In the Rule of 3 Inverse, you must multiply the second term by the first (or first term by the second) and divide the Product thereof by the third term, so the quotient will give you the 4th term sought in an Inverted Proportion. The same order being observed in this Rule, as in the Rule of 3 Direct, for placing and disposing of the given numbers, and after your numbers are placed in order, that you may know whether your Question be to be resolved by the Rule Direct or In-

verse, observe the general Rule following.

3. When your Question is stated, and your numbers orderly disposed, consider in the first place whether the fourth term or number sought, ought to be more or less than the second term; which you may easily do: And if it is required to be more, or greater than the second term, then the lesser Extream must be your Divisor; but if it require less, then the biggest Ex-

i **3.** Digitizad & Google tream must be your Divisor (in this Case the first and third numbers are called Extreams in respect of the second) and having found out your Divisor, you may know whether your question belongs to the Rule Divel or Inverse; for if the third term be your Divisor, then it is Inverse; but if the first term be your Divisor, then it is a Direct Rule. As in the following Questions.

Quest. 1. If 8 Labourers can do a certain piece of work in 12 days, in how many days will 16 Labourers do the same? Answer, in 6 days.

Having placed the numbers according to the 6th Rule of the 10th Chapter, I consider that if 8 Men can finish the lab. days lab. Work in 12 days, 16 men will 8-12 do it in leffer (or sewer days, than 12,) therefore the biggest 16) 96 (6 days Extream must be the Divisor. which is 16, and therefore it is the Rule of a Inverse, wherefore I multiply the first and second numbers (o) together, viz. 8 by 12, and their product is 96, which divided by Facit & days. (16, Auotes 6 days for the Answer, and in so many

days will 16 Labourers perform a piece of work, when 8 can do it in 12 days.

Quest. 2. If when the measure (viz. a peck) of Wheat

cost 2 shillings, the penny Loaf weighed (according to the Standard, Statute, or Law of England) 8 Ounces, I demand how much it will weigh when the peck is worth 1 s. 6 d. according to the same rate or proportion ? Answer, 10 ex. 13 p.w. 8 gr.

Having placed and reduced the given numbers according to the 6 and 9 Rules of the 10th Chapter, I confider, that at 1 s. 6 d. per peck; the penny Loaf will weigh more than at 2 s, per peck; for as the price

decreafeth, the weight increafeth, and as the price incresseth, so the weight diminisheth, wherefore because the first term requireth more than the second, the lesser Extream must be the Divisor, 1s. 6d. or 18d. and having finished the work, I find the Answer to be 10 oz. when the peck of Wheat is worth 1 s. 6 d. according to the given rate of 8 ounces, when the peck is worth 2 shillings, the work is plain in the following operation.

| llings, | the work is plain | in the fo |
|---------|---------------------------|---------------------------------------|
| 2 12 | 8 24 | 1 |
| 24 | 32 | 18 |
| • : | 16 02. 18) 192 (10- | p.w. gr |
| ٠. | 18 | i i i i i i i i i i i i i i i i i i i |
| | (12) | |
| | 18) 240 (13 / | .w. |
| | 18 | |
| , , | 54 | |
| - | (6) 24 | |
| | 24 12 | |
| , | 18) 144 (8 gr | |
| . , | (0) | ,*** j |

Quest. 3. How many pieces of Money or Merchandise at 20.5, per piece are to be given or received for 240 pieces, the value or price of every piece being 12 shillings? Answer, 144. For if 125, require 240 pieces, then 20 shillings will require less; therefore the biggest Extream must be the Divisor, which is the third number, Gre. See the Work.

s. pieces s.

If 12—240—20

12

480
240

2[0] 288 0 (144 pieces at 20 s. per piece

8 8

(o)

Quest 4. How many yards of 3 quarters broad are required to double, or be equal

in measure to 30 yards, that are
5 quarters broad? Answer, 50
9 yards: For say, If 5 quarters
wide require 30 yards long,
what sength will three quarters
broad require? Here I consider
that three quarters broad will
tequire more yards than 30, for
the narrower the Cloth is, the

10 30 3
30 3
30 3
30 3
30 3

more in length will go to make equal measure with a broader piece.

Quest. 5. At the Request of a Friend I lent him 200 l. for 12 months, promising to do me the like Courtesse at my Necessity; but when I came to request it of him, he could let me have but 150 l. now I desire to know how long I may keep this Money to make plenary satisfaction for my former kindness to my Friend? Answer, 16 months. I say, If 200 l. require 12 months, what will 150 l. require? 150 l. will require more time than 12 months, therefore the lesser Extream (viz. 150) must be the Divisor, multi-

ply

Chap. II. of Three Inverse. 127

ply and divide, and you will find the fourth inverted Proportional to be 16, and so many months I ought to keep the 150 l. for latinfaction.

Quest. 6. If for 24s, I have 1200 l. weight carried 36 miles, how many miles thall 1800 l. be carried for

the fame Money ! Anfiver, 24 miles.

Quest: 4. If for 24 s. I have 1200 l. carried 36 miles, frow many pound weight shall I have carried 24 miles for the same Money? Answer, 1800 pound weight.

Quest. 8. If 100 Workmen in 12 days finish a piece of work or service, how many Workmen are sufficient to do the same in 2 days? Answer, 400 Workmen.

Quest 9. A Colonel is belieged in a Town in which are 1000 Soldiers, with provision of Victuals only for 3 months, the question is, how many of his Soldiers must be dismiss, that his Victuals may last the remaining Soldiers 6 months? Answer, 500 he must keep, and dismiss as many.

Quest. 7c. If Wine worth 20 1, is sufficient for the Ordinary of 100 Men, when the Tun is sold for 30 1. how many Men will the same 20 pounds worth suffice

when the Tun is worth 24 l. Answer, 125 Men.

Quest. 11. How much Plush is sufficient to line a. Cloak, which hath in it 4 yards of 7 quarters wide, when the Plush is but 3 quarters wide? Answer, by yards of Plush.

Quest. 12. How many yards of Canvas that is Ellwide, will be sufficient to line 20 yards of Say, that is 2 quarters wide? Answer, 12.yards.

Quest. 13. How many yards of Matting that is two foot wide, will cover a Floor that is 24 foot long, and

20 foot broad? Answer, 240 foot.

Quest. 14. A Regiment of Soldiers confishing of 1000, are to have new Coats, and each Coat to contain 2 yards, 2 quarters of Cloth, that is 5 quarters wide, and they are to be lined with Shalloon that is 2 quarters wide, I demand how many yards of Shalloon will line them? Answer, 16666 quarters of yards, or 4166 yards.

Quest.

Quest. 14. A Messenger makes a Journey in 24 days, when the day is 12 hours long, I desire to know in how many days he will go the same when the days is

16 hours long? Answer, in 18 days.

Quest. 16. Borrowed of my Friend 64 l. for 8

months, and he hath occasion another time for to borrow of me for 12 months, I defire to know how much i must lend to make good his former kindness to me? Answer, 42 l. 13 s. 4 d.

4. The general Effect of the Rule of a Inverse is contained in the definition of the same, that is, to find a tourth term in a Reciprocal Proportion, inverted to

the Proportion given.

The second Effect, is by two prices, or values of two several pieces of Money or Merchandize known, to find how many pieces of the one price is to be given for so many of the other. And consequently to reduce and exchange one fort of Money, or Merchandize into another. Or contrariwise to find the price unknown of any piece given to exchange in Reciprocal Proportion.

The third Effect, is, by two differing prices of a measure of Wheat bought or fold, and the weight of the Last of Bread, made answerable to one of the prices of the measure given, to find out the weightof the same Loaf answerable to the other price of the faid measure given. Or contrariwise by the two several weights of the same prized Loaf, and the price of the measure of Wheat answerable to one of those Weights given, to find out the other price of the measure answerable to the other weight of the same Loaf.

The fourth Effect, is, by two lengths, and one breadth of two Rectangular Planes known to find our another breadth unknown. Or by two breadths and one length given, to find out another length unknown in an inverted proportion.

The fifth Effect, is, by double time and a capital fum of money borrowed or lent, to find out another capital fum answerable to one of the given Times

or otherwise, by two capital sums, and a time answer able to one of them given to find out a time answerable to the other capital fum in Reciprocal Reason.

The fixth Effect, is, by two differing weights of Carriage, and the diffance of the places in Miles or in Leagues given, to find another distance in Miles answerable to the same price of payment: Or otherwise by two distances in Miles, and the weight answersble to one of the distances (being carried for a certain price) to find out the weight answerable to the other distance for the same price.

The feventh Effect, is, by double Workmen, and the time answerable to one of the numbers of Workmen given, to find out the time answerable to the other number of Workmen, in the performance of any work or fervice. Or contrariwise, by double time and the workmen answerable to one of those times given, to find but the number of workmen answerable to the other time, in the performance of any work or service.

Also by a double price of Provision, and the number of Men, or other Creatures nourished for a tertain time, answerable to one of the prices of Provision given, to find out another number of Men or other. Greatures answerable to the other price of the provifion for the same time. Or contrariwife by two numbers of Men or other Creatures nourished, and one price of Provision answerable to one of the numbers of Creatures given, to find out the other price of the same Provision answerable to the other number of Creatures, both being supposed to be nourified for the same, G. As in the foregoing Examples is fully declared.

. To prove the Operation of the Rule of a Inverse, multiply the third and fourth terms together, and note their product; and multiply the first and second together, and if their product is equal to the product of third and fourth, then is the work truly wrought, but if it falleth out otherwise, then it is erroneous.

As in the first Question of this Chapter, 16 (the third number) being multiplied by 6 (the f urth number) the product is 96, and the product of 8 (the first number) multiplied by 12 (the second number) is 96, equal to the first product, which proves the work to

be right.

And Note, that if in Division any thing remain, such remainder must be added to the product of the third and fourth terms, and if the Sum be equal to the product of the first and second (the homogeneal terms being of one denomination) the work is right.

CHAP. XII.

The Double Rule of Three Direct.

The have already delivered the Rules of Single Proportion, and we come now to lay down the

Rules of Plural Proportion.

1. Plural Proportion, is when more Operations in the Rule of Three than one, are required before a Solution can be given to the Question propounded. Therefore in Questions that require Plurality in Proportion, there are always given more than a Numbers.

2. When there are given 5 numbers, and a fixth is required in proportion thereunto, then this fixth proportion is faid to be found out by the double Rule of

Three, as in the Question following, viz.

If 100 L in 12 Months gain 6 L. Interest, how much

will 75 L gain in 9 months?

3. Questions in the double Rule of Three may be resolved either by two single Rules of Three, or by one
single Rule of Three, compounded of the five given
Numbers

4. The double Rule of Three is either Direst, or elle

Inverse.
5. The double Rule of Three Direct, is, when unto 5 given numbers, a fixth proportional may be found out by two fingle Rules of Three Direct.

6. The five given Numbers in the double Rule of

Three confift of 2 parts, viz. First, a Supposition, and Secondly, of a Demand; the Supposition is contained in the three first of the five given Numbers, and the Demand lies in the two last; as in the kxample of the second Rule of this Chapter, viz. If 100 L in 12 months gain 6 L Interest, what will 75 L gain in 9 months? Here the Supposition is expressed in 100, 12, and 6; for it is said, if (or suppose) 100 L in 12 months gain 6 L Interest, and the Demand lyeth in 75 and 9; for it is demanded how much 75 L will gain in 9 months?

7. When your Question is stated, the next thing will be to dispose of the given Numbers in due orderand place, as a preparative for Resolution; which that you may do, First, observe which of the given Numbers in the Supposition is of the same Denomination with the Number required, for that must be the fecond number (in the first operation) of the single Rule of 3, and one of the other Numbers in the Supposition (it matters not which) must be the first Number, and that Number in the Demand which is of the same Denomination with the first, must be the third number, which three Numbers being thus placed, will make one perfect Question in the fingle Rule of Three, as in the forementioned Example: First, I consider that the Number required in the Question is the Interest or Gain of 75 1. therefore that number in the Supposition which hath the fame name (viz. 61. which is the Interest or Gain of 100 L) must be the! fecond Number in the first Operation. 100-6-78

and either 100 or 12 (it matters not which) must be the first Number 3 but I will take

100, and then for the third Number, I put that Number in the Demand which hath the same Denomination with 100, which is 75, (for they both signifian pounds principal) and then the Numbers will stand as you see in the Margent.

Refa

But if I had for the first number put the other num-ber in the Supposition, viz. 12, which fignifieth 12 months, then the third number must have been 9, which is that number 12-

Denomination with the first, viz. o months, and then they will fland as in the Margent,

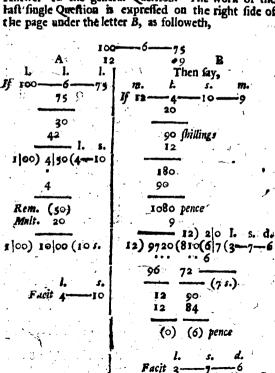
There yet remain two numbers to be disposed of, and those are, one in the Supposition, and another in the Demand; that 100which is of the Supposition I place under the first of the three numbers, and the other which is in the Demand I place under the third number, and then 2 of the terms in the Supposition will stand (one 100 over the other) in the first place. and the a terms in the Demand will stand (one over the other) in the third place, as in the Margent.

8. Having disposed, or ordered the numbers given according to the last Rule, we may proceed to a resolution, and first I work with the three uppermost numbers, which according to the first disposition are 100, 6, and 79, which is as much as to fay, If 100 /. require 61. (Interest) how much will 75 1. require? which by the third Rule of the eleventh Chapter I find to be Direll, and by the 7th and 8th Rules of the noth Chapter, I find the fourth Proportional Number to be 41. 10 s. so that by the foregoing single Question I have discovered how much Interest-75 L will gain in 12 months, the operation whereof followeth on the left hand under the letter A; and having discovered how much 75 l. will gain in 12 months, we may by another question easily discover how much it will gain in 9 months, for this fourth number (thus found) I put in the middle between the two lowest numbers of the five, after they are placed according to the seventh Rule of this Chapter; and then it will be a second

number, in another Question in the Rule of Three. the numbers being 12-4-10-9 the first and third

Sa

numbers being of one Denomination, viz. both months, and may be thus expressed, If 12 months require 4 le 10 s. Interest, what will 9 months require ? And by the third Rule of the 11th Chapter I find it to be the Direst-Rule, and by working according to the directions laid down in the 7, 8, and 9 Rules of the 10th Chapter, I find the fourth Proportional number to the last single Question to be 03 l. 07 s. 06 d. which is the 6th Proportional number to the 5 given numbers, and is the Answer to the general Question. The work of the last single Question is expressed on the right side of the page under the letter B, as followeth,



So that by the foregoing Operation I conclude that if 100 l. in 12 months gain 6 l. Interest, 75 l. will gain 3 l. 75. 6 d. in 9 months after the same rate,

The Answer would have been the same if the s given numbers had been ordered according to the second method, wir. as 100

you see in the Margent.

For first, I say, If 12 months gain 61. what will 9 months gain? This Question I find to be Direst by the 3d Rule of the 11th Chapter, and by the 7th and 8th Rules of the 10th Chapter, I find the south propor-

tional Number to these three to be 41. 10 s.

Thus have I found out what is the Interest of 100 l. for 9 months, and I am now to find the Interest of 75 l. for 9 months at 0 effect which, I make this 4th number (found as before) to be my second number in the next Question, and say, If 100 l. require 4 l. 10 s. what-will 75 l. require? This Question I find (by the said third Rule of the 11th Chapter) to be Direst, and by the said 7th, 8th, and 9th Rules of the 10th Chapter, I find the Answer to be as before, viz. 3 l. 7 s. 6 d.

This Rule hath been sufficiently explained by the sofegoing Example, so that the Learner may be able to resolve the sollowing (or any other) Questions pertinent to the double Rule of 3 Direst, whose Answers are there given, but the Operation purposely omitted to try the Learner's ability in the knowledge of what hath been before delivered.

Queft. 2. A second Example in this Rule may be as followeth, viz. A Carrier receiving 42 shillings for the Carriage of 300 weight 130 miles, I demand how much he ought to receive for the Carriage of 7 C. 3 qrs. 14 l. 40 miles at that rate? Answer, 26 s. 9 d.

Quest. 3. A Regiment of 936 Soldiers eat up 351 quarters of Wheat in 168 days, I demand how many quarters of Wheat 11232 Soldiers will eat in 56 days.

at that rate? Answer, 1404 grs.

Quest. 4. If 40 Acres of Grass be mowed by 8 Men in 7 days, how many Acres shall be mowed by 24 Men in 28 days? Answer, 480 Acres. Google Quest.

Quest. 5. If 48 bushels of Corn (or other Seed) yield 576 bushels in 1 year, how much will 240 bushels yield in 6 years at that rate? That is to say, if there were sowed 240 bushels every one of the 6 years? Answer, 17280 bushels.

Quest. 6. If 40 shillings is the Wages of 8 Men for 5 days, what shall be the Wages of 32 Men for 24

days? Answer, 768 (hillings, or 38 l. 8 s.

Quest. 7. It 14 Horses cat 36 bushels of Provender in 16 days, how many bushels will 20 Horses cat in 24

days? Answer, 120 bushels.
Quest. 8. If 8 Cannons in one day spend 48 barrels of Powder, I demand how many barrels 24 Cannons will spend in 12 days at that rate? Answer, 1728 barrels.

Quest. 9. If in a Family, confishing of 7 persons, there are drunk out 2 Kilderkins of Beer in 12 days. how many Kilderkins will there be drunk out in 8 days by another Family confifting of 14 persons? Answer, 48 Gallons, or 2 Kilderkins and 12 Gallons.

Quest. 10. An Usurer put 75% out to receive Interest for the same, and when it had continued 9 months, he received for Principal and Interest 78 1. 7 s. 6 d. I demand at what rate per Cent. per Annum, he received Interest ? Answer, at 6 l. per Cent. per Annum.

CHAP. XIII.

The double Rule of Three Inverse.

HE double Rule of 3 Inverse, is, when a Question in the double Rule of 3 is resolved by 2 single Rules of 2, and one of those sugle Rules falls out to be Inverse, or requires a fourth number in Proportion

Reciprocal (for both the Questions are never Inverse.)

2. In all Questions of the Double Rule of 3 (as well Inverse as Direct) you are in the disposing of the 5 Digitized by GOOGLE given

given numbers) to observe the 7th Rule of the 12th Chapter, and in resolving of it by two single Rules, observe to make choice of your numbers for the first and second single Questions according to the directions given in the eighth Rule of the same Chapter, as in the Example following, viz.

Quest. 1. If 100 l. Principal in 12 months gain 6 l. Interest, what Principal will gain 3 l. 7 s. 6 d. in 9

months ?

This Question is an Inversion of the first Question of the 12th Chapter, and may serve for a proof thereof.

In order to a Resolution, I dispose of the s given numbers according to the 7th Rule of the last Chapter. and being so disposed, will stand as followeth.

Or thus,

Here observe, that according to the eighth Rule of the twelfth Chapter, the first Question, if you take it from the s numbers (as they are ordered or placed first) will be, If 12 months require 100 l. principal, what will 9 months require to make the same Interest? This (according to the third Rule of the 11th Chapter) is Inverse, and the answer will be found (by the 2d Rule of the 11th Chapter) to be 1331. 6 s. 8 d. the second question then will be, If 6 l. Interest require 133 l. 6 s. 8 d. principal, how much principal will 3 1. 7 s. 6 d. require? This is a direct Rule, and the answer in a direct proportion is 75 l. See the Work.

9) 60 (65,

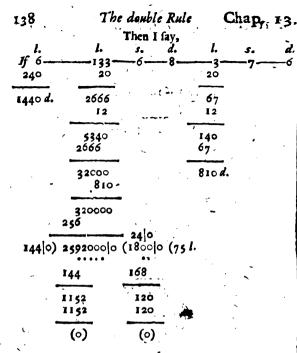
(6)

(°)

9) 72 (8 d. 72

Then,

137



So that by the foregoing Work I find that if 6 l. Interest be gained by 100 l. in 12 months, 3 l. 7 s. 6 d. will be gained by 75 l. in 9 months.

But if the resolution had been sound out by the Numbers as they are ranked in the second place, then the second Question in the single Rule would have been Inverse, and the first Question Direst, and the conclusion the same with the sirst method, viz. 75 L.

Quest. 2. If a Regiment confisting of 936 Soldiers can eat up 351 quarters of Wheat in 168 days, how many Soldiers will eat up 1404 quarters in 56 days at that rate? Answer, 11232 Soldiers.

Quest. 3. If 12 Students in 8 Weeks spend 48 t. I demand how many Students will spend 288 t. in 18 Weeks? Answer, 32 Students. Quest. Quest.

Quest. 4. If 48 l. serve 12 Students 8 Weeks, how many Weeks will 288 l. serve 4 Students? Answer,

144 Weeks.

Quest. 5. If when the bushel of Wheat cost 3 s. 4 d. the penny Loaf weigheth 12 ounces, I demand the weight of the Loaf worth o d. when the bushel cost so s. ? Answer, 26 ounces.

Quest: 6. If 48 Pioneers in 12 days cast a Trench

24 yards long, how many Pioneers will cast a Trench
168 yards long in 16 days? Answer, 252 Pioneers.

Quest. 7. If 12 C. weight being carried 100 miles
cost 51. 12 s. I desire to know how many C. weight
may be carried 150 miles for 12 l. 12 s. at that rate?

Answer, 18 C.

Queff. 8. If when Wine is worth 30 l per Tun, 20 pounds worth is sufficient for the ordinary of 100 Men, how many Men will 4 pounds worth suffice when it is

worth 24 l. per Tun? Answer, 25 Men.
Quest, 9. If 6 Men in 24 days, mow 72 Acres, in how
many days will 2 Men mow 24 Acres, 2 Answer, in 6

days.

Quest. 10. If when the Tun of Wine is worth 30 l. 100 Men will be satisfied with 20 L worth, I desire to know what the Tun is worth when 41 worth will satisfic 25 men at the same rate? Answer, 24 l. per Tun.

CHAP. XIV.

The Rule of Three composed of five Numbers.

HE Rule of Three Composed, is, when Que-flions (wherein there are 5 numbers given to find a 6th in proportion thereunto) are resolved by one fingle Rule of 3 composed of the 5 given numbers,
2. When Questions may be performed by the don-

ble Rule of 3 Direct, and it is required to resolve them by the Rule of 3 composed, (first order or rank your Numbers according to the 7th Rule of the 12th Chapter, then) Digitized by Google

The Rule is,

Multiply the Terms or (Numbers) that stand one over the other, in the first place, the one by the other, and make their product the first Term in the Rule of Three Direct, then multiply the Terms that stand one over the other, in the third place, and place their product for the third term in the Rule of Three Direct, and put the middle term of the three uppermost for a second term; then having sound a sourth proportional, direct to these three, this sourth proportional so sound, shall be the Answer required.

So the first Question of the 12th Chapter being proposed, viz. If 100 l. in 12 months gain 6 l. Interest, what will 75 l. gain in 9 months? The Numbers being ranked (or placed) as is there directed and done.

Then I multiply the two first terms, 100 and 12, the one by the other, and their product is 1200 (for the firm term;) then I multiply the two last terms 75 and 9 together, and their product is 675, for the third term. Then I say, as 1200 is to 6, so is 675 to the Answer, which by the Rule of Three Direct will be found to be 31. 75. 6 d. as was before found.

3. But if the Question be to be answered by the double Rule of Three Inverse, then (having placed the five given terms as before) multiply the lower-most term of the first place, by the uppermost term of the third place, and put the product for the first term; then multiply the uppermost term of the first place, by the lowermost term of the third place, and put the product for the third term, and put the second term of the three highest Numbers for the middle term to those two, then if the inverse proportion is found in the uppermost three numbers, the 4th proportional Direct to these three shall be the answer to the first Question of the 13th Chapter being stated, wit. If a 100 L. Principal in 12 months gain 6 L. Interest, what Principal will gain 3 L. 7 L. 6 d. in 9 months? State the Numbers as is there directed in the first order, vic.

then reduce the 61. and 31. 75. 6d. into pence, the 61 is 1440d. and 31. 75. 6d. is 810d. then multiply 1440 by 9, the product is 12960 for the first term in the Rule of Three Direct, and multiply 810 by 12, the product is 9720 for the third term; then I say, As 12960 is to 1001. so is 9720 to the Answer, wiz. 751. as before. But if the terms had been placed after the second order, viz.

then the Inverse Proportion is found in the lowest. Numbers, and having composed the Numbers for a fingle Rule of Three as in the second Rule foregoing, then the Answer must be found by a single Rule of Three Inverse; for here it falls out to multiply 800 by 12 for the first Number, and 1440 by 9 for the third Number, and then you must say, As 9720 is to 1001. So is 12960 to the Answer, which by Inverse Proportion will be found to be 751. as before.

The Questions in the 12th and 13th Chapters may

Terve for thy farther Experience.

CHAP. XV.

Single Fellowship.

1. FELLOWSHIP is that Rule of Planal Proportion, whereby we ballance Accompts depending

pending between divers Persons having put together a general Stock, so that they may every Man have his proportional part of Gain, or sustain his proportional part of Loss.

2. The Rule of Fellowship is either fingle, or it is

double.

3. The fingle Rule is when the Stocks propounded are tingle Numbers without any respect or relation to time, each Partner continuing his Money in Stock for the same time.

4. In the fingle Rule of Fellowship, the proportion is as the whole Stock of all the Partners is in proportion to the total Gain or Lois, so is each Man's parti-cular share in the Stock, to his particular share in the Gain or Lofs. Therefore take the Total of all the Stocks for the first Term in the Rule of Three, and the who'e Gain or Loss for the second Term, and the particular Stock of any one of the Partners for the third Term, then multiply and divide according to the 7th Rule of the 9th Chapter, and the 4th proportional Number is the particular Loss or Gain of him whose Stock you made your second number, wherefore repeat the Rule of Three as often as there are particular Stocks, or Partners in the question, and the 4th Terms produced upon the feveral Operations are the respective Gain or Lofs of those particular Stocks given; as in: the Examples following.

Quest. 1. Two Persons, viz. A and B, bought a Tun of Wine for 20 l. of which A paid 12 L and B paid 8 l. and they gained in the Sale thereof 5 l. now I demand each Mans share in the Gains according to his Stock?

First, I find the Sum of their Stocks, by adding.

them together, viz. 12 l. and 8 l. which are 20 l. then according to this Rule, I say first, If 20 l. (the Sum of their Stocks) require 5 l. the total Gain, how much will 12 l. (the Stock of A) require? Multiply and Divide by the sth Rule of

20 L

ply and Divide by the 7th Rule of the ninth Chapter, and the Answer is 3 L for the share of A in the gains; then again I say, If 20 l. require 5 l. what will 8 l. require? The Auswer is 2 l. which is the gain of B. So I conclude that the share of A in the gain is 3 l. and the share of B in the gain is 2 l. which in all is 5 l.

Quest. 2. Three Merchants, viz. A, B, and C, enter upon a joint Adventure, A put into the common stock 78 l. B put in 117 l. and C put in 234 l. and they find (when they make up their Accompts) that they have gained in all 264 l. now I defire to know each Mans particular share in the gains?

First, I add their particular stocks together, and their Sum is 429 l. then
say, If 429 l. gain 264 l. what will 78 l.
gain? and what 117 l. and what will
234 l. (the Stocks of A, B, and C,)
gain? Work by three several Rules of 2,
Sum 429

and you will find that

The Gain of $\begin{cases}
A \\
B \\
C
\end{cases}$ is $\begin{cases}
48 \\
72 \\
144
\end{cases}$ Sum 264

Quest. 3. Four Partners, viz. A, B, C, and D, between them built a Ship which cost 1730 L of which A paid 346 L B 519 L C 692 L and D 173 L and her Freight for a certain Voyage is 370 L which is due to the Owners or Builders, I demand each Man's Chare therein according to his Charge in building her.



Quest. 4. A, B, and C, enter Partnership for a certain time, A put into the common stock 364 l. B put in 482 l. C put in 500 l. and they gained 867 l. now I demand each Man's share in the Gain proportionable to his Stock.

Answer,

l. s. d.

A \$234-09-37114
B \$310-09-5732
C \$322-01-3734
Sum 867-00-0

S. To prove the Rule of Single Fellowship, add each Man's particular Gain or Loss toge.

The Proof of the Rule of Single ther, and if the total Sum is equal fo the general Gain or Loss, then is the Work rightly performed, but otherwise it is Erronious. Example, In the first Question of this Chapter, the An-

inver was that the Gain of A was 3 l. and the Gain of B 2 l. which added together make 5 l. equal to the total Gain given.

If in finding out the particular Shares of the several Partners, any thing remain after Division is ended, such remainders must be added together, (they being all Fractions of the same denomination) and their sum divided by the common Divisior in each Question (viz. the total stock) and the quotient and to the particular Gains, and then if the total Sum is equal to the total Gain the work is right, otherwise not,

As in the fourth Question, the remainders were 354, 62, and 930, which added together make 1346, which divided by 1346, (the sum of their Stocks) the Quotient is 1 d. which I add to the pence, 67c. and the sum of their shares is 867 L. equal to the total

Gain; wherefore I conclude the work is right.

CHAP. XVL

Double Fellowship. -

Ouble Fellowship is when several Persons enter into Rartnership for unequal time, that is, when every Man's particular Stock hath relation to a

particular Time.

2. In the double Rule of Fellowship, multiply cach particular Stock by its respective time, and having added the several products together make their sum the first number (or term) in the Rule of 3, and the total gain or loss the second number, and the product of any ones particular Stock by his time, the third term, and the 4th number in proportion thereunto is his particular gain or loss, whose product of Stock, and Time is your third number.

Then repeat (as in Single Fellowship) the Rule of 3, as often as there are Products or (Partners) and the 4 terms thereby invented are the numbers required.

Example.

Quest. 1. A and B enter Partnership, A put in 40 to for 3 months, B put in 75 to for 4 months, and they gained.

| 146 | Double Fellowship. | Chap. 16 |
|-------------|--------------------------------|-------------------|
| gained 70 | L now I demand each Man | is there in the |
| gains, pro | pertionable to his flock and | d time? Anfaver. |
| A 201. B | 301. | 40 J 19 |
| To reso | lve this Question, I first mul | tiply the Stock |
| of A, (vi | (401.) by its time | |
| (3 months | | 1. 1. |
| | I multiply the Stock | 40 75 |
| of B by it | s time (viz-75 by 4) | 3 4 |
| and it pro | duceth 300, which I'd - | |
| add to th | e Product of A his A is | 20 B 308 |
| Stock and | Time, and the fum | 120 |
| is 420. | Then by the Rule of | - |
| e Direct. | I fay, A3 420 (the | Sum 420 |
| Sum of th | e Products) is to 70 | |
| (the total | gain) fo is 120 (the product | of A his Stock |
| and time | to 20 L (the share of A in t | he gains) and fo |
| is 300 (th | e product of B his Stock and | time) to 50% |
| (the share | of B in the gains.) And so n | nuch ought each |
| to have fo | r his share. | • |
| Quest. 2 | . A,B and C, make a Stock | for 12 Months, |
| A put in a | it first 3641. and 4 Months a | ifter that he put |
| in 40 l. B | put in at first 408 l. and a | it the end of 4 |
| Months he | took out 86 l. C put in at | first 1484. and |
| 2 Months | after he put in 86 1. more | e, and 5 Months |
| after that | he put in 100 L more, and a | at the end of 12 |
| Months th | eir gain is found to be 1436 | il. I defire to |
| know eac | h Man's thare in the gains | according to his |
| Stock and | time? | |
| First, 1 | confider that the whole tim | e of their Part- |
| nership is | 12 Months. Then I proceed | i to find out the |
| Leveral pro | oducts or Stock and Time as f | followeth. |
| A had a | st first 364 l. for 4 months | : `` |
| wherefore | their product is | 5 43 |
| Then he | put in 40 l, which with the | εŠ |
| firft Sam r | nakes 404 L which continue | •(|

wherefore their product is

Then he put in 40 l, which with the first Sum makes 404 l, which continued the remainder of the time, viz. 8

months, and their product is

The Sum of the products of the Stock

A688

. B had

| Chap, 16. | Double Fellowshi | |
|---------------------------------------|--|-------------------|
| B had 408 l. | in 7 months, whose | 2856 |
| And then tool | k out 861, therefore he |) |
| reft of the time. | Light continued the viz. five months, whose | orði < |
| product is | |) |
| and Time of B | e products of the Stock s | 4466 |
| product being m | L for 3 months, whose ultiplied is in \$6 L, which added | 444 |
| to the first. (vi | z. 148) makes 234 l. ock 5 Months, their pro- | 1170 |
| . Then he put i | n 100 l. more, fo then | |
| months) which m | 334L which continued of the time, (viz. 4 nultipli'd together pro- | 1336 |
| The Sum of t ney and Time of | the product of the Mo- | 2950 |
| · · · · · · · · · · · · · · · · · · · | A | 4466 4688 |
| The Total Su | ım of all the product | 12104 |
| Then I fay, a | s 12104 is to 1436 (th | e total gain) for |
| is 4688 to the fl | hare of A in the gains, g Examples, and you | Oc. go on as |
| shares in the gai | n to be as followeth, Answer, | iz. |
| X 1 2 | l. s. | rate of miles |
| The share | of B is \\ 556-03-16-\\ C \\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ | -b-1496 |
| | Sum 1436—30 | |
| | ・・・・・・・ | auf. |

Quest. 3. Three Grassers, A, B, and C, take a piece of Ground for 46 l. 10 s. in which A put in 12 Oxen for 8 months, B put in 16 Oxen for 5 months, and C put 18 Oxen for 4 months, now the question is, what shall each Man pay of the 46l. 10s. for his share in that charge?

3. The proof of this Rule is the same with that of Single Fellowship, laid down in the 5th Rule of the 5th

Chapter; and note that,

if a loss be sustained instead of gain among Partners, every Man's share to be born in the loss is to be found after the same method as their gain, whether their stocks be for equal or unequal time.

C H-A P. XVII.

Alligation Medial.

proportion, by which we relove Quentions, wherein is a composition or mixture of divers simples, as also it is useful in the composition of Medicines both for quantity, quality, and ppice. And its species are two, viz. Medial and Alternate.

2. Alligation Medial is when having the several quantities and prices of several simples propounded, we discover the mean price or rate of any quantity of the mixture compounded of those simples, and the pro-

portion is,

As the fum of the simples to be mingled is to the total value of all the simples, so is any part or quantity of the composition or mixture to its mean Rate or Price.

Quest: 1. A Farmer mingleth 20 bushels of Wheat at s. per bushel, and 36 bushels of Ryc at 3 s. per buffiel, with 40 bushels of Barley, at 2 s. per bushel, now I defire to know what one bushel of that mixture is worth?

To resolve this Question add together the given quantities, and also their values, which is 96 bushels, whose total value is 14 1, 8 a as appeareth by the Work following; for,

bu(b. 20 of Wheat at 5 s. per Bufbel, is 5-0 36 of Rye at 3 s. per Bufbel, is 5-8 40 of Barley at 2 s. per Bufbel, is 4:-0

The Sum of 96, and their value is the given anantities is Then say by the Rule of 3 Direct, If 96 bulhels cost (or is worth) 14 l. 85. what is 1 bulhel worth?

Quest. 2. A Vintner mingleth 15 Gallons of Canary at 8s. per Gallon, with 20 Gallons of Malaga at 75. 4d. per Gallon, with 10 Gallons of Sherry at 6s. 8d. per Gallon, and 24 Gallons of White-wine at 4s. per Gallon. now I demand what a Gallon of that mixture is worth? Work as in the last Question, and you will find the Answer to be 6s 2d. 2grs-45. Quest.

Alligation Alternate. Chap. 18.

Queft. 3: A Grocer hath mingled 3 C. of Sugar at 36 s. per C. with 3 C. of Sugar at 3 l. 14s. 8d. per C. and with 6 C. at 1 l. 17 s. 04 d. per C. I defire to know the price of an hundred weight of that mixture?

Answer, 2 l. 11 s. 4 d.

Answer, 2 l. 11 s. 4 d.

3. The proof of this Operation is by the price of any quantity of the mixture to find out

The Proof of the total value of the whole compositi
Alig. Medial. on, and if it is equal to the total value of the several simples, the work is right,

otherwise not. As in the first Example, the answer to the question was that 2s. is the price of one bushel, wherefore I say by the Rule of Proportion, if I bushel be 3 shillings, what is 96 bushels? Answer, 141. 8s. which is the total value of the several simples, wherefore the Work is right.

CHAP. XVIII.

Alligation Alternate.

Lligation Alternate is when there are given the particular prices of feveral finiples, and thereby we discover such quantities of those simples, as being mingl'd together shall bear a certain rate propounded.

2. When such a question is stated, place the given prices of the simples one over the other, and the propounded price of the composition against them in such fort that it may represent a Root, and they so many branches springing from it, as in the following example.

Quest. 1. A certain Farmer is desirous to mix 20 bushels of Wheat at 35. or 60d per bushel, with Rye at 25. or 36d per bushel, and with Barley at 25. or 24d per bushel, and Oats at 15. 6d per bushel, and defireth to mix such a quantity of Rye, Barley and Oats with the 20 bushels of Wheat, as that the whole composition may be worth 25. 8 d. or 32 d. per bushels

The Prices of the simples being placed according to the last Rule, with the price of the composition propounded as a Root to them will stand as followeth.

2. Having thus placed the given Numbers, you are to link or combine the feveral rates of the simples the one to the other, by certain Arches, in such a fort that one that is lesser than the root (or mean rate) may be linked or coupled to another that is greater than the mean rate, so the question last propounded will stand.

4. Then take the difference between the root and the several branches, and place the difference of each against the number or branch, with which it is coupled or linked, and having taken all the differences and placed them as aforesaid, then those differences so placed will shew you the number of each simple to be taken to make a composition to bear the mean rate propounded.

So the branches of the last question being linked to-

gether as in the first manner, I say the difference between 32 and 60, is 28, which I put against 18, because 60 is linked with 18, then the difference between 22 and 36 is 4, which I

 $32 \begin{cases} 60 \\ 36 \\ 24 \\ 18 \end{cases}$

put

Alligation Alternate. Chap. 18.

rut against 24, because 36 is linked or coupled with 24, then I say the difference between 32 and 24 is 8, which I place against 36 (for the reason aforesaid) then I say the difference between 32 and 18 is 14, which I place against 60; and then the Work will

stand as you see in the Margent.

So I conclude that a composition made of 14 bushels of Wheat at 80 d. per bushel, and 8 bushels of Rye at 36 d. per bushel, and 4 bushels of Barley at 24 d. per bushel, and 28 bushels of Oats at 18 d. per bushel, will bear the mean price of 32 d. or 2 s. 8 d. per bushel. And here observe that in this composition there is but 14 bushels of Wheat; but I would mingle 20 bushels, and this kind (or rather case) of Alligation Alternate (viz.) when there is given a certain quantity of one of the simples, and the quantities of the rest sought to mingle with this given quantity, (that the whole may bear a price propounded) is called Alternation Partial.

And the proportion to find out the several quantitics to be mingled with the given quantity is as follow-

eth, viz.

As the difference annexed to the branch that is the value of an integer of the given quantity, is to the other particular differences, to is the quantity given

to the leveral quantities required.

So here, how to find out to much Rye, Barley and Outs as must be mingled with the 20 bushels of Wheat, I say by the single Rule of 3 Direct, if 14 bushels of Wheat require 8 bushels of Rye, what will 20 bushels of Wheat require? Answer, 1174 bushels of Rye.

Again, if 14 bushels of Wheat require 4 bushels of Barley, what will 20 bushels of Wheat require? Answ. 57 bushels of Barley. Again I say, if 14 bushels of Wheat require 28 bushels of Oats, what will 20 bushels of Wheat require? Answer, 40 bushels of Oats.

And now I fay, that 20 bushels of Wheat mingled with 11.7 bushels of Rye, and 5.7 bushels of Barley, and 40 bushels of Oats, each bearing the Rates as aforefuld, will make a composition or heap of Corn that may yield 32 d. per bushel.

But if the branches had been coupled according to the second order, or manner, the differences would have been thus placed. viz. the

have been thus placed, viz. the differences between 32 and 60 is 28, which I fet against 24, because 60 is linked thereto; and the difference between 32 and 36 is 4, which I fet against 18,

 $32 \begin{cases} 60 \\ 36 \\ 24 \\ 18 \end{cases} \begin{vmatrix} 8 \\ 14 \\ 28 \\ 4 \end{vmatrix}$

and the difference between 32 and 24 is 8, which I fet against 60; then the difference between 32 and 18 is 14, which I set against his yoke-fellow 36, and then I conclude that if you mix 8 bushels of Wheat with 14 bushels of Rye, 28 bushels of Barley, and 4 bushels of Oats, each bearing the aforesaid Prices, the whole mixture may be sold for 32 d. per bushel, as by the

work in the Margent.

You see by this work, we have found how many bushels of Rye, Barley and Oats, ought to be mixed with 8 bushels of Wheat, and to find out how many of each ought to be mixt with 20 bushels of Wheat, I say, as 8 is to 14, so is 20 to 35 bushels of Rye. As 8 is to 28, so is 20 to 70 bushels of Barley. As 8 is to 4, so is 20 to 70 bushels of Barley. As 8 is to 4, so is 20 to 10 bushels of Oats, whereby I conclude that if to 20 bushels of Wheat I put 35 bushels of Rye, 70 bushels of Barley, and 10 bushels of Oats, bearing each the foresaid prices per bushel, that then a bushel of this mixture will be worth 32 d. or 23.8 d.

And if the Branches had been linked as you see in the third place, where each branch bigger than the root, is linked to two that are lesses than the root, then in this case you must have placed the several differences between the root and branches, against those two with which each is coupled, as first the difference between 22 and 60 is 28, which I put against 24 and 18 be-

cause it is concled

| (60 | 1 8,14 | 22 |
|---------|------------------------------|------|
| 32 36 D | 8,14 8,14 28,4 28,4 | 22 |
| (18) | 28,4 | 32 |
| H | Digitized | y GO |

mith

with them both, then the difference between 32 and 36 is 4, which I fet likewise against 24 and 18, because 36 is linked to them both, then the difference between 32 and 24 is 8, which I put against 60 and 26, because 24 is linked to them both, then the difference between 32 and 18 is 14, which I put against 60 and 26, the yoke-fellows of 18.

Lastly, I draw a line behind the differences, and add the differences which fland against each branch, and put the fum behind the fild line against its proper branch,

as you see in the Margent.

And now by this work I find that 22 bushels of the Wheat mingled with 22 bushels of Rye, and 32 bushels of Barley, and 32 bushels of Oats, each bearing the faid price will make a mixture bearing the mean-rate of 22 d. per hushel.

And to find how much of each of the rest must be

mingled with 20 bushels of Wheat, I say,

As 22 is to 22, so is 20 to 20 bushels of Rye. As 32 is to 32, fo is 20 to 29 3 bushels of Barley. As 22

is to 22, fo is 20 to 29 3 bushels of Oats.

Whereby you see the questions of Alligation Altermate will admit of more true Answers than one; for we have found three several Answers to this first Question.

Questions of Alternation partial are proved the same way with Questions in Alligation medial, which you may fee The Proof of Altern in the 3d. Rule of the 17th Chap. nation partial. Queft. 2. A Grocer hath 4 forts

of Sugar, viz, of 12d. per l. of 10d, per l. of 6d. per l. and of 4d per 1, and he would have a composition worth 8d, per 1, the whole quantity whereof should contain 144 L made of these 4 forts, I demand how much of each he must take?

Questions of this nature are resolved by that part of Alligation alternate called by Arithmeticians Alternation total, viz. where there is given the sum, and prices of several simples to find out how much of each simple ought to be taken to make the faid sum or Oquantity.

quantity, so that it may bear a certain Rate pro-

pounded.

To resolve this Question I place the several prices of the simples and mean rate propounded, and link them together, as is directed in the 2d and 3d Rules of this Chapter, and place the differences between the root and branches according to the 4th Rule of this Chapter, which will then stand one of these three ways.

| First. | | Second. | | |
|---|-------------|---------|---------|--|
| 8 \$ 10 } | 4 2 2 4 | 8 2 6 4 | 4 4 2 - | |
| ing open Stagen Sta Stagen Stagen | I2 Third | | 12: | |

| Third | | |
|------------|--------------------------|-------|
| 8 { 12 6 } | 2,4 2,4 4,2 4,2 | 6 6 6 |
| - | _ | _ |

e. Then add the several differences together, which I have done, and the fums of the first and second order are 12 l. and of the third 24 l. as you may see above, but it is required that there should be 444 l. of the composition, therefore to find the quantity of each fample, to make the whole composition 144 l. observe this general Rule, viz.

As the sum of the differences is to the several differences, so is the total quantity of the composition to

the quantity of each fimple.

So to find how much of each fort of Sugar I ought to take to make 144 l. at 8d. per l.

As 12 is to 4, so is 144 to 481, at 12d, per t. As 12 is to 2, to is 144 to 241, at 10d. per 1. 'As 12 is to 2, so is 144 to 241. at 6d. per l. As 12 is to 4, so is 144 to 481, at 4d. per I.

156 Alligation Alternate. Chap. 18.

Whereby I find that 48 l. at 12 d. per l. and 24 L. at 10 d. per l. and 24 L. at 6 d. per l. and 48 l. at 4d. per l. will make a composition of Sugar containing

1441. worth 8d. per L.

But as the branches are linked in the second order, the answer will be 241. at 12d perl. and 48l. at 10d per l. and 48l. at 6d. per l. and 24 l. at 4d. per l. to make the said quantity, and to bear the said price.

And if you had worked as the branches are linked after the third order, then you would have found the

after the third order, then you would have found the quantity of 36 L. of each.

Queft. 3 A Vintner hath four forts of Wine, viz. Canary at 10s. per Gallon, Malaga at 8 A per Gallon;

Rhenish-wine at 6s. per Gallon; and White-wine at 4s. per Gallon, and he is minded to make a Composition of them all of 60 Gallons that may be worth 5 shillings per Gallon, I desire to know how much of

cach he must have?

The numbers of terms being ranked according to the fecond Rule of this Chapter, the branches will be linked as tolloweth, and will admit of no other manner

ed as followeth, and will admit of no other manner of coupling, because there is but one branch that is lesser than the Root; therefore all the rest must be linked unto it; and the

differences between the Root and the three first branches, viz. 10, 8, and 6, which are 5, 3,

and r, must be set against 4, because they are all coupled with it, and the
difference between the Root, (viz. 5.) and 4, which is

difference between the Root, (1/2, 5.) and 4, which is 1, must be let against the three other, because it is linked to them all.; so I find I Gallon of Canary, I Gallon of Malaga, I Gallon of Rhenish-wine, and 9 Gallons of White-Wine, prized as above being mingled together,

will be worth 5s. per Gallon, the sum being 12 Gal-

lons, but there must be 60 Gallons; wherefore I say,
As 12 is 10 1, so is 60 to 5 Gallons of Canary.
As 12 is to 1, so is 60 to 5 Gallons of Mallaga.

As 12 is to 1, fo is 60 to 5 Gallons of Rhemith.
s 12 is to 9, fo is 60 to 45 Gallons of White-wine.

So that 5 gallons of Canary, 5 gallons of Malaga, 5 gallons of Rhenith, and 45 gallons of White-wine mingled together, will be in all 60 gallons, worth 55. per gallon, which was required.

Quest. 4. A Goldsmith bath Gold of 4 several sorts of sinceres, viz. of 24 Caretts sine, and of 22 Caretts sine, of 20 Caretts Read Chap. 2. sine, and of 15 Caretts sine. And def. 2. of this he would mingle so much of each Book.

me would mingle to much of each 1800.

with alloy, that the whole Mass of
28 ounces of Gold so mingled may bear 17 Carects.

fine. I demand how much of each he must take, the second and third Rules of this Chapter being observed, (for instead of the alloy I put o, because it bears no finences, but it makes a branch in the Operation) the terms may be alligated and the differences added any of these 4 ways following, when

First thus,

24
22
20
15
17
2 2, 17
19
15, 3
8
7, 3
10

Sum 56

| Second | Sun ly thus, | 56 |
|--------|-----------------|----|
| (24) | 2 | 17 |
| 17 20 | 2, 17 | 19 |
| 11524 | 7.3 | 10 |
| | 5,3 | 8 |

Sum 36.

| (24 | 2, | 2 | | | |
|---------|-------|-----|--|--|--|
| 22 | 2, | 2 | | | |
| 17 (20) | 2,17 | 19 | | | |
| 11643 | 7,5,3 | 15 | | | |
| しんるノー | 13. | . 3 | | | |
| | | | | | |

Sum 41

Tou thly,

Chap. 18.

| Fourthly thus, | | | | | |
|----------------|--------|----------|----|--|--|
| ٠, | 24 | 2, 17 | 19 | | |
| | 22 | 2, 17 | 19 | | |
| 17 | 20- | 2, 17 | 19 | | |
| | 15-14/ | 7, 5, 3, | 15 | | |
| į, | Outs | 7, 5, 3, | 15 | | |

Sum 87

. More ways may be given for the Alligating, or linking of the Terms in this Question, but these are sufficient for the Industrious, and it shall also suffice to give an answer to the Question as the Terms are link'd the first way, not doubting but the ingenious Practitioner will be able at his leifure to find Answers to the other 2 ways, viz. p.w.

As 56 is to 17, so is 28 to 8-10 of 24 As 46 is to 2, 10 is 28 to 10 00 of 22 As 56 is to 19, so is 28 to 9—10 of 20
As 56 is to 18, so is 28 to 4—00 of 15
As 56 is to 10, so is 28 to 5—00 of alloy.

Thus much well practifed and understood, is sufficient for the understanding of Alligation,

In Questions of Alternation Total. The proof of Al- the Answer given is true, when the ternation Total. Sum of each of the quantity of simples found, agrees with the Sum or quan-

tity propounded, as in the last Question, the Answer was 8 oz. 10 p.m. of 24 Carects fine, 10 oz. of 22 Carects fine, 9 ez. 10 p.w. of 20 Carects fine, 4 oz. of 14 Carects fine, and 5 oz. of Alloy, which added together make 28 oz. the quantity propounded.

> CHAP. XIX. Reduction of Vulgar Fradions.

Hat a Vulgar Fraction is, and its parts and feveral kinds, hath been already shewed in

Chap. 10

the 19, 20, 21, 22, 23, 24, and 31 Definitions of the first Chapter of this Book, which the Learner is defi-

red diligently to observe before he proceeds.

2. To reduce a Vulgar Fraction (which discovereththe principal knowledge of Fractions, and therefore ought greatly to be regarded) we shall discover plain-Iv under these eight several Heads (or Rules) follow-

r. To reduce a mixt number into an improper

Fraction.

2. To reduce a whole number into an improper Fraction.

2. To reduce an improper Fraction into its equiva-

lent whole (or mixt) number.

4. To reduce a Fraction into its lowest terms equivalent to the Fraction given.

s. To find the value of a Fraction in the known

parts of Coyn, Weight, Measure, &c.

6. To reduce a compound Fraction to a simple one of the fame value.

7. To reduce divers Fractions having unequal Denominators, to Fractions of the same value, having an equal Denominator.

8. To reduce a Fraction of one Denomination to

another of the same value.

I. To reduce a mixt Number to an improper Fraction.

The Rule is,

Vide Chap. I. debn. 31.

Multiply the Integral part (or whole Number) by the denominator of the Fraction, and to the Product add the Numerator, and that Sum place over the Denominator for a new Numerator; so this new Fraction shall be equal to the mixt number given. As for Example.

1. Reduce 183 into an improper Fraction, multiply the whole number 18 by 7 the denominator, and to the Product add the numerator 3, the Sum is 129, which put over the denominator 7, and it makes 12% for the Answer, as followeth.

Chap. 19.

18**3**

129 facit

I 29

7

2. Reduce 183 4 to an improper fraction facit 3 844 3. Reduce 9644 to an improper fraction, facit 1244

II. To reduce a whole Number to an improper fraction.

The Rule is,

Multiply the given Number by the intended denominator, and place the Vide Chap. 1. product for a numerator over it. As defin. 23. for Example.

1. Let it be required to reduce 15 into a fraction whose denominator shall be 12.

To effect which I multiply 15
by the intended Denominator
(12) the product is 180, which
I plate over 12 as a Namera- facit 1.0 15
tor, and it makes 180 15
is equal to 15, as was required,
as per Margent.

2. Reduce 36 into an improper fraction whose de-

nominator shall be 26, facit 315.

3. Reduce 135 into an improper fraction whose demominator shall be 16, facit 2159.

III. To Reduce an improper fealtion into its equivalent whole or mine number.

The Rule is.

Divide the Numerator by the Denominator, and the Quotient is the whole number equal to the fraction, and it any thing remain, part it for a Numerator over the Divilor, Example.

itized by Googly. Reliece

1. Reduce 434 into its equivalent mixt number. divide the Numerator 436 by the denominator 8, and the quotient is 54, and 4 remains, which put for a numerator over the divisor 8, the Answer is 54 4, as followeth.

8) 436 (544

36 facit 54 \$

2 Reduce \$475 to a mixt number, facit 23155. 3. Reduce 1775 to a mist number, facit 114773.

IV. To reduce a fraction into its lowest terms equivalent to the fraction given. The Rule is.

T. If the numerator and denominator are even numbers. take half of the one, and half of the other as often as , may be, and when either of them falls out to be anodd number, then divide them by any number that you can discover will divide both numerator and denominator, without any Remainder; and when you have thus proceeded as low as you can reduce them, then this new Fraction to found out shall be the Fraction you. defire, and will be in value equal to the given Fraction. Example.

1. Let it be required to reduce : ? into its lowest

First, I take the half of the Nume-

192 | 96 | 48 | 24 | 12 | 4 336 | 168 | 84 | 42 | 21 | 7 rator 192 and it is 96. then half of the De-

nominator, and it is 168, so that now it is brought to 125, and next to \$8, and by halfing still to 34, and their half is 12, and now I can no longer half it, becanse 21 is an odd number, wherefore I try to divide them by 3, 4, 5, 6, 6% and I find 3 divides them both without any remainder, and brings them to 4, as per-Margent.

So I conclude 4 thus found to be equal in value to the given fraction 133.

2. What is 10 in its lowest terms? Answer

3. What is $\frac{1}{12}$ in its lowest terms? Answer $\frac{1}{12}$.

There is yet another way more excellent than the former to reduce a fraction into its Vide Ought. Cla. lowest terms, and that is by finding a common Measurer, viz. the greatest number that will divide the nu-Math. Cap. 7.

merator and denominator without any femainder, and by that means reduce a frastion to its lowest terms at the first work; and to find out this common measurer divide the denominator by the numerator, and if any thing remains divide your Divisor thereby; and if any thing yet remains, then divide your last Divisor by it; do to until you find nothing remains; then this last Divisor shall be the greatest common measurer, which will divide both numerator and denominator, and reduce them into their lowest terms at one Work.

Example.

4. Reduce 13 into its lowest terms by a common measurer. To effect which, I divide the denominator 304 by the numerator 228 and there remains 76, then I divide 228 (the first Divisor) by 76 (the remainder) and it quotes 3, and nothing remains; wherefore the last Divisor 76 is the common measurer, by which I divide the numerator of the given Fraction, viz. 228, it quotes a for a new numerator, then I divide the densminater 304 by 76, and it quotes 4 for a new denominator, that now I have found a equal to 33%.

5. Reduce 5048 into its lowest terms by a common

measurer, facit 72.

6. Reduce 33.8 into its lowest terms by a common mealurer, facit 13. A Compendium.

Note that if the numerator and denominator of a fra-Bion, and each with a Cypher or Cyphers, then cut off as many Cyphers from the one as from the other, and the remaining figures will be a Fraction of the same value, viz. 3400 will be found to be reduced to \$4. by cutting off the two Cyphers from the numerator and denominator, with a dash of the Pen thus, 34 20, and 400, will be 40, thus 400. Oc.

Y. To find the Value of a Fraction in the known parts of Coyn, Weight, &c.

The Rule is,

Multiply the numerator by the parts of the next inferiour denomination that are equal to an Unit of the same denomination with the Fradion; then divide that Product by the denominator, and the quote gives you its value in the same parts you multiplied by, and if any thing remain multiply it by the parts of the next inferiour denomination, and divide as before, do so till you can bring it no lower, and the several quotients will give you the value of the Fradion as was required, and if any thing at last remain; place it for a numerator over the former denominator; some sew Examples will make the Rule plain.

1. What is the value of $\frac{37}{27}l$. Sterling? To answer this Question I multiply the numerator 27 by 20 (the shillings in a pound) the product is 540, which I divide by 29 (the denominator) and the quotient is 18s. and there remains 18, which I multiply by 12 pence, and the product (216) I divide by the denominator 29, the quotient is 7d. and 13 remains, which I multiply by 4 Barthings, the product is 52, which I fill divide by 29, the quotient is 1 Farthing, and there remaineth 23, which I put for a numerator over the denominator 29, so I find the value of \(\frac{2}{27}l \). to be 18s. 7d. 14r. \(\frac{2}{27} \), as by the following Operation, and after the same manner are the values of the Fractions in the several Examples following found out.

₹71.

Multiply . 20

29) 540 (18% 7d. 123).

29 250 232

Remains (18)

Multiply 12

18 36

29) 216 (74.

203

Remains (13)
Multiply 4
——— qr.

29) 52 (1²⁴/₂₈

Remains (23)

s. d. qr. Facit 18-7-123

1d. 17.

4. What is 15 C. weight? Facit 3 qrs. 11. 572. 37.

5. What is 11 l. Troy weight? Facit 3 oz. 5 p.m.
22 11 gr.
6. What is 11 of a year? Answer, 299 days 7 bours

12 min.

VI. To Reduce a compound Fraction to a simple one of the same value.

What a compound Fraction is, hath been shewed in Chap. 1. Definition 24, and to reduce it to a simple Fraction of the lame Value.

The Rule is.

Multiply the Numerators continually, and place the last product for a new Numerator, then multiply the Denominators continually, and place the last product for a new Denominator. So this single Fraction shall be equal to the compound Fraction given. Example.

L. Reduce ? of ? of ? to a simple Fraction.

Multiply the Numerators 2, 3, and 5 together, they make 30 for a new Numerator 3 then I multiply the Denominators 3, 5, and 8 together, and their Product is 120 for a Denominator, so the simple Fraction is 35, and cutting off the Cyphers, it is -3 equal to 1 by the fourth Rule foregoing.

| 5 | 12 | ٠.٠ | • | • <u>i</u> | .2 |
|------|----|-----|---|--|----|
| ં કે | | | | | 2 |
| | ٠. | | | | - |
| 15 | | | | | 6 |
| 8. | i. | , | | ن ــــــــــــــــــــــــــــــــــــ | 5 |
| 1 | | | | | _ |
| 120" | | • | | | ŞΟ |

Facit, -1: or -3 or 4.

2. What is -? of \$ of \$ of \: Answer, \$? 8 or \$? \$: or 27 in its least terms.

3. What is $\frac{1}{12}$ of $\frac{1}{13}$ of $\frac{2}{13}$? Answer, $\frac{1}{24}$? By this you may know how to find the value of a Compound Fraction, viz. first reduce it to a simple one, and then find out his value by the 5th Rule forcgoing.

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What is the value of 1 of 1 of 2 of a pound?

Answer, 11s. 3d.

VII. To reduce Fractions of unequal Denominators to Fractions of the same value, having equal Denominators.

The Rule is,

Multiply all the Denominators together, and the Product shall be the Common Denominator. Then multiply each Numerator into all the Denominators except its own, and the last product put for a Numerator over the Denominator found out as before: So this new Fraction is equal to that Fraction, whose Numerator you multiplied into the said Denominators. Do so by all the Numerators given, and you have your defire.

Example.

1. Reduce \(\frac{1}{4}, \frac{4}{5}, \) and \(\frac{7}{2}, \) to a common Denominator. Multiply the Denominators \(4, 5, 6\), and 8 together continually, and the product is 960 for the common Denominator; then multiply the Numerator \(\frac{1}{2}\) into the Denominators, \(5, 6\), and \(8\), and the product is 720, which is a Numerator to 960 (found as before) fo \(\frac{7}{2}\) is equal to the first Fraction \(\frac{1}{4}\), then I proceed to find a new Numerator to the second Fraction, \(\siz_1\), \(\frac{1}{4}\), and I multiply \(4\) (into all the Denominators except its own, \(\siz_1\)) into \(4\), \(6\), and \(8\), which produce th \(\frac{7}{4}\), equal to \(\frac{1}{4}\), then multiply the Numerator \(\frac{1}{4}\) into the denominators \(4\), \(5\), and \(6\), the product is \(\frac{3}{2}\), equal to \(\frac{7}{4}\), and the work is done; so that for \(\frac{1}{4}\), \(\frac{3}{4}\), and \(\frac{7}{4}\), I have \(\frac{72}{260}\), \(\frac{760}{2600}\).

2. Reduce 13, 14, and 12, into a common deno-

minator, faciunt 1738, 1538, and 1344.

VIII.

VIII. To reduce a Fradion of one Denomination to another.

1. This is either Afcending, or Defcending. Afcending when a Fraction of a smaller is brought to a greater Denomination, and Descending when a Fraction of a greater Denomination is brought lower-

2. When a Fraction is to be brought from a leffer to a greater Denomination, then make of it a compound Fraction by comparing it with the intermediate Denominations between it, and that you would have it reduced to, then (by the 6th Rule foregoing, reduce your Compound to a simple Fraction, and the Work is done. Example.

Quest. 1. It is required to know what part of a

pound fterling 5 of a peny is?

To refolve this, I confider that Id. is To of a shilling, and a milling is 11 of a pound; wherefore \$ d. is $\frac{1}{2}$ of $\frac{1}{12}$ of $\frac{1}{12}$ of a pound, which by the faid 6th Rule I find to be $\frac{1}{12}$ of a l. sterling of English Money.

Quest. 2. What part of a pound Troy weight is 4 of

a peny weight? Answer, & of 15
3. When a Fraction is to be brought from a greater to a lesser denomination, then multiply the Numerator by the parts contained in the several denominations betwixt it; and that you would reduce it to; then place the last product over the denominator of the given Fraction. Example,

Quest. 3. I would reduce \$ L to the Eraction of a Peny; to do which I multiply the Numerator 3 by 20 and 12, the product is 720, which I put over the

Denominator 5, it makes 225 of a peny, equal to \$ L. Quest. 4. What parts of an Ounce Troy is 15 1.?

Answer, 50 oz.

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CHAP. XX.

Addition of Vulgar Fractions.

I. IF your Fractions to be added have a common Denominator, then add all the Numerators together, and place their fum for a Numerator to the common Denominator, which new Fraction is the Sum of all the given Fractions; and if it be improper, reduce it to a whole or mixt number, by the 3d. Rule of the 19th. Chapter.

Quest. 1. What is the Sum of 37, 14, 14, and 14?

The Denominators are equal, viz. every one is 24, wherefore add the Numerators together, viz. 7, 9, 16 and 14, their Sum is 46, which put over the Denominator 24, it makes \$5 the Sum of the given Fractions, which will be reduced to the mixt Number 1, 30 or 12.

2. But if the fractions to be added have unequal Denominators, then reduce them to a common Denominator by the 7th Rule of the 15th Chapter, and then add the Numerators together, and put the fum over the common Denominator, 47c. as before in the last

Example.

The fractions reduced to a common Denominator are \$880, 4100, 4110, and 4400, the fum of their Numerators is 1,800, which put over the common Denominator, makes \$150,00 150, equal to the mixt number 344, or 352 for the fum required.

Quest. 3. What is the sum of 13, 17, and 15?

Answer, 143 14.

3. If you are to add mixt numbers together, then add the fractional parts as before, and if their sum be an improper fraction reduce it to a mixt number, and add its Integral part to the Integral parts of the given mixt Numbers, and the Work is done.

Quest. 4. VVhat is the sum of 13 1 and 24 1?

Firft

First add the fractions \(\frac{1}{4}\) and \(\frac{1}{4}\), the sum is \(\frac{1}{4}\)\frac{1}{2}\, then add this Integer 1, to 13 and 24, their sum is 38, and put after it the fraction \(\frac{1}{4}\)\rightarrow
it is \(28\)\frac{1}{4}\.

Quest. 5. What is the sum of 483, 644, and 1303?

facit, 243 32, or 24345.

4. If any of the fractions to be added is a compound fraction, it must first be reduced to a simple fraction by the 6th Rule of Chapter 19, and then add it to the rest, according to the 2d. Rule of this Chapter. Example,

Quest. 6. What is the sum of \(\frac{1}{2}, \frac{1}{2}, \) and \(\frac{2}{3} \) of \(\frac{1}{2} \) of \(\frac{1}{2} \) into a simple fraction, and it is \(\frac{1}{2} \) \(\frac{1}{2} \), which reduced with the other two, and added are 27\(\frac{1}{2} \) \(\frac{1}{2} \).

Quest. 7. What is the sum of 11 and 4 of 4 of 5?

Answer, 1-5.

3. If the fractions to be added are not of one denomination, they must be so reduced, and then proceed as before.

Quest. 8. What is the Sum of 11. and 5 s.?

Of the given Fractions here; one is of a pound and the other the Fraction of a shilling; and before you can add them together, you must reduce \$5. to the Fraction of a pound as the other is (by the 8th Rule of Chapter 19.) and it makes \$\frac{1}{12}\sight\{l}\$. then \$\frac{1}{2}\ll \text{ and }\frac{1}{12}\sight\{l}\$. will be found to be \$\frac{3}{2}\sight\{l}^2\cdot\ll \text{ l}\$ by the \$7th Rule of Chapter 19, and in its lowest terms \$\frac{1}{2}\ll \ll \text{ l}\$. by the \$4th Rule of Chapter 19.

It would have been the same, if (by the latter part of the 8th Rule of Chapter 19.) you had reduced 21. to the Fraction of a shilling, which you would have found to have been \$\frac{2}{3}s\$. which added to \$\frac{2}{3}s\$, by the said \$17th\$ Rule of the last Chap, the sum is \$15.5.\frac{2}{3}s\$, which is equal to the sum sound as before, viz. \$\frac{1}{3}\$\$ \$\frac{1}{3}\$\$ \$1. for (by the \$5th\$ Rule of Chapter 19.) the value of \$\frac{3}{4}\$\$ \$\frac{1}{3}\$\$ will be found to be \$15.5.\$ \$10.d.\$ and so will \$15.5.\frac{2}{3}\$\$ be found to be just as much.

Subtraction of Chap. 21.

Quest. 9. What is the Sum of & L. & s. and & d. Anforer, 35 3500 or \$500 L. or in its lowest terms - \$2.00 L.

CHAP. XXI.

Subtraction of Vulgar Fractions.

THE Rules in Addition for reducing the given Fractions to one denomination, are here to be observed; for before Subtraction can be made, the Fractions must be reduced to a common denominator, then subtract one Numerator from the other, and place the remainder over the common denominator, which Fraction shall be the excess or difference between the given Fractions. Example,

Quest. 1. What is the difference between \(\frac{1}{2}\) and \(\frac{1}{2}\)? The given fractions are reduced to \(\frac{1}{2}\) and \(\frac{1}{2}\) and there remains 1, which being put over the denominator 28, makes \(\frac{1}{2}\) for the answer or difference between \(\frac{1}{2}\) and \(\frac{1}{2}\). What is the difference between \(\frac{1}{2}\) and \(\frac{1}{2}\).

of i?

170

Reduce the compound fraction of 3 of 5 to a simple fraction, then proceed as before, and the answer is

110 equal to 11.

whole a fraction is given to be fubtracted from a whole number, subtract the numerator from the denominator, and put the remainder for a numerator to the given denominator, &! subtract an Unit (for that you borrow'd) from the whole number, and the remainder place before the fraction found as before, which mixt number is the remainder or difference sought. Example,

Quest. 3. Subtract - ? from 48.

Answer, 4773, for if you subtract 7 (the numerator from 10 (the deconinator) there remains 3, which put over 10 is 73 and 1 (I borrowed) from 48 rests 47, to which join 73 and it makes 47 73 for the excess.

Quest. 4. Subtract 17 from 57 mains 56 18.

3. If Digitized by Google

2. If it is required to subtract a fraction from a mixt number, or one mixt number from another, reduce the Fractions to a common denominator, and if the fraction to be subtracted be lesser than the other, then subtract the lesser numerator from the greater, and that is a numerator for the common denominator; then Subtract the lesser integral part from the greater, and the remainder with the remaining frallion thereto annexed, is the difference required between the two given mixt numbers. Example.

Quest. s. Subtract 26 3 from 54 5.

First, Subtract &, viz. 45 from &, viz. 45, the remainder is \$17, then 26 from 54 remaineth 28, to which annex \$27, it makes 28\$2 for the Answer.

4. But if the fraction to be subtracted is greater than the fraction from whence you subtract, then having first reduced the fraction to a common denominator. take the numerator of the greater Frallion out of the denominator, and add the remainder to the numerator of the leffer Fraction, and their Sum is a new numerator to the common denominator, which fraction note, then (for the 1 you borrowed) add 1 to the integral part to be subtracted, and subtract it from the greater number, and to the remainder annex the fra-Fion you noted before, fo this new mixt number shall be the difference fought. Example.

Quest. 6. Subtract 142 from 224.
The fractions reduced are, viz. equal to 24, and 4 equal to 16, now I should subtract 14 from 16, but I cannot, therefore I subtract 21 from 28 rests 7, which added to 16 (the leffer numerator) makes 23 for a numerator to 28, viz. 33, then I come to the integral parts 14 and 29, and fay, I that I borrowed and 14 is 14, which taken from an there rests 14, to which annexing 2 it is 142 for the remainder or difference between 14% and 29%.

Quest. 7. Subtract 367? from 744, facit 2722.

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CHAP. XXII.

Multiplication of Vulgar Fractions.

1. TF the Multiplicand and Multiplier are simple (or fingle) Fractions, then multiply the numerators together for a new numerator, and the denominators for a new denominator, which new Fraction is the product required.

Quest. 1. What is the product of 5 by 12? facit 45. For the numerators 5 and 9 being multiplied make 45, and the denominators 7 and 11 being multiplied

make 77.

Quelles What is the product of 13 by 37? fac. 372. 2. Af the Fractions to be multiplied are mixt numbers reduce them to improper Fractions by the Ist the 19th Chapter, then proceed as before. -

Quelt. 2. What is the product of 48 by 13 1? The given mixt numbers being reduced to improper Fractions, are 482 equal to 243, and 121 equal to 32. now 143 multiplied by 83 according to the first Rule

of this Chapter, produceth 2014? or 672-2. Quest. 4. What is the product of 430-5 by 183?

facit, 535474 or 793524.

a. If a compound Fraction is to be multiplied by a fimple Fraction, first reduce the compound Fraction into a simple Fraction, then multiply the one by the other, as is taught above.

Quest. 3. What is the product of 14 by 3 of 4 of 4? The Compound Fraction 2 of 5 of 4 reduced is 500 or 15, which multiplied by 15 produceth 395, which in its lowest terms is 15 for the Answer.

And if the Multiplicand and Multiplier are both compound Fractions, reduce them both to simple ones, then multiply these new Fractions as before, so have you the product.

Quest. 6. What is the product of 2 of 3 by 2 of 2? Answer, -13, in its lowest terms 3.

Quest. 7. What is the product of ? of \$ by ? of \$? Answer.

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Answer, 360 or 36 or in its least terms 2.

4. If a Fraction be to be multiplied by a whole number, put under the given whole number an Unit for a denominator, whereby it will be an improper Fraction, then multiply these Fractions as before. Example.

Quest. 8. What is the product of 24 by??

Answer, 43, for 24 by putting an Unit under it will be 24, and 24 by 2 produceth 43 or 16.

Quest. 9. What is the product of 36 by 12? Answer,

3-4 or 29 - 5.

CHAP. XXIII.

Division of Vulgar Fractions.

1. IF the Dividend and the Divisor are both simple Fractions, then multiply the numerator of the dividend into the denominator of the Divisor, and the product is a new numerator, and multiply the denominator of the Dividend into the Numerator of the Divisor, and the product is a new denominator, which new Fraction thus found, is the Quotient you defire. Example.

Quest 1. What is the Quotient of & divided by ??

Answer, 25 or 124, for first I mul-tiply (5) the numerator of the divividend into (5) the denominator of the divisor, and the product (25) is a numerator for the Quotient, then 1 multiply (8) the denominator of the dividend into (3) the numerator of the divisor, and the product (24) I put in the quotient for a denominator, so I find $\frac{1}{2}$ is the quotient fought.

Quest 2. What is the quotient of 12 divided by 3?

Answer, 10 equal to ; in its lowest terms.

2. But if you would divide a simple Fraction by a compound, or a compound by a fimple, first reduce fuch itized by Google

fuch compound to a simple Fraction, then go on as before.

Quest. 2. What is the Quotient of 1 divided by 2 of]? Answer, 35 or 3, first reduce 3 of 3 into a fimp'e Fraction, and it is Ti, by which To being divided, the Quotient is 35, equal in its least terms to ?. And if the Dividend and Divifor be both compound Fractions, reduce them both to simple Fractions, then diwide the one by the other, as in Rule 1. beforegoing.

Quest. 4. What is the quote of ? of ? divided by ?

of \$?

Answer, 180 or 18 or 175 or 13 in its lowest terms. 3. If the Dividend or Divisor, or both are mixt

numbers, reduce them to improper Fractions, and perform Division as you were raught before, Example. Quest. . What is the quote of 124 divided by 214?

Answer, 252, for 124 is equal to 72, and 212 is equal to 'of, and the quote of 14 divided by 102 is as

efore 215.

4. If you divide a Fraction by a whole number, or a whole number by a Fraction, make the whole number an improper Fraction, by putting an Unit for a denominator to it, as was taught in Rule 4. of Chap. 22. and then perform Division as before was taught. Example,

Quest. 6. What is the quote of 8 divided by ??

Answer, 49 which is equal to 131, being reduced as is before directed. See the Work in the Margent.

Quest. 7. What is the quotient of & divided by 8? Answer, - .

as per Margent.

CHAP. XXIV.

The Rule of Three Direct in Vulgar Fractions.

S in the Rule of Three in whole Numbers, so likewise in Fractions, you must see that the Fractions of the first and third places be of the same denomination.

2. See that if any of the given Fractions be compound, that they be reduced to simple of the same

value.

3 If there are given mixt numbers, reduce them to

improper Fractions by the first Rule of Chap. 10.

d. if any of the three terms is a whole number, make it an improper Fraction by constituting a Unit

for its denominator.

Having reduced your Fraction as is directed in the 4 last Rules, then proceed to a Resolution which is performed the same way as in whole Numbers, respect being had to the Rules delivered for the working of Fractions, viz. multiply the 2d and 3d Fraction together, according to the 1st Rule of Chap. 22. and divide the product by the first Fraction, according to the 1st. Rule of Chap. 22. and the Quotient is the Answer.

Or (which is better)

5. Multiply the numerator of the first Fraction into the denominators of the second and third, and the product is a new denominator, then multiply the denominator of the fiell Fraction into the numerators of the fecond and third, and the product is a new numerator; which new Fraction is the 4th proportional or answer, which (if it is an improper Fraction) must be reduced to a who'e or mixt number by the third Rule of Chap. 10. Examples.

Quest. 1. If 3 yards of Cloth cost \$1. what will - ?

vards-coft ?

Having placed the given Fractions according to the 6 Rule of Chap. 10. I proceed to the resolution, and first I multiply the numerator of the first Fraction (3)

into

| 1.76 into 8 | The Rule of and 10, the de- | Three i | n | Cha | p. 24. |
|---|--|----------------|----------------|-------------|-------------------|
| cond and and the | ors of the fe- l third fractions product is 240 | yds. | 1. | yds. | 180 |
| for a der I multip minator | lominator, then ly 4 the deno- of the first fra- o 5 and 9 the | 4 facit | 8 1. 180 | 10 equal | 240 1. to 3 |
| Numerat | ors of the fe- third fractions, | | 240 | | 4 |
| the proc tor 180 fwer, eq Quest. | luck is 180 for a 1 and denominator unal to \$ 1. or 15 2. If \$ 1. buy \$ | 240 mak s. | C 3 4 0 | l. for th | e An- |

yds cost at that rate? Answer. 12:1. equal to 11 1. or 14 s. 8 d.

Quest. 3. If ? 1. cost ? s. what will & s. buy ?

Answer, $\frac{2}{2}\frac{14}{16}$ l. equal to $1\frac{1}{2}$ l.

Quest. 4. If ? of an Ell of Holland cost 1 of a pound, how much will 123 Ells cost at that rate? Answer, 190 equal to 7 17 1.

in resolving the last question and the two next, obferve the third Rule of this Chapter foregoing.

Quest. 5. If 7? of a C. cost 284 s. what will 71 C. cost at that rate?

Answer, 23662 s. or 118 l. 6 s. 8 d.

Quest. 6. If 34 yds of Velvet cost 351. how much will 10 1 yds cost at that rate?

Answer, 1147 L

Quest. 7. If 3 yds of Broad Cloth cost 24 1. what will 141 yds cost?

Answer, 13 l. 9 s. 4 d.

In working the last question and the 4 next, observe the 4th Rule of this Chap. foregoing.

Quest. 8. If 14 1. of Pepper cost 14 s. 63 d. I de-

mand the price of 731 L.

Answer, 3 l. 16 s. 74 d.

Quest. 9. If 1 l. of Cochenele cost 1 l. 5 s. what will 36-71. cost?

Anjwer, 45 l. 17 s. 6 d.

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Quest. 10. If one yard of Broad-Cloth cost 15 \$ 5. what will 4 pieces, each containing 27% yards at that rate ?

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Answer, 851. 143. 31d.

Quest. 11. A Mercer bought 3 pcs of filk, each pc. qt. 24 Ells at 6s. 03d. per Ell, I demand the value of a! pcs at that rate?

- Answer, 261. 25. 13d.

In resolving the 4 next questions observe the 8th Rule of Chapter 19.

Quest. 12. If ? of an ounce of silver cost 2s. I de-

mand the price of 113 l. at that rate?

Answer, 35 l.

Quest. 12. If 551. of Gold is worth 2051. 14s. 23d. what is I grain worth at that rate?

Answer, 13.

Quest. 14. If 3 yards of Silk is worth 3 of \$ 1. what is the price of 152 Ells Flemish?

Answer, 91. 12s. 6d.

Quest, 15. If 3 of 3 of a pound of Cloves cost 6s 23d. what cost the C. weight at that rate?

Answer, 69 l. 6s. 8d.

Note that when the Auswers to the Questions in this and the next Chap, are given in Fractions, they are given in their lowest terms.

CHAP. XXV.

The Rule of Three Inverse in Fractions.

1. IT hath been already taught (in the third Rule of the 11th Chap.) how to discover when the 4th proportional number (to the 3 given numbers) to be found out by a Rule of 3 Direct, and when by a Rule of a Inverse, to which Rule the Learner is now referred.

2. When (in Fractions) you find a question to be resolved by the Rule of 3 Inverse, viz. when the third Term is the Divisor, (then having reduced the terms,

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cxaft'y according to the Rules in Chap. 24.) multiply the numerators of the 3 Fractions into the denominators of the second and first Fractions, and the product is a new denominator, then multiply the denominator of the third Fraction into the numerators of second and first Fractions, and the product is a new numerator, which new Fraction thus found is the answer to the question.

Quest. 1. If \(\frac{1}{2}\) of a yard of Cloth that is 2 yds wide will make a Garment, how much of any other Drapery that is \(\frac{1}{2}\) of a yard wide will make the same Gar-

ment?

Answer, 21 yards:

Quest. 2. Lent my Friend 461. for $\frac{4}{7}$ of a year, how much ought he to lend me for $\frac{2}{12}$ of a year?

Answer 63, 31.

Quest. 3. It 3 of a yard of Cloth that is 24 yards wide will make any Garment, what breadth is that Cloth, when 14 yards will make the same Garment?

Answer, 13 of a yard wide.

Quest. 4. How many inches in length of a board that

is o inches broad will make a foot square?

Answer, 16 inches in length.

Quest. 5. If when the bushel of Wheat cost 42 s. the peay Loaf weigheth 103 ounces, what will it weigh when the bushel cost 8-2s.?

Answer, 51 \$4 Ounces.

Quest. 6. If 12 Men can mow 24 Acres in 10 days, in how many days will 6 men do the same ?

Answer, in 21 days.

CHAP. XXVI.

Rules of Practice.

7. IN the fingle Rule of Three, when the first of the 3 Numbers in the Question (after they are disputed according to the 6th Rule of Chap. 20) hapneth

to be an Unit (or 1) that Question many times may be resolved far more speedily than by the Rule of 3, which kind of Operation is commonly called Practice, and indeed it is of excellent use amongst Merchants, Tradesmen and others, by reason of its speediness in finding a Resolution to such kind of Questions.

2. The chiefest Question resolvable by these brief Rules may be comprehended under the several general heads or cases following, viz.

When the given price of the Integer toujifts,

1. Of farthings under 4.
2. Of pence und farthings.
4. Of fillings under 20.
5. Of fillings, pence and farthings.
6. Of pounds,
7. Of pounds, shillings, pence and farthings.
things.

It would be very convenient for the Practical Arithmetician to have by heart the several products of the Nine Digits multiplied by 12, for his speedy reducing pence into shillings, or shillings into pence, which he may gain by the following Table.

3. Shillings are practically reduced into pounds thus, viz. cut off the figure standing in the place of. Units with a dash of the Pen and note it for shillings, then draw a line under the given Number, and take

half of the remaining figures (after the first is cut off) and set them under the line, and they are so many pounds, but if the 4365|8 last figure is odd, then take the sets off (as before) for shillings, as if I 2182—18 were to reduce 43658 shillings into pounds, first I cut off the last figure (8) for shillings, then I take half of the remaining figures (4365) thus half of 4 is 2, which I put under the line, then half of 3 is 1, and because 3 is an odd number, I make the next figure 6 to be 16, and I go on, saying, half of 16 is 8, and then half of 5 is 2, which is the last figure, wherefore because 5 is an odd number, I add 10 to the 81 cut off, and it makes 185. so that I find it to be

4. It is likewise convenient that the Learner be acquainted with the practical Tables following, the first containing the Aliquot (or even) parts of a shilling, the second containing the Aliquot parts of a

pound.

2182 l. 18 s. as per Margent.

The even
$$\begin{cases} d. \\ 6 \\ 4 \\ 3 \end{cases}$$
 is
$$\begin{cases} \frac{1}{4} \\ \frac{1}{4} \\ \frac{1}{4} \end{cases}$$
 fhilling.
$$\begin{cases} 1 \\ 1 \\ 1 \end{cases}$$

Cafe I.

5. When the price of the Integer is a farthing, then take the 6th part of the given number, which will be so many three-half-pences, and if any thing remains it is farthings, by the 7th Rule of Chapter 9. then consider that three-half-pence is \(\frac{1}{3}\) of a shillings, wherefore take the eighth part of them for shillings, and if any thing remain they are so many 3 half pence, which reduce into pounds by the third Rule foregoing. Example, What comes 67486 l. to, at a Farthing per l. First I take \(\frac{1}{2}\) of 67486 and it is 11247 three half-pence and 4 farthings, or one peny; then \(\frac{1}{3}\) of 11247 is 1405 s. and 7 remains, which is 7 three-half-pence, or 10\(\frac{1}{3}\)d. which with the 4 farthings before make 11\(\frac{1}{2}\). d and 1405 shillings, which by the 3d Rule is 70l. 5s. In all 70l. 5s. 11\(\frac{1}{2}\). d for the Answer. See the Work following.

Other Examples follow.

| at I qr. | | 6380 l. at 1 gr. |
|-----------|--------------------------------|---------------------------|
| 2 qrs. | 1 | 1063 2 qrs. |
| 8 d. | | 13 2 — 11 d. |
| 3—8 facit | | l. 3. d. 6-42-11 facie |
| | 2 qrs. 8 d. 6. d. 3—8 facis | 8 d. |

6. When the price of the Integer is a farthings, then take the third part of the given Number for fo many three-half-pences, and the remainder (if any) is halfpence, then take the eighth part of that for shillings, as before, &c.

|] ; | Examp 17368 l. at 2 qrs. | les. - | qrs. |
|-------|-----------------------------|-------------|------------------|
| ; | 2456 | 27822 | qrs. |
| 1 2 4 | 301 | 7: 34/79 | $d, \frac{1}{3}$ |
| | l. s. 15—7 facit | l. s. d. | facit |

7. When the price of the Integer is 3 farthings, then take half the given Number for three-half-pen, (and if any thing remain it is 3 farthings) then take the 8th. of that for shillings, as before, erc.

| 1 1/2 | 14736 l. at 3 grs. | Example | } -≟ | 5425 l. at 3 grs. |
|-------|----------------------|---------|---------|--------------------------------|
| 1 8 | 2368 | • | - 1 | 2712—3 qrs. |
| 1 20 | 29 5 | | 30 | 33 9- |
| | 1, 5. 14—16 facit | | | 1. s. d. qes. 16-19-0-3 fa. |

Case 2.

8. When the given price of the Integer, is a part, or parts of a shilling (viz. pence) divide the given Number of Integers (whose value is sought) by the denominator, of the Fraction representing the even part, and the quote is shillings (always minding the 7th Rule of the 9th Chap.) and those shillings may be reduced into pounds by the 30 Rule of this Chapter. Example, Let it be required to find the value of 438 & at 3d. per l. I confider 3d. is $\frac{1}{4}$ of a shilling, and 438. will cost so many 3 pences, wherefore I divide 438 by 4 the denominator of $\frac{1}{4}$, and the quote is 109 shillings, and 2 remains, which is 2 three-pences or 6d. the whole value is 3l. 9s. 6d. as by the following work appeareth.

More Examples follow.

| • | • • |
|----------------------------|---------------------------|
| 1. d. 357 at 6 per 1. | l. d. 5316 at 2 per l. |
| 178 | 2 886 |
| facit 89 l. ms. | facit 44 t. 6s. |
| 1. d. 438 at 4 per l. | 1. d. 6389 at 1½ per l. |
| 14/6 | 79 8 - 7d. 1 |
| facis 7 1. 6 s. | facit 39 L 18 s. 7 d. 1 |
| 1. d. 1 879 at 3 per l. | 1. d. 11 88 at 1 per k |
| $\frac{1}{20}$ 21 9-9d. | 1 6 8 - 2 d |
| facit 101.19 1.9d. | facit 3 l. 8 s. 2 d. |

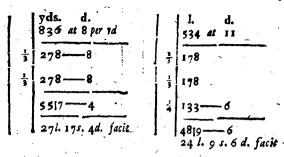
9. If the price of the Integer be pence under 123, and yet not an even part, then it may be divided into even parts, and so the parts of the given Number ta-

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Chap. 26.

ken accordingly, and added together, as if it were 5d. which is 3d. and 2d. viz. \(\frac{1}{2}\) and \(\frac{1}{6}\) of a fhilling, first take \(\frac{1}{4}\) of the given number, and then \(\frac{1}{6}\) thereof, and add them together, and their Sum is the Answer in shillings, still observing Rule 7. of Chap. 9. for the remainders (if any be) then bring the shillings into pounds by the 2d Rule foregoing. Likewise 7d. is \(\frac{1}{2}\) and \(\frac{1}{4}\), so 9d. is \(\frac{1}{4}\) and \(\frac{1}{4}\), and \(\frac{1}{6}\) and \(\frac{1}{2}\), and \(\frac{1}{3}\) and \(\frac{1}{3}\) and \(\frac{1}{4}\), and \(\frac{1}{6}\) is \(\frac{1}{2}\) and \(\frac{1}{3}\), and \(\frac{1}{4}\), and \(\frac{1}{6}\) is \(\frac{1}{2}\) and \(\frac{1}{3}\) of a shilling, or else many times your work may be shortned thus, viz. when the said given price is to be divided into even parts of a shilling or of a pound, after you have taken the first even part, the other may be an even part of that part, as in the next Example, where is given 439 l. at 5d. per l. now I may divide it thus, viz. into 4d. and 1d. and 4d. being \(\frac{1}{3}\) of 439 l. and it gives 1d. being \(\frac{1}{4}\) of 4d. I first take \(\frac{1}{3}\) of 439 l. and it gives 146 s. 4d. and for the 1d. I take \(\frac{1}{4}\) of 146 s. 4d. which is 26s. 7d. which in all comes to 9l. 2s. 11d.

which is 36s. 7d. which in all comes to 9l. 2s. 11d. Examples follow. yds at 9 per ya 439 at 5 per l. 208 146 104 31 2-18 2-11 151. 125 gd. facit 9 l. 2 s. 11 d. facit clis clis 286 at 10 at 7 pet eil 193 32 1 I s. 8 d. facit



Cafe 2.

10. When the price of the Integer is pence and farthings, if it make an even part of a shilling, work as before, but if they are uneven, as peny farthing, peny three farthings, 2d. 1qr. or 2d. 3qrs. or 3d. agrs. or the like, then fifft work for fome even part, and then consider what part the rest is of that even part, and divide that quotient thereby, then add them together, and reduce them

to pounds as before Example,3470l. at 1d. 1qr. per l. first I work for the peny by dividing 3470 by 12, for 1d. is - of a shilling, and the quote is 289 s. 2d.then I conceive that a farthing is the Lof a peny, and the value of one farthing will be i of the value at 1 peny, and therefore I take 4 of 289 s. 2 d. which is 72 s.

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3 d. 2 grs. and add them together, and they are 18 l. I s. 5d. 2 grs. as by the Margent, Other Examples of the same nature follow.

Cafe. 4.

off the figure in the place of Units of the given number, and double it for shillings, and the figures on the other hand are pounds, Example, 436 yds at 2s. per yd. cut off the last figure 6 and double it, it makes 12 shillings, and the other two figures, viz. 43, are so many pounds, so that there value is 43l. 12s. as per Margent.

Digitized by Google 12. Hence

12. Hence it is evident that when the given price of an Integer is an even number of shillings, then if you take half of that even number of shillings, and multiply the given number of Intogers thereby, doubling the first figure of the product, and setting it apart for skillings, the rest of the product will be pounds, which pounds and shillings is the value sought. Example, What cost 536 yds at 8s. per yd? To resolve which I take tof 8s. (the price of a yd.) which is a. and multiply 536 thereby, faying, 4 times 6 is 24, then I double the 536 yds at 8s. first figure 4, makes 8 for shillings, and carry 2 to the next product, drc. I find the rest of the product 214 1. 8s. to be 214, which I note for pounds so the value of 536 yds, at 8s. per yd. is 214 l. 8s. as per Margent. More Examples follow.

| 56 yds at 68. per yd. | 420 yds at 125. per yd. | | |
|-------------------------|-------------------------|--|--|
| 161. 16s. facit. | 2521. facit. | | |
| 123 yds at 4s. per yd. | 326 yds at 14s. per yd. | | |
| 241. 125. fácit. | 2281. 4s. facit. | | |
| 48 ells at 8s. per ell. | 48 yds at 16s. per yd. | | |
| 19l. 45. facit. | 381. 8s. facit. | | |
| 84 yds at 108. per yd. | 52 yds at 18s. per yd. | | |
| 42l. facit. | 461. 195. facit. | | |

13. If the given price of the Integer is an odd number of shillings, then work first for the even number of shillings by the last Rule, and for the odd shilling take 12 of the given number of Integers according to the 3 Rule of this Chapter, and add them together, and you have your desire. Examples sollow.

| yds. s. | ells s. |
|-------------------|--------------------|
| 422 at 3 per yard | 431 at 13 |
| 1. s. | l. s. |
| 42—4 | 258—12 |
| 21—2 | 21—11 |
| 63-6 facit. | 280-03 facit |
| ells. s. | ells. s. |
| 516 at 7 per ell. | 324 at 17 per ell. |
| 1. s. | 1. s. |
| 154——16 | 259—04 |
| 25——16 | 16—04 |
| 180-12 facit | 275-08 facit |

14. Except when the given price of the Integer is 5. for then it is sooner answered by taking \$\frac{1}{4}\$ of the given number whose value is sought, as in the following Example.

Case 5.

15. When the given price of an Integer is shillings and pence, or shillings, pence and farthings; then if the shillings and pence be an even part of a pound, divide the given number of Integers, whose value you seek by the denominator of that Fraction representing that even part. As for Example, what is the price of 384 yards at 6s. 8d. pr yard? Here I consider that 6s. 8d. is \(\frac{1}{3} \) of a pound, where-

17. When

The quote is the Answer, viz. 128 l.

To that 384 yds, at 6 s. 8d. per yd,
armounts to 128 l. as per Margent,

Itil observing the 7th Rule of the

More Examples follow.

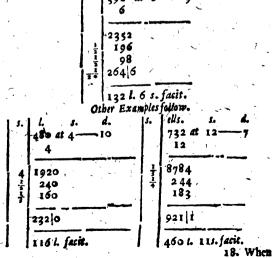
| 1/3 | 438 ells at 6's. 8 d. | 1/8 | 443 yds at 2 s. 6 d. | 55 l 7 s. 6 d. facit. | 525 at 3 s. 4 d. | 1/4 | 726 yds at 1 s. 8 d.

16. When the given value of the Integer is shillings and pence, and not an even part of a pound, yet many times it may be divided into parts (viz. 6s. 6d. is 4 s. and 2 s. 6 d. for the 4 s. work according to the 12th Rule foregoing, and for the 2 s. 6 d. take the

ther, then their fum is the value required.)
So 8 s. 6 d. will be divided into 6 s. and 2 s. 6 d.
and the price of the given Number may be found out
as before. Occ. Examples follow.

eighth part of the given Number, and add them toge-

17. When the given price of the Integer is shillings and pence, and you cannot readily divide them according to the last Rule, then multiply the given number whose value you seek by the number of shillings is. the price of the Integer, and then for the pence work by the 8th Rule foregoing, then add the Numbers together, and their Sum is the value fought in Chillings; as for Example, what is the value of 292 pds at 6 s. 9 d. per yd? Here 6 s 9 d. cannot be made any even part, nor indeed can it be divided into even parts of a pound; wherefore I multiply the given number of yards 392 by 6, for the 6s. the product is 2352 shillings, then for the 9d. I divide it into 6d. and 3d. and work for them by the 8th Rule foregoing, and at last add the shillings together, they make 2646 s. and by the 3d. Rule they are reduced to 132 l. 6 s. the value of 392 yds at 6 s. 9d.per yard. See the work following. yds.



18. When the given price of the Integer is shillings, pence and farthings, then multiply the given number of Integers by the number of shillings contained in the value of the Integer, and for the pence and farthings follow the 10th Rule of this Chapter.

Example.

| , , | | Exampl | f• | 1 |
|---------|---|--------|------|---|
| | yds. s. d. 438 at 8—63 | | | ells - s. d. 370 at 1424 14 |
| 1/21/8 | 3504 219 27—4 ¹ d. | | | 1480 370 |
| | 37510-41 | ` ' | 1 | 5180 d. |
| 1 | fac. 187 1. 10 s. 41 | i. | 4178 | 781 |
| _ | | | | 526 4-91 |
| | | | | fac.2631. 4s.9d. |
| # 6 = 4 | ells s. d. 136 at 9 2 5 8 | 1.5 | 80 | 31 at 2 4 ½ 2 62 62 62 62 7 7 8 62 7 8 64 7 8 65 7 8 65 7 8 65 7 8 65 7 8 65 8 7 8 65 8 7 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 |

Cafe

Case. 6.

19. When the given value of the Integer is pounds then multiply the Number of Integers, whose value fought by the price of the Integer, and the product the answer in pounds.

C. l. C. l. 13 at 8 per C.

84 l. facit. 104 l. facit.

C. l. 20 at 3 jer C. 48 at 12 per C.

90 l. facit. 576 l. facit.

case 7.

20. If the price of the Integer is pounds and shillings, then for the pounds work as in the last Rule and for the shillings as in the 12 and 13 Rules beforegoing, then add the Numbers produced from them both, and the Sum is the value sought.

Examples. grofs 228 IOS. 4 s. facit. 369 l. facit gross er of s 48 at 2-7 26 at 2-15 78 3 l. 65. 17----8 18-145. I S. 1 5. 194 li 6 s. facit 97 l. 10 s. facit 21. When

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21. When the given price of an Integer confifts of pounds, shillings, and pence, with farthings, then work for the shillings, pence, and farthings, first according to the 18th Rule of this Chapter, and find the total value of the given Number, as if there were no pounds, then work with the pounds according to the 19th Rule of this Chapter, and add the Numbers thus found, and their Sum is the total value required.

| | Examples of this C l. s. d. 213 at 1-13-4 1 | C l. s 37 at 3—8 | |
|--------------------|---|------------------------|---------------------|
| | 639 213 | 296 d. 186 | 8 s. 6 d. |
| 13 s. 3 d. | 2769 d. 533 | 9-3 4-7 ½ | 3 d. |
| $1 \frac{1}{2}d$. | 7 1/2 | $32/8-4\frac{1}{2}d$. | 1 |
| | 284 8101 | 16 l. 8s. | $4^{\frac{1}{2}}d.$ |
| 1 <i>l</i> . | 142 l. 08s. 10 ½ d. | 111 | 3 <i>l</i> . |
| 213 | 127 l. 8 s. 4 | d. fac | |
| ` | 355l. 8s. 101 d. facit | | |
| : * | grofs l. s. d. 416 at 2-9-3 ³ | grofs 1. 48 at 3— | s. d. |
| 3d. | 3744 104 26 | 240 48 720 | 15 5. |
| | | 16 | 6 d. |
| 11.5 | 387 4 | 6 | 1 1d. |
| 2 % | 193 L 14 s. 832 | 76 6 386 | - 2 l. |
| 17.00 | 1025 l. 14s. facit | 182 l. 6 s. fa | |

22. When there is given the value of an Integer, and it is required to know the value of many fuch Integers together, with 1 or 1 or 1 of an Integer, then first (by the former Rules) find out the Value of the given number of Integers, and then for 1 of an Integer take 4 of the given value of the integer, or for 1 take 1 of the given value of the Integer, and for I first take the & of the given value, and then & of that . fetting each part under the precedent, then adding them together, their Sum will be the required value of the Integers and their parts. Example; what is the value of 116 yds at 4 s. 6 d. per yard? To give an Answer, first I work for the

value of \$16 yds, by the 15th Rule foregoing, and then for the 1 jd I take 1 of 4 s. 6 d. which is 2 s. 3 d. and add to the rest found as before, then is that Sum the total value of

116 yds. at 4 s. 6 d. per yd. which I find to amount to 261. As. 2 d. as by the work in the Margent.

yds 1 16 at 4-14-10 d. 25. 6 d. 2-3 } ₹ jd.

26-4-3 facit.

Other Examples follow.

| 3247 /43. # 4 3. | 10 4. |
|-------------------|--------------------------|
| 1296 | 6 d. |
| | 4 d. |
| 1 56 7 5. | $\sqrt{2\frac{1}{2}d}$. |
| 78 1.7 5. 21 d. 1 | acit. |
| 228 ells at 12 s | . 11 d. |

12 s. 4 ď.

> 4 d. 3 d. ું લી. ·2‡ d. à ell.

295 4-48 d. 140 l. 14 s 8 d d. facit. 720 1 ydi. at 6 s. 8 d. 240 l. 3 s. 4 d. facit.

C. grs. 1. 28--3--14 at 1 141 .-IOS.

co-155. 1C. 75.6d. . G. 35.9d. 14%. 3 1. 6 s. 3d. facit.

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Many more questions may be stated, and several other Rules of Practice may be shewn according to the method of divers Authors, but what hath been delivered here are sufficient for the practical Arithmetician in all cases whatsoever.

C H A P. XXVII.

The Rule of Barter.

a. D Arter is a Rule amongst Merchants, which (in the exchanging of one Commodity for another) informs them fo to proportion their Rates as that

neither may fuftain lofs.

2. To relolve Questions in Barter, it will not be difficult to him that is acquainted with the Golden Rule, or Rule of 3, it being altogether used in resolation ving such Questions.

Queft. 1. Two Merchants (viz. A and B) Barter, A hath 12 C. 2 grs. 14 l. of Pepper at 2l. 16s. per C. and B hath Cotton at 9d. per l. I demand how much

Cotton B must give A for his Pepper?

Answer, 9 C. 1 gr. First, find by the Rule of 3, or the Rules of Practice foregoing, how much the Pepper is worth, faying,

If I C. cost 21. 16s. what will 12 C. 2 grs. 141.

floa

Answer, 38 l. 17 s.

Secondly, By the Rule of 3 say, If 9d, buy 11. of

Cotton, how much will 381. 17s. buy?

Answer, 9 to and so much Cotton must B give to A for 13 C. 3 qrs. 14 l. of Pepper at 21, 16s. per Cent. when the Cotton is worth od. per l.

146 Quest. 2. Two Merchants (A and B) barter, A hath

Ginger worth 1 l. 17 s. 4 d. per C. but in barter he will have 2 l. 16 s. per C. B hath Nutmegs worth 5 l. 12 s. per C. now I demand how B must rate his Nutmess per C. to make his gain in barter equal to that of A?

Answer. 8 1. 8 v.

Say, by the Rule of Three, If 1 l. 17 s. Ad. require 2 1. 16 s. in barter, what will 5 L 12 s. require in barter ?

Facit. 8 1. 8 s.

• Quest. 3. A and B barter, A hath 120 yards of Broadcloth worth 6 s. per yd. but in barter he will have 8 s. per yd. B hath Shalloon worth 4 s. per yd. now I demand how many yards of Shalloon B must give A for his Broad-cloth, making his gain in barter equal to that of A?

Answer, 180 yds of Shalloon.

First (as in the last question) find out how Bought to fell his Shalloon in barter, viz. fay, If 6 s. require 8 s. what will 4 s. require?

Answer, 5 s. 4 d.

Thus you see that B must sell his shalloon in barter at e s. 4 d. if A fell his Broad-cloth at 8 s. per yd.

. It remaineth now to find out how much Shalloon B must give for 120 yards of Broad-cloth, which after the same method used to resolve the first question of this Chapter is found to be 180, and so many yards of Shalloon must B give A for the 120 yards of Broadcloth.

-Quest. 4. A and B bartered, A had 14 C. of Sugar worth 6 d. per 1. for which B gave him 1 C. 3 grs. of. Cinnamon I demand how B rated his Cinnamon Der 1.

Answer, 4 s. per l.

Quest. 5. A and B barter, A hath 4 Tun of Brandy worth 27 l. 16 s. ready Money, but in barter he hath 50 1. 8 s. per Tun, and A giveth B 21 C. 2 grs. 114 1. of Ginger for his 4 Tun of Brandy, I defire to know how B fold his Ginger in barter per C. and how much it was worth in ready Money.

Answer. Digitized by Google

Chap. 28. Questions in Loss, &c.

Answer, For cl. as. and 8d in barter, and it was

Queft. 6. A and B barter. A hath 220 doxen of Candles at 4s. 6d. per dozen, for which, B giveth him 30l. in Money, and the rest in Cotton at 8d. per 1. I demand how much Cotton he must give him more than the 201.

Answer, 11 C. 1 gr.

Quest. 7. A and B barter. A hath 608 yards of broad Cloth worth 14s. per yd, for which B giveth him 125l. 12s. ready Money, and 85l. 2 qrs. 24l. of Bees Wax, now I defire to know how he reckoned his Wax per C.

Answer, 3l. 10s. per C.

CHAP. XXVIII.

Questions in-Loss and Gain.

Merchant bought 436 yards of broadit again at tos. 4d. per yard, now I desire to know how much he gained in the Sale of the 426 yards?

Answer, 391. 19s. 4d.

First find out by the Rule of Three, or by practice, how much the Cloth coft him at 8s. 6d. per yd. which I find to be 1851. 65. then by the same Rule find out how much he sold it for, viz. 2251. 55, 4d. then subtract 1851, os. which it cost him, from 2251, 55-4d, which he sold it for, and there remaineth 201. 10s. 4d. for his gain in the Sale thereof

Otherwise it may sooner be resolved thus, first find out how much he gained per jd. viz. subtract \$6.64. which he gave per jd, from 10s. 4d. which he sold it for per yd. the remainder is 13. 10d. for his gains per

yd, then fay,

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If 1 yd gain 1 s. 10 d. what will 436 yds gain? The Answer by Practice, or the Rule of Three is 39 l. 19 s. 4 d. as was found before.

Quest. 2. A Draper bought 124 yds of Holland Cloth, for which he gave 31 h. I defire to know how he must fell it per yard to gain 10 h. 6 s. 8 d. in the whole Sale of the 124 yds? Answer, at 6 s. 8 d. per yard.

Add the price which it cost him, (viz. 31 l.) to his intended gain, (viz. 10 l. 6 s. 8 d.) the sum is 41 l.

6 s. 8 d. then fay,

If 124 yds require 41 l. 6 s. 8 d. what will 1 yd require? By the Rule of Three I find the Answer 6 s. 8 d.

Quest. 3. A Grocer bought 3. C. 1 qr. 14 l. of Cloves, which cost him 2 s. 4 d. per l. and sold them for 52 l. 14 s. I desire to know how much he gained in the whole, Answer, 8 l. 12 s.

Quest. 4. A Draper bought 86 Kerseys for 129 l. I demand how he must sell them per piece to gain 15 L in laying out 100 l. at the rate? Answer, 1l. 145- 6d.

ter piece; for,

As roo l. is to 115 l. so is 129 l. to 148 l. 7 s. So that by the proportion above, I have found how much he must receive for the 86 Kerseys to gain after the rate of 13 l. per C. then to find how he must sell them per piece. I say,

As 86 pieces are to 148 l. 7 s. fo is a piece to 1 l.

14's. 6 d, which is the number fought.

Quest. 5. A Grocer bought 4. C. of Pepper for 15 l. 37 s. 4 d. and (it proving to be damnified) is willing to lose 12 l. 10 s per Cent. I demand how he must sell it per l. Answer, 7 d. per l.

Subtract 121. 101. the los of 100 L from 100 l.

and there remains 87 1: 10 s. then fay,

As reo 4 is to 87 l. 10 s. so is 15 l. 17 s. 4 d. to 13 l. 17 s. 8 d. so much as he must sell it all for to sose after the rate propounded, then to know how he must sell it per h. I say,

As 13 4 17 5 6 de is to 44 C. lo is 11. to 7 d.

Quest.

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Quest. 6. A Plummer fold to Fodder of Lead (the Fodder containing 19 C.) for 2041. 15s. and gained after the rate of 121. 1cs. per 10cl. I demand how much it cost him per C? Answer, 181. 84.

To refolve this question add 121. 10s. (the Gainper Cent.) to 1001, and it makes 1121, 10s. then

fay,

As 112 l. 10s. is to 10cl. so is 204l. 15s. to

Which 1821, is the Sum it cost him in all, then reduce your 10 Fodders to half hundreds, and it makes

390, then fay,

As 390 half hundreds is to 1821. So is 2 half hundreds to 185. 8d. the price of 2 half hundreds, or one C. weight, and so much it stood him in per C.

weight.

Quest. 7. A Merchant bought 8 Tuns of Wine, which being sophisticated, he select for 400l. and loseth after the rate of 12l. in receiving 100l. now I demand how much it cost him per Tun? and how he selleth it per Gallon to lose after the said rate? Answer, it cost 56l. per Tun, and he must sell it at 2s. 11d. 2 10 grs. per Gallon to lose 12l. in receiving 100l.

To resolve this question, I consider in the first place, that in receiving rool. he loseth 121. therefore 10cl. comes in for 1121. laid out, wherefore to find how

much he laid out for the whole, I say,

As rool. is to 112l. so is 40ol. to 448l. and so much the 8 Tuns cost him, then to find how much it cost per Tun, I say,

As 8 is to 4481, so is 1 to 561, the price it cost par

Tup.

Now to find how he must fell it per. Gallon, reduce the 8 Tuns into Gallons, they make 2016, then say,

As 2016 Gallons is to 400l. so is 1 Gall. to 3s. 11d. 214 qrs. the price he must sell it at per Gallon to lose. as aforesaid.

K.,4

Quest.

200 Quest. 8. A Merchant bought 8 Tuns of Wine, which

being sophisticated, he is willing to sell for 400 %. and loseth at that rate 12 % in laying out 100 % upon the same, now I demand how much it cost him per Tun?

Here I confider that for 100 l. laid out, he receiveth but 88 /. therefore to find what the 8 Tuns coff him, I fay,

As 88 1. is to 100 1. fo is 400 1. to 454-f the price it all cost him, then to find how much per Tun, I say,

As 8 is to 454 25 1. So is 1 to 56 25, or 56 1. 16 s. 4 d. set ar. per Tun.

CHAP. XXIX.

Equation of Payments.

Quation of Payments, is that Rule amongst Merchants whereby we reduce the times for payment of several Sums of Money, to an equated time for the payment of the whole Debt without dam. age to Debtor or Creditor, and

The Rule is.

2. Multiply the fums of each particular payment by is respective time, then add the several products together, and their Sum divide by the total Debt, and the quotient thence arising is the equated time for the payment of the whole debt. Example,

Quest. 1. A is indebted to B in the sum of 1301. whereof 50 1. is to be paid at 2 Months, and 50 1. 4 months, and the rest at 6 months, now they agree to make one payment of the total Sum, the question is what the equated time for payment without damage

to Debtor or Creditor?

Chap. 29. Equation of Payments. 201

To refolve this Question I multiply each payment by its time, viz.

| 50 l. | multiplied | <i>by</i> . 2 | mon. | produceth—100 |
|-------|------------|---------------|------|------------------|
| 50 l. | multiplied | by 4 | mon. | produceth200 |
| 30 l, | multiplied | by 6 | mon. | produceth —— 180 |

The Sum of the product is ______480.

Then I divide 480 (the Sum of the Products) by 130 (the total Debt) and the Quotient is 37? months

for the time of paying the whole Debt-

Quest 2. A Merchant hath owing him 1000 l. to be paid as followeth, viz. 600 l. at 4 months, 200 l. at 6 months, and the rest (which is 200 l.) at 12 months, and he agreeth with his Debtor to make one payment of the whole, I demand the time of payment without damage to Debtor or Creditor?

600 l. multiplied by 4 months is 2400
200 l. multiplied by 6 months is 1200
200 l. multiplied by 12 months is 2400

The Sum of the Product is -----6000

and the Sum of the product (6000) being divided by the whole Debt (1000).) quotes 6 months for the time of payment of the whole Debt.

2. The truth of this Rule is thus manifest, if the

interest of that Money which is paid (by the equated time) after it is due, be equal to the interest of that Money which (by the equated time) is paid to much sooner than it is due at

any rate per C. then the Operation is true, otherwise

not. Example.

In the last Quest. 600 L. should have been paid at 4 months, but it is not discharged till 6 months (that is two months after it is due) wherefore its interest for 2 months at 6 per Cens. per Annum is 6 L. and then

K 5 Digitized by Google 2006

The Proof of the

Rule of Equation

of Payments.

2001. was to be paid at 6 months, which is the equated time for its payment, therefore no Interest is reckoned for it, but 2001. should have been paid at 12 Months, but it is to be paid at 6 months, which is 6 months sooner than it ought, wherefore the interest of 2001. for 6 months is 61. (accounting 61. per Cent. per Annum) which is equal to the interest of 6001. for 2 months, wherefore the work is right.

Quest. 3. A Merchant hath owing him a certain sum to be discharged at 3 equal payments, viz. f at two Months, f at four months, and f at 8 months, the question is, what is the equated time for the payment

of the whole Debt?

In questions of this nature, (viz. where the Debt is divided into equal or unequal parts) each of the parts is to be multiplied by its time, and the sum of the product is the Answer,

Multiplied by 2 mon. produceth 14 Multiplied by 4 mon. produceth 14 Multiplied by 8 mon. produceth 23

The Sum of the Products is 43

which is 43 months for the equated time of payment. If infless of the Fractions (representing the parts) you had wrought by the numbers themselves (represented by those parts) according to the lirst and second Examples, it would have been the same Answer, as suppose the Debt had been 90 s. then \$ of it is 30 for each payment, viz, at 2, 4, and 8 months, then

30 1. Multiplied by 2 mon. producetb 60 30 1. Multiplied by 4 mon. producetb 120 30 1. Multiplied by 8 mon. producetb 240

The Sum of the Products is 420

which divided by 90 (the whole Debt) quateth 45% or 43 mouths as before.

Quest. 4. A Merchant oweth a Sum of Money to be paid 4 at 5 months, and 4 at 8 months, and 4 at 10 months, and he agreeth with his Creditor to make one total payment; I demand the time, without damage to Debtor or Creditor? Work as in the last Question, and you will find the Answer to be 7 months.

Quest. 5. A is indebted to B 640 l. whereof he is to pay 40l. present money, and 350l. at 3 months, and the rest (viz. 250l.) at 8 months, and they agree to make an Equated time for the whole payment?

now I demand the time?

In questions of this nature (viz. where there is ready money paid) you are in Multiplying, to neglect the money that is to be paid present, and work with the rest as is before directed, and divide the sum of the products by the whole Debt, and the Quote is the Answer: For here 4cl. is to be paid present, and hath no time allowed, and according to the Rule it should be multiplied by its time, which is (0) therefore 40 times 0 is 0, which neither augmenteth nor diminishesh the Dividend; wherefore (to proceed according to direction) I say,

350 by 3 Months produceth——1050 250 by 8 Months produceth——2000

The Sum of the product is _____ 3050

which divided by 640, the whole Debt, the quote is

429 Months, the time of payment.

Quest. 6. As is indebted to B in a certain Sum, \frac{1}{2} whereof is to be paid present Money, \frac{1}{2} at 6 months, and the rest at 8 Months, now I demand the equated time for the payment of it all?

Answer 31 months is the time of payment.

Quest. 7. A is indebted to B 120st. whereof $\frac{1}{2}$ is to be paid at 3 months, $\frac{1}{4}$ at 6 months, and the rest at 9 months; what is the equated time for the payment of the whole Sum?

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Antier,

Answer, 61 months.

Quest. 8. A is indebted to B 4201. which is due at the end of 6 months, but A is willing to pay him 14cl. prefent, provided he can have the remainder forborn fo much the longer to make satisfaction for his kindness, which is agreed upon, I desire to know what time ought to be allotted for the payment of the

2801. remaining?

To resolve this question, sirst, and out what is the interest of 1401. for the time it was paid beforeit was due, at 6 per Cent. (or any other rate) viz. 6 months) and you will find it to be 41. 45. Then it is evident that the remaining 2801. must be detained so much longer than 6 months as the while it may eat out that interest, viz. 41. 45. which is thus found out, viz. First, see what is the Interest of 2801. for a mouth, or any other time; but here we will take one month. and its Interest, for one month is 28s.

Then by the Rule of Three, say,
As 28s. is to 1 month, so is 84s. to 2 months; so that the 2801: remaining must be kept 3 months, beyond its first time of payment (viz. 6 months) which added the eto, makes 9 months, at the end of which time A ought to make payment of the remainder.

CHAP. XXX.

EXCHANGE.

how to exchange informeth Merchants how to exchange Moneys, Weights, or Measures of one Country into (or for) the Moneys, Weights, or Measures of another Country, and when the Rate, Reason, or Proportion betwixt the Money, Weights, or Measures of different Countrys is known, it will not be difficult for the Practitioner that is well acquainted with the Rule of proportion (or Rule of Three) to resolve any Opesion wherein it is required. Three) to resolve any Question wherein it is required Digitized by Google

to Exchange a given quantity of the one kind into the same value of another kind.

2. In Questions of Exchange there is always a comparison made between the Coyns, Gre. of two Coun-

tries (or kinds) or of more.

3. In Questions where there is a comparison made between two things (whether they be Moneys, Weights, (%c.) of different kinds or (Countries) there may be a folution found by a fingle Rule of Three, as may appear by the following Example.

Quest. 1. A Merchant at London deliver'd 370 l. Sterling, to receive the same at Paris in French Crowns; the Exchange 3 French Crowns per pound Sterling. I demand how many French Crowns ought he to receive?

In placing the numbers observe the 6th Rule of the 10th Chapter, which being done, the given numbers will stand thus,

_____ 3 ____

and being reduced according to the Rules of the 24th Chapter, will stand thus ;

l. Crowns l. Crowns
As # is to 19 fo is 370 to 1233;

So that I conclude he ought to receive 1233; French Crowns at Paris for 370 L. delivered at London.

Queft. 2. A Merchant delivered at Amsterdam 587 1. Flemish to receive the value thereof at Naples in Ducats; the Exchange 44 Ducats per I. Flemifb. I demand how many Ducats he ought to receive?

The proportion is as followeth.

l. Ducats l. As # is to 24 fo is \$ \$2 to 2817 #.

So I find he ought to receive 28174 Ducats at Naples,

for the 587 l. Flemish delivered at Amsterdam.

Quest.4. A Merchant at Florence delivereth 3478 Ducatoons, to receive the value at London in pence, the Exchange 52½ pence Sterling per Ducatoon. I demand how much Sterling he ought to receive? The

The Proportion for Resolution is,

Duc. d. Due. d. As \(\frac{1}{2} \) is to \(\frac{1}{2} \) fo is \(\frac{1}{2} \) to 186073

which is equal to 7751. $6^{-\frac{1}{2}}$ for the Answer.

I might here (according to the Custom of Arithmetical Writers) lay down Tables for the Reduction of Foreign Coyns to English; but by Reason of their Instability (for they continue not at a constant standard, as our Sterling Money doth, but are sometimes raised, and sometimes depressed I shall forbear.

4. When there is a comparison made between more than two different Coyns, Weights or Measures, there ariseth ordinarily two different cases from such a com-

parison.

r. When it is required to know how many pieces of the first Coyn, Weight or Measure, are equal in value to a known number of pieces of the last Coyn,

Weight or Measure.

2. When it is required to find out how many pieces of the last Coyn, Weight or Measure, are equal in value to a given Number of the first fort of Coyn, Weight or Measure.

An Example of the fuft Casemay be this, V.I Z.

Quest: 4. If 150 pence at London are equal to 3 Ducats at Naples make 34½ shilings at Brusses; then how many pence at London are equal to 138.shillings at Brussels? Facit, 960 do.

This question may be refolyed at two single Rules

of Three; for first, I say,

If † Ducass at Naples make 150 pence at London, how many pence will 4 Ducats make?

Auswer, 240 penee.

By the foregoing Proportion, we have different ed that 42 Ducats at Naples make 240 peace at Landan. London: And by the Tenour of the Question we see. that 44 Ducats at Venice make 34. Ihillings at Bruffels, therefore 24od. at London are equal to 34!s. at Bruffels. (for the things that are equal to one and the same thing are also equal to one another) wherefore we have a way laid open to give a folution to this Question by another fingle Rule of Three, whose proportion is,

As 34½ thillings at Bruffels is to 240 pence at London, to is 138 shillings at Bruffels to 960 pence at Lan-

don, which is the Answer to the Question.

An Example of the second Case may be thus. VIZ.

Queft. s. If 401. Averdupois weight at London is equal to 361. weight at Amsterdam, and 901. at Amsterdam makes 1161, at Dantzick, then how many pounds at Dantzick are equal to 1121. of Averdupois weight at London.

Answer, 1291 pounds at Dantzick.

This Question is likewise answered at two single Rules of Three, viz. First, I say,

As 36l, at Amflerdam is to 40l. at London,

So is gol. at Amsferdam to 1001. at London.

And by the question you find that gol. at Amsterdam is 1161, at Duntzick, and therefore 1001, at London is. likewise equal thereueto, wherefore again, Lsay,

As 10cl. at London is to 1161: at Dantzick, So is 1121, at London to 129 1 1. at Dantzick.

By which I find that 129 13 at Dantzick are equal to

પાંદ્ર

5. There is a more speedy way to resolve such Que-Rions as are contained under the two Cases beforementioned, laid down by Mr. Kerfey in the third Chapter of his Appendix to Mr. Wingate's Arithmetick, where he hath given two Rules for the Resolution of the Questions pertinent to the two said Cales

6. But I shall lay down a general Rule for the solution of both Cofes; and first, let the Learner observe the following Directions in placing of the given terms,

Exchange.

7. Let there be made two Columns, and in their Columns to place the given terms one over the other, as that in the same Column there may not be found two terms of the same kind one with the other.

Having thus placed the terms, the general Rule is. Observe which of the said Columns hath the most terms placed in it, and multiply all the Terms therein continually, and place the last product for a dividend; then multiply the terms in the other Column continually, and let the last product be a Divisor, then divide the said Dividend by the said Divisor, and the Quotient then arising is the Answer to the Ouestion.

So the Example of the first of the said Cases being again repeated, viz. if 150 pence at London make 3 Ducats at Naples, and 43 Ducats at Naples make 34; shillings at Bruffels, then how many pence at London

are equal to 138 shillings at Brussels?

The terms being placed according to the 7th Rule

will stand as followeth.

| Pence at Lond. Ducats at Na. Shill. at Bruff. 138 having thus placed the Terms that in either Column there is two terms of one kind, then observe that the Column under A hath most terms in it, therefore they must be multiplied together for a dividend; 217. 150 multiplied by 43 produceth 3600, which multiplied by 138 produceth 496800, for a dividend, then in the Column under B there are 3 and 341, which multipli- |
|---|
| having thus placed the Terms that in either Column there is two terms of one kind, then observe that the Column under A hath most terms in it, therefore they must be multiplied together for a dividend; viz. 150 multiplied by 44 produceth 3600, which multiplied by 128 produceth 496800 for a dividend, then in the |
| having thus placed the Terms that in either Column there is two terms of one kind, then observe that the Column under A hath most terms in it, therefore they must be multiplied together for a dividend; viz. 150 multiplied by 44 produceth 3600, which multiplied by 128 produceth 496800 for a dividend, then in the |
| there is two terms of one kind, then observe that the Column under A hath most terms in it, therefore they must be multiplied together for a dividend; viz. 150 multiplied by 44 produceth 3600, which multiplied by 128 produceth 496800 for a dividend, then in the |
| there is two terms of one kind, then observe that the Column under A hath most terms in it, therefore they must be multiplied together for a dividend; viz. 150 multiplied by 44 produceth 3600, which multiplied by 128 produceth 496800 for a dividend, then in the |
| Column under A hath most terms in it, therefore they must be multiplied together for a dividend; viz. 150 multiplied by 44 produceth 3600, which multiplied by 128 produceth 496800 for a dividend, then in the |
| must be multiplied together for a dividend; wiz. 150 multiplied by 44 produceth 3600, which multiplied by 128 produceth 496800 for a dividend, then in the |
| multiplied by 44 produceth 3608, which multiplied by |
| 128 produceth 496800 for a dividend, then in the |
| Column under B there are 2 and 341, which multipli- |
| |
| All a median 207 for a division, then having |
| ed together produce 20% for a divisor; then having |
| divided 49600 by 107, the quotient is 960 pence for |
| the answer as before. |

Again, let the Example of the second Case be again repeated, viz It 40 l. Averdupois weight at London make 361 weight at Amsterdam, and 901. at Amsterdam make 116 l. at Dantziek, then how many pounds at Dunt zick are equal to 1124, Averdupois weight at Las-

The terms being disposed according to the 7th Rule foregoing will stand thus,

> l. at Lond. 40 36 l. at Amsterdam l. at Amst. 90 116 l. at Dantziek l. at London.

whereby I find that the Terms under B multiplied together produce 467712 for a dividend, and the Terms under A, viz. 40 and 90 produce 3500 for a divisor, and Division being finished, the quotient giweth 1293312 pounds at Dantzick for the Answer.

CHAP. XXXI.

Single Position.

Egative Arithmetick, called the Rule of False, is that by which we find out a truth, by numbers invented or supposed, and this is either single or double.

2. The Rule of Single Position is when at once, vizby one false position, or seigned number, we find out

the true number fought.

3. In the fingle Rule of False, when you have made choice of your position, work it according to the te-nour of the question, as if it were the true number fought, and if by the ordering your position you find the result either too much or too little, you may then find out the number fought by this proportion following, viz.

As the result of your position is to the position, so is the given number to the number sought.

Example.

Quest. 1., A person having about him a certain number of Crowns, faid, if the fourth and third and fixth of them were added together, they would make just 45 ; now I demand the number of Crowns he had about him? Answer, 60 Growns.

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To refolve this question, I suppose he had 24 Crowns (or any other number that will admit of the like division) now the fourth of 24 is 6, and the third is 8, and the fixth is 4, all which parts, (viz. 6, 8, and 4) being added together make but 18, but it should be 45, wherefore I say by the Rule of Three,

As 18, the Sum of the parts is to the position 24, to is 45 the given number to 60, the true number

fought.

For the fourth of 60 is 15, and the third of 60 is 20, and the fixth of 60 is 10, which added together

make 45.

Quest. 2. Three Persons, viz. A, B, C, thus discourse together concerning their Age, quoth B to A, I am as old and half as old again as you, then quoth C to B, I am twice as old as you, then quoth A to them, and I am sure the Sum of all our Ages is 165, now I demand each Man's Age? Answer, A 30, B 45, C co years of Age, which added together, make 165.

CHAP. XXXII.

Deuble Position.

Politions are assumed to give a Resolution to the question propounded.

2. When any Question is stated in double Position

make fuch a Cross as followeth.

⁴X^b

3. Then make choice of any number you think may be convenient for your working, which call your first position, and place it at that end of the Crois at a, then work with this position (as if it were the true number

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number fought) according to the nature of your queflion, then having found out your erron, either too much or-too little, place it on that fide the Cross at d, then make choice of another number of the same denomination with the first Position (which call your second Position) and place it on that fide of the Cross at b; then work with this Polition as with the former, and having found out your error, either too much or too little, place it on that fide of the Cross at c. and then the Politions will fland at the top of the Groß, and the errors at the bottom, each under his correspondent Position, and then multiply the errors into the position's cross-wife, that is to say, mu'tiply the first position by the second error, and the second position by the first error, and put each product over its position.

4. Having proceeded to far, then confider whether the errors were both alike, that is, whether they were both too much, or both too little, and if they are alike, then subtract the lesser product from the greater, and let the remainder for a dividend, then fubtract the leffer error from the greater, and let the remainder be a divisor, then the quotient arising by this Division.

is the answer to the question.

5. But if the errors are unlike, that is one too much and the other too little, then add the products of the politions and errors together, and their lum shall be a dividend, then add the errors together, and their fum shall be a divisor, and the quotient arising hence is the Answer; which two last Rules may be kept in

memory by this Verse following, viz.

When Errors are of unlike kinds Addition doth ensue. But if alike Subtraction finds Dividing work for you.

Quest. 1. A, B and C build a House which cost 76 L. of which A paid a certain Sum unknown, B paid

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B paid as much as A, and rol. over, and C paid as much as A and B, now I defire to know each Man's

share in that charge ?

Having made a cross according to the second Rule, I come according to the third Rule to make choice of my first position; and here I suppose A paid 61. which I put upon the cross as you (ce, then B paid 161. (for it is said he had paid 10 1. more than A) and C paid 221, for 'tis faid he paid as much as A and B, then I add their parts.

| | * | |
|--------------|-----------------------------|---------------|
| L. | | <i>t</i> , ' |
| L . 9 | · • | A 6 |
| 19 | | В 16. |
| 28 | 120 168 288 | C 22 |
| | 6女アタ | |
| 56 | 6 12) 32 (14 20 | Sam 44 |
| 76 | 12 | 76 |
| 76 56 | | 44 |
| 20 | , F | Error 32 |

and they amount to 44, but it is said they paid 761. wherefore it is 32 too little, which I note down at the bottom of the cross under its position for the first

Secondly, I suppose A paid of. then B paid 191. and C 281. all which added together make 56, but they should make 76, wherefore the Error of this position is 20, which I put at the bottom of the cross under his position for the second Error, then I multiply the Errors and the positions cross-wife, viz. 22 (the Error of the first position) by 9 (the second pofition) and the product is 288. Then I multiply 20-(the Error of the second position) by 6 (the first position) and the product is 120.

Then (according to the 4th Rule) I subtract the leffer product from the greater (viz. 120 from 288, because the Errors are both alike, viz. too little)

and

and there remaineth 168 for a Dividend, then I subtract 20 (the lesser Error) from 32 (the greater Error) and the remainder is 12 for a divisor, then divide 168 by 12, and the Quotient is 14 for the Answer, which

is the share of A in the Payment.

6. Again Secondly, If the Errors had been both too big it had had the same effect, as appeareth by the following Work; for first I suppose A paid 201. then B paid 301. and C 501. which in all is 100, but it should have been no more than 76, wherefore the first Error is 24 too much. Again, I suppose A paid 181. then B must pay 281. and C must ray 461. which in all

| 24 Error | 8 | Error | <u>.</u> |
|----------------------|---------------------------------|---------------|----------|
| 100 Sum 76 Subtr. | 8) (14 facit | Súm Subtr. | |
| 50 C | 320 112 432 20 T 7 18 | C | 46 |
| 30 B | | В | 28 |
| 20 A | | A | 18 |

is 921. but it should have been but 761. wherefore the second Error is 16 too much: then I multiply 20 (the first Position) by 16 (the second Error) and the product is 320; again I multiply 18 (the second Position) by 24 (the first Error) and the product is 432, Then because the Errors are both too much, I subtract 320 the lesser product (from 432 (the greater product) and there remaineth 112 for a dividend, likewise I subtract 16 (the lesser Error) from 24 (the greater Error) and the difference is 8 for a divisor, then perform Division, and the quotient is 14 (as before) for the answer.

Again Thirdly, If the Errors had been the one too big and the other too little, Respect being had to the 5th Rule foregoing, the Answer would have been the same; as thus, I take for my first Position 6, and then the Error is 32 too little, then I

take for my second position 18, and then the error is 16 too much, then I multiply the positions and errors cross-wife, and the products are of and e76. and because the Errors are unlike.



(viz) one too big, and another too little, I add the products 96 and 596 together, and their Sum is 672 for a dividend; I likewise add the errors 32 and 16 together, and their sum is 48 for a Divisor, then having simpled Division, I find the Quotient to be 14, which is the answer as was found our at the two feveral Tryals before.

| For proof of the Work I fay, | |
|------------------------------|----------------------|
| If A paid | 1. 14 24 38 |
| The Sum of all is- | 76 |

which is the total value of the building, and equal to

the given number.

Those who desire to see the demonstration of this Rule, let them read the 7th Chap. of Mr. Kerfey's Appendix to Wingate's Arithmetick, Petiscus in the 4th Book of Trigonometria. Or Mr. Oughtred in his Clauk Mathematica.

Quest. 2. Three Persons, A, B, C, thus discoursed together concerning their Age; quoth A I am 18 years of Age, quoth B I am as old as A and & C; and quoth C, I am as old as you both, if your years were added together. Now I defire to know the Age of each person? Answer, A is 18, B is 54, and C is 72 years of Agc.

Quest. 3. A Pather lying at the point of Death, left to his 3 Sons, viz. A, B, C, all his Estate in Mohey, and divideth it as followeth, viz. to A he gave 1 wanting 441. to B he gave 1 and 141. over, and to C he gave the remainder, which was 821, less than the thare of B, now I demand what was the Sum left. and each Man's part? Answer, The Sum bequeathed was 5881 and whereof A had 2501 B had 2101. and C had 1281.

Quest. 4 Two persons, viz. A and B had each in their hands a certain number of Growns, and A faid to B, if you give me one of your Crowns I shall have five. times as many as you; and faid B to him again, if you give me one of yours, then we shall each of us have an equal number; now I demand how many Crowns had each person? Answer, A had 4, and B had 2 Crowns.

Quest. 5. What number is that unto which if I add of it self, and from the Sum subtract 4 of it self, the remainder will be 216 ? Answer, 192.

Many more questions may be added, but these well underftood, will be fufficient, (even for the meaneft Capacity) for the Resolution of any other question per-

tinent to this Rule.

There may be an objection made because we have not treated particularly upon Interest and Rebate, but the operation of fuch Questions being more applicable to Decimals, are omitted, till we come to acquaint the Learner therewith.

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